
2016 SIMP L1L1 Unblinding Proposal

Alic Spellman

Cameron Bravo + Matt G

07/23/2024

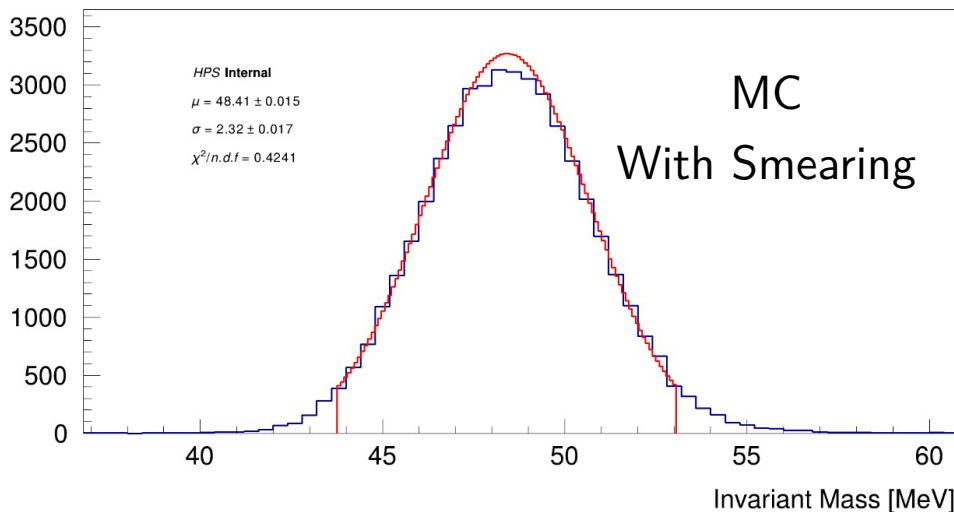
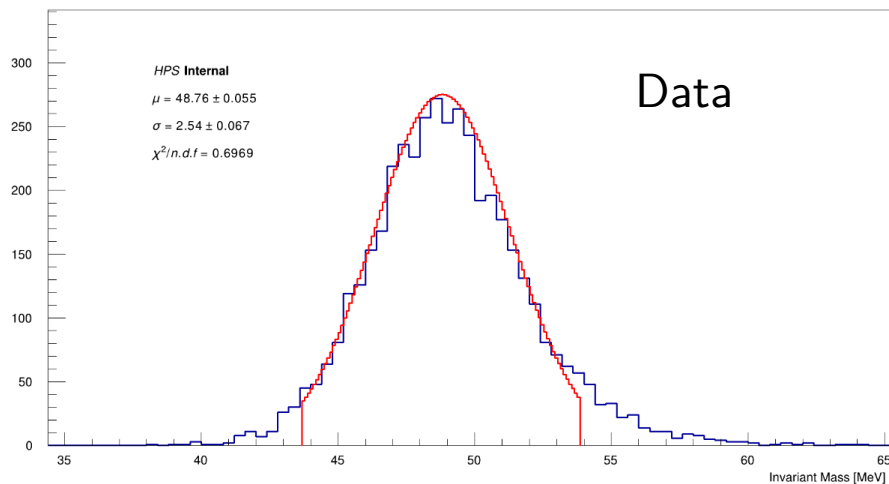


Introduction

- Request to unblind 100% SR data for 2016 L1L1 SIMPs
- Hit killing + momentum smearing applied to all MC samples
- MC background and Data agree well
- RadFrac + RadAcc + Mass resolution updated
- Full selection optimized using 10% Data in SR
- Background estimation and search window size studied using 10% Data in SR
 - Performance also tested on larger stats 100% **CR**
- * $z_{0\min}$ cut shape was optimized using 10% data SR
 - Studied impact of further tightening cut to protect against statistical fluctuations in the 100% data SR
 - Decided to tighten...**remaining events in 10% data now SR very low**
- OIM method sets upper limits on expected signal rate

Mass Resolution with MC Momentum Smearing

Moller Peaks with Momentum Smearing



Unconstrained Vtx KF Tracking

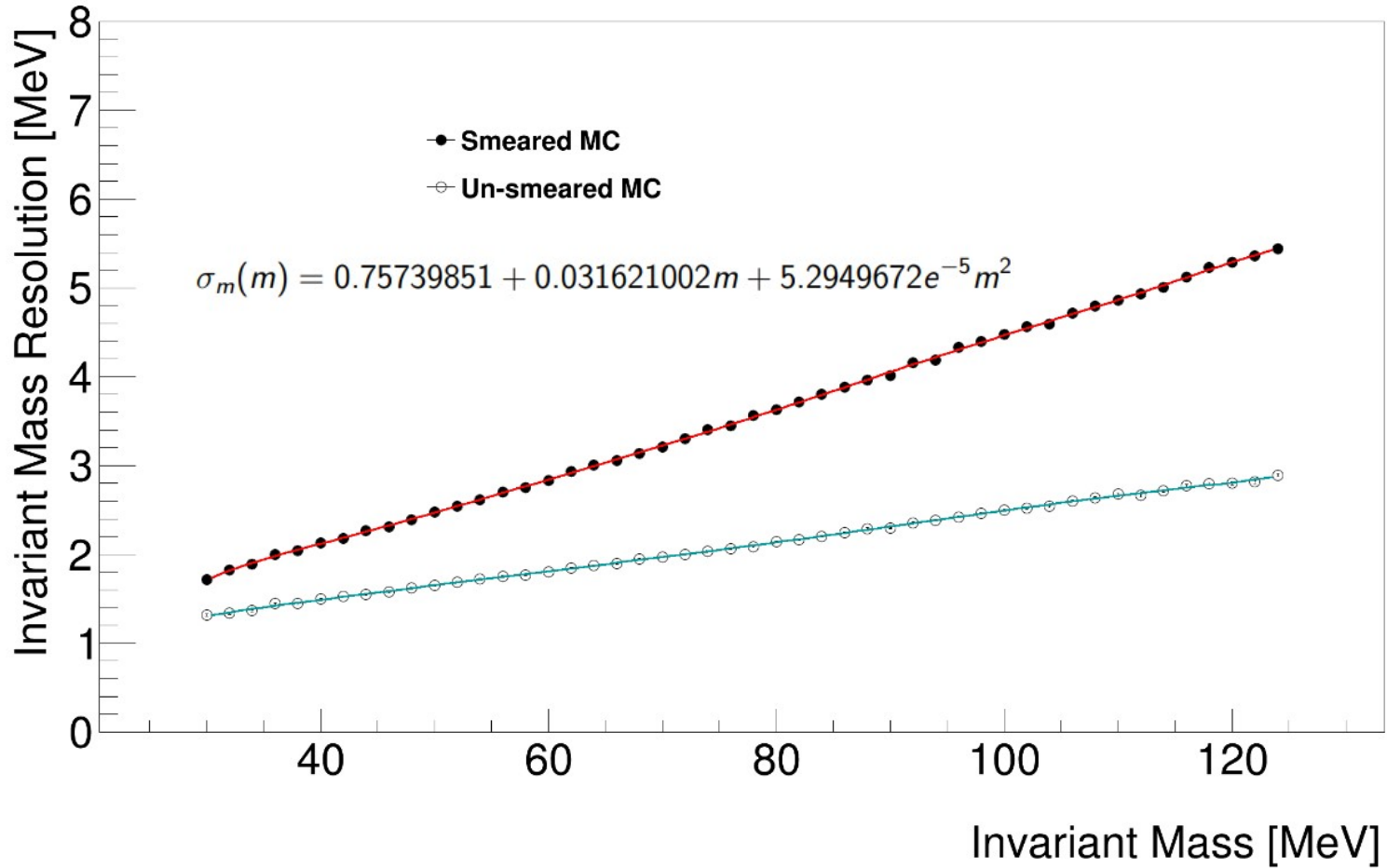
	μ [MeV]	σ [MeV]	σ_{err} [MeV]
Data	48.76	2.54	0.067
MC	48.52	1.87	0.016
MC _{smeared}	48.41	2.32	0.017

Constrained Vtx Seedtracker+GBL

	μ [MeV]	σ [MeV]	σ_{err} [MeV]
Data	48.93	2.06	0.012
MC unsmeared	48.43	1.	0.0033
MC smeared	48.35	1.93	0.0026

*MC Mollers skimmed from tritrig+beam MC, so difference in tails attributed to differences in MC beam and actual bkg in data

Smearred MC Mass Resolution



Selection

Preselection

Table 5: The Preselection cutflow efficiency after each cut is applied in order.

Cut Description	Requirement
Trigger	Pair1
Track Time	$ Track_t < 6$ ns
Cluster Time Difference	$\Delta_t(Cluster_{e^-}, Cluster_{e^+}) < 1.45$ ns
Track-Cluster Time Difference	$\Delta_t(Track, Cluster) < 4.0$ ns
Track Quality	$Track\chi^2/n.d.f. < 20.0$
Beam electron cut	$p_{e^-} < 1.75$ GeV
Minimum Hits on Track	$N_{2dhits} Track > 7.0$
Unconstrained Vertex Quality	$Vtx\chi^2 < 20.0$
Vertex Momentum	$p_{e^-+e^+} < 2.4$ GeV

Table 6: V_0 selection. The time offset for data is 56 ns and the time offset for MC is 43 ns.

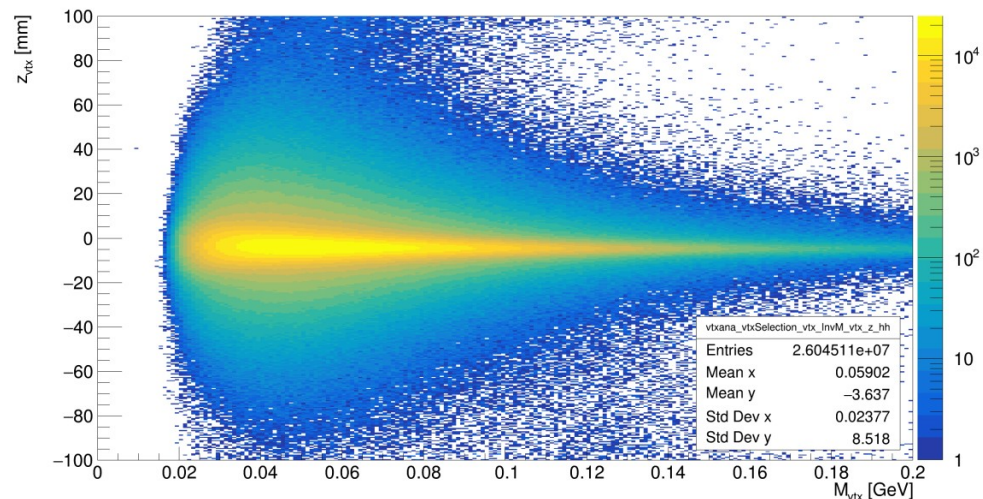
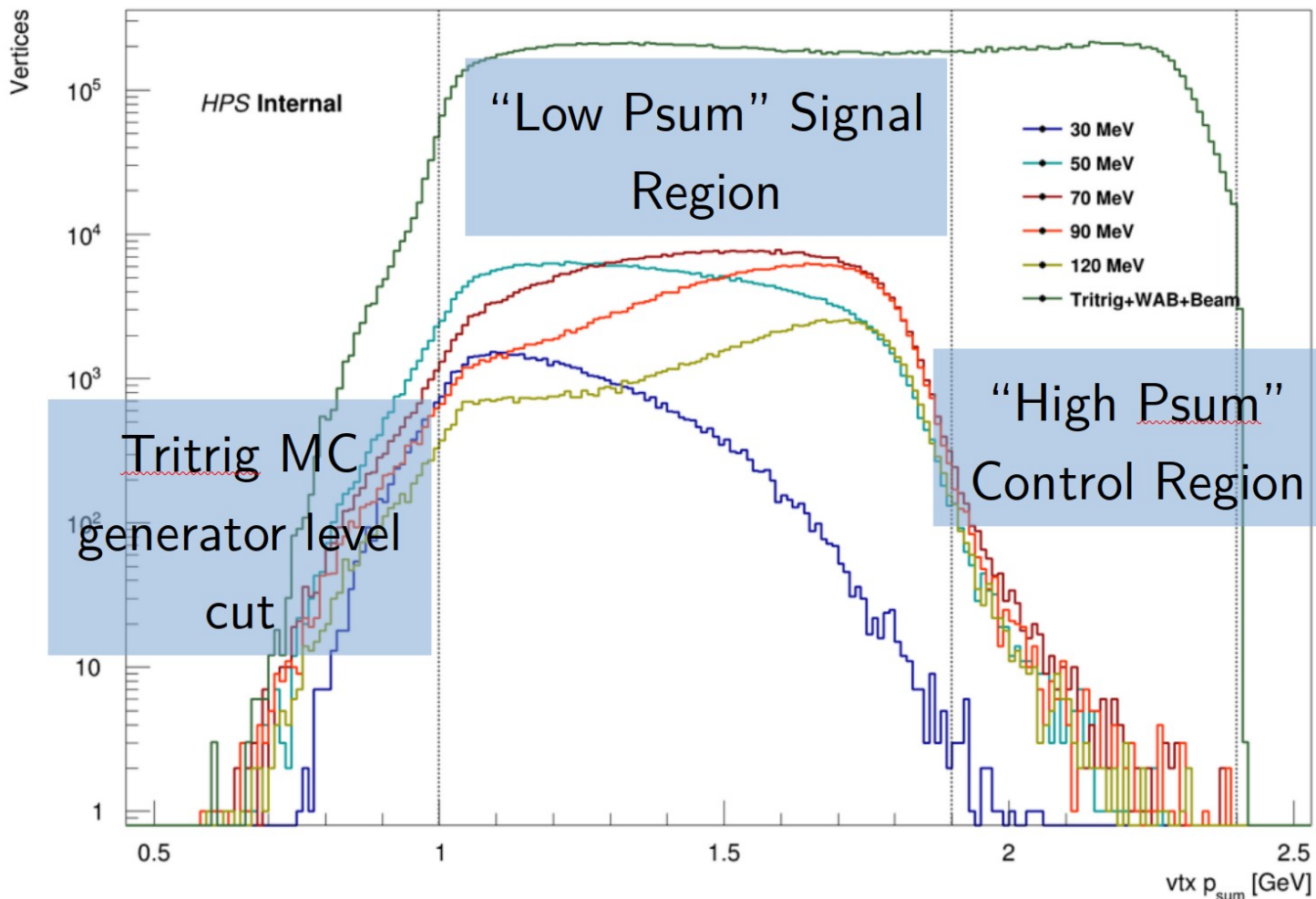


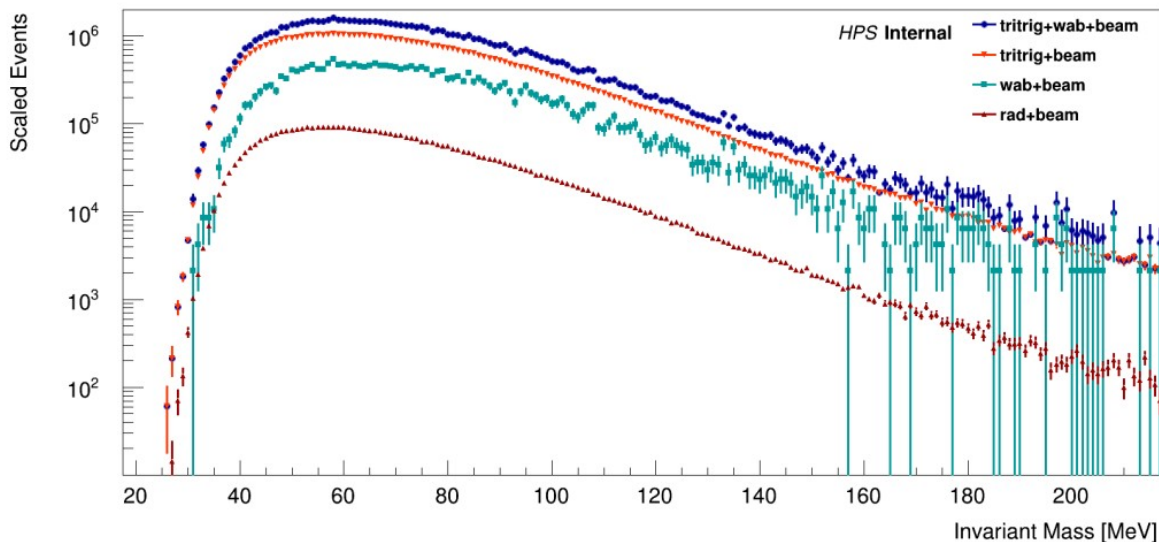
Figure 43: Reconstructed vertex z position versus Invariant Mass for the $\sim 10\%$ Data sample.

Signal and Control Regions



Expected Signal Calculation

Radiative Fraction



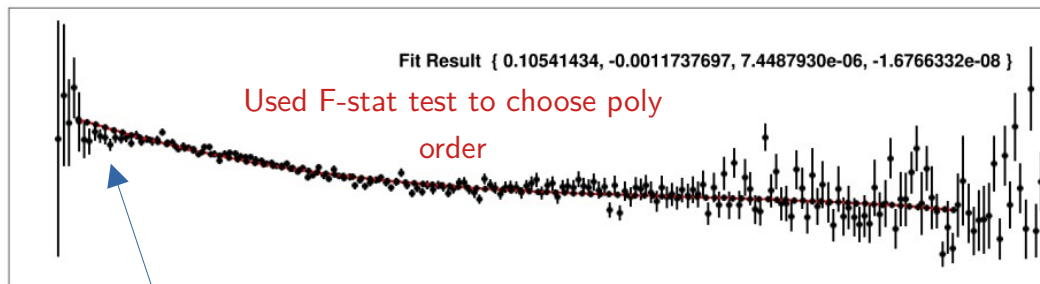
$$f_{rad}(m_{A'}) = \frac{dN_{\gamma^* CR}}{dm_{A'}} \bigg/ \frac{dN_{CR}}{dm_{reco}}$$

γ^* truth-matched
to eliminate false
reconstructions

Not truth-matched

Systematic Uncertainty

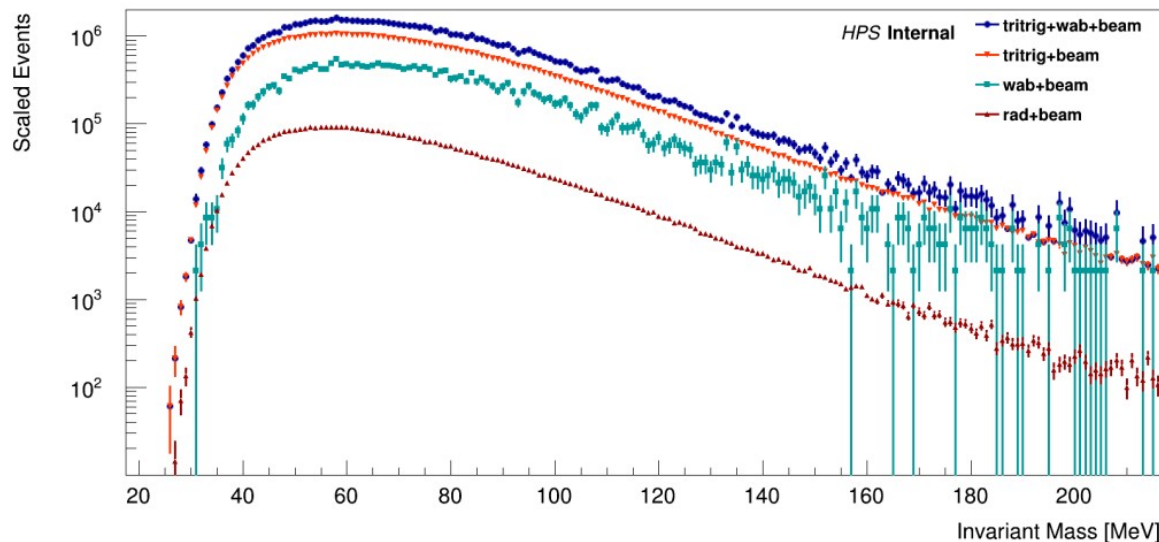
- Driven by MC cross-section uncertainties
- Estimated as $\sim 7\%$ in 2016 A' analysis
- Same here



*Fit is kind of poor here



Radiative Fraction



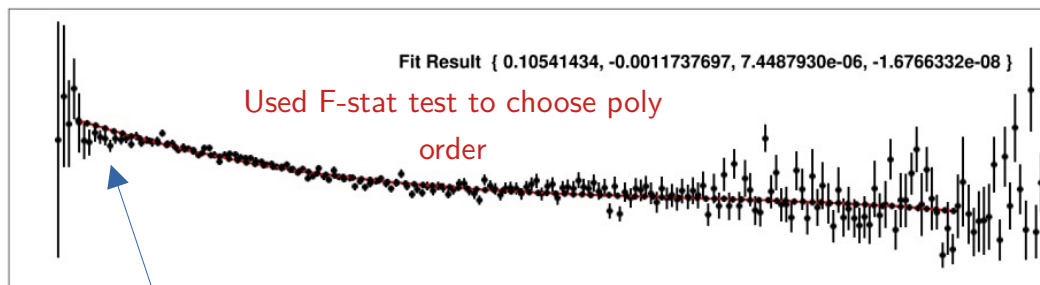
$$f_{rad}(m_{A'}) = \frac{dN_{\gamma^* CR}}{dm_{A'}} / \frac{dN_{CR}}{dm_{reco}}$$

γ^* truth-matched
to eliminate false
reconstructions

Not truth-matched

Is there a “fake”
contribution to the
reconstructed background
rate in data?

- D uncertainties
- Estimated as $\sim 7\%$ in 2016 A' analysis
- Same here

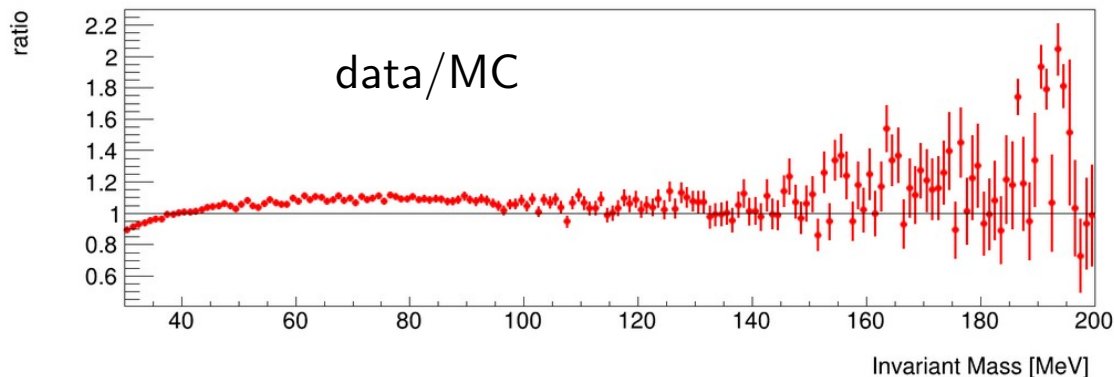
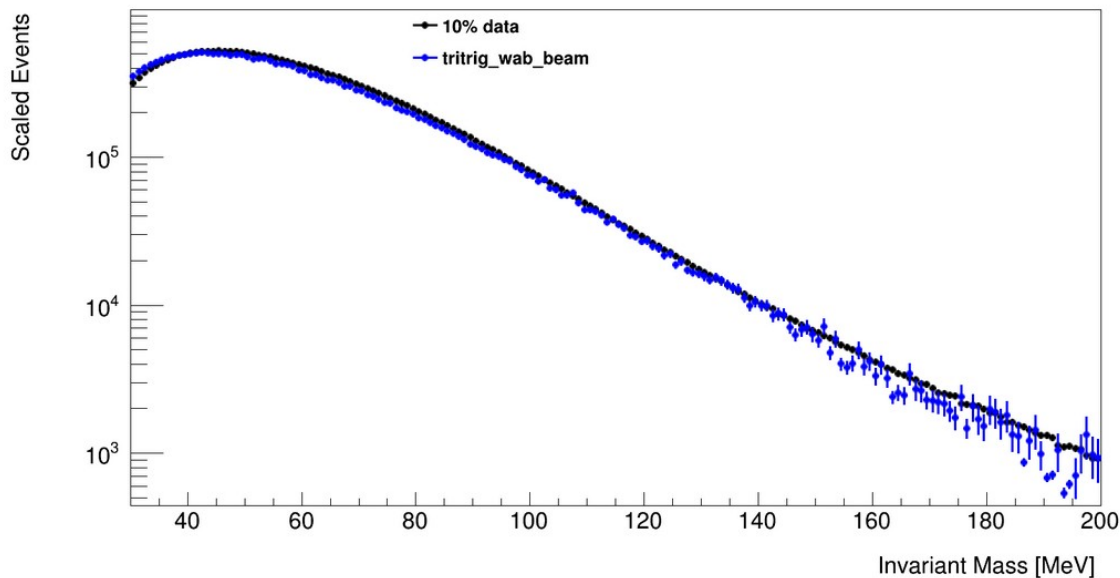


*Fit is kind of poor here

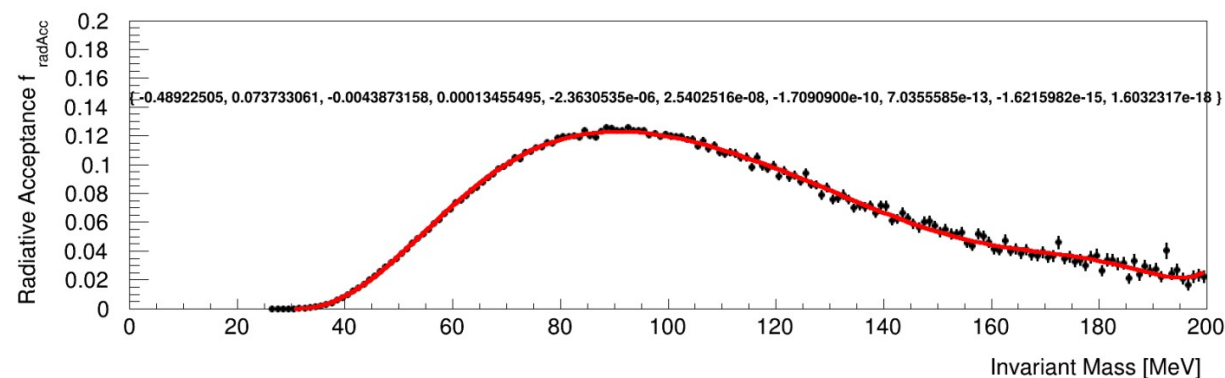
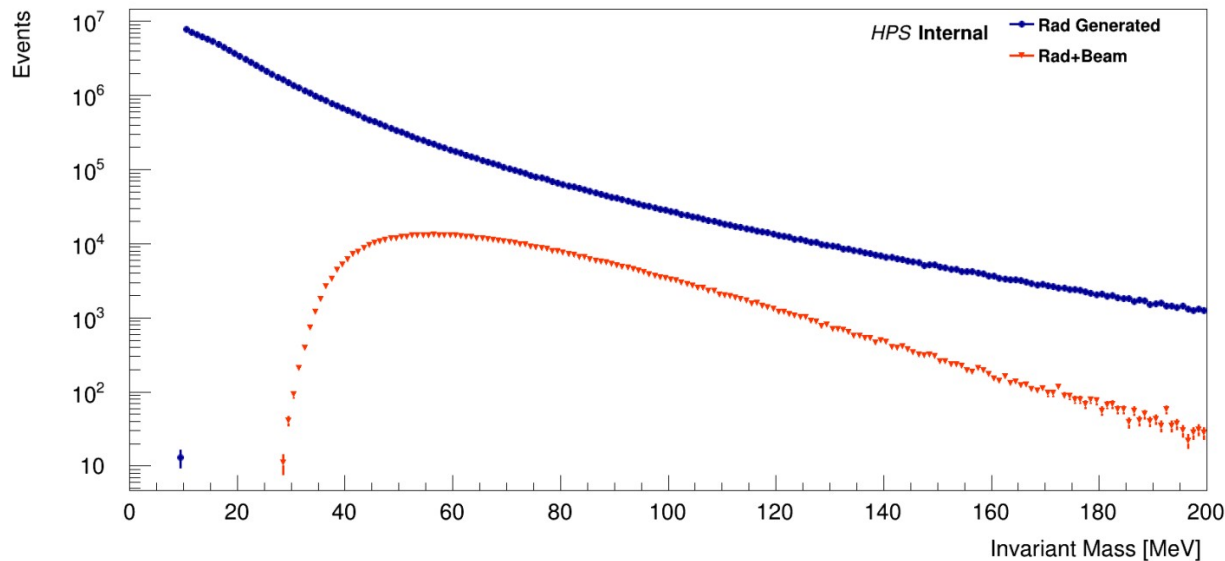


Radiative Fraction – Fakes in Data?

- Background primarily Bethe-Heitler+Radiative tridents and cWABs
- No processes expected to contribute to meaningful fake trident rate
- Compare invariant mass in 10% data and tritrig+wab+beam (scaled to ~10%)
- No evidence of significant fake trident process in data
- Scale and shape both look reasonable



Radiative Acceptance



Truth-matched

$$A_{rad}(m_{A'}) = \frac{dN_{\gamma^* CR}}{dm_{A'}} / \frac{dN_{\gamma^*}}{dm_{A'}}$$

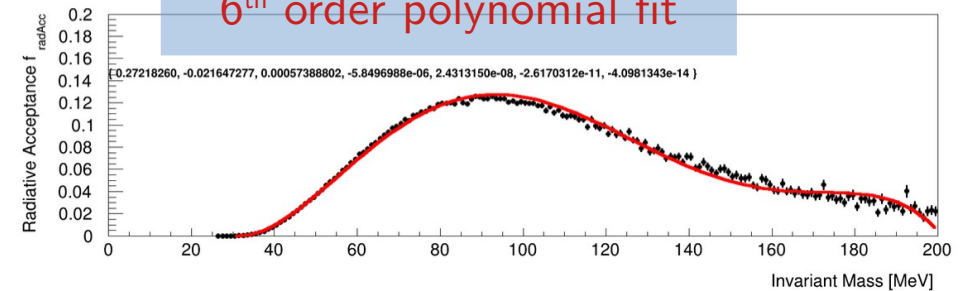
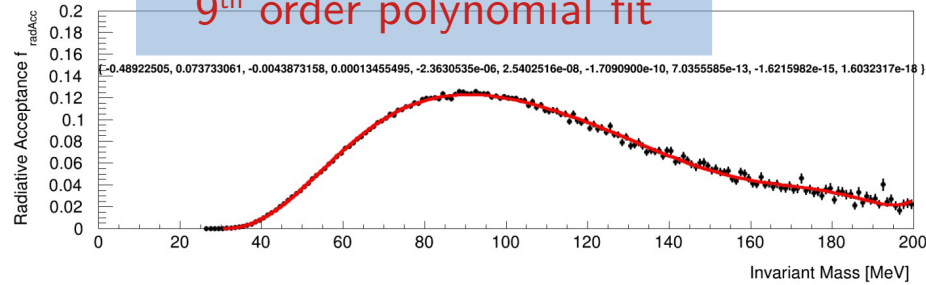
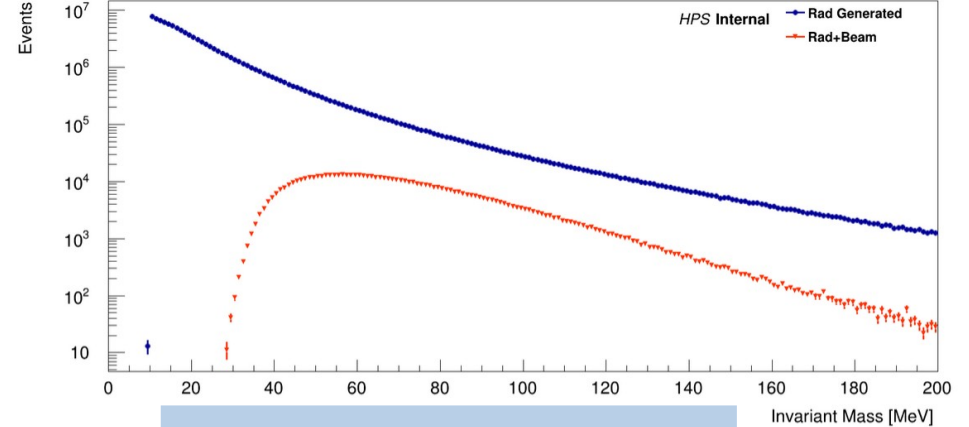
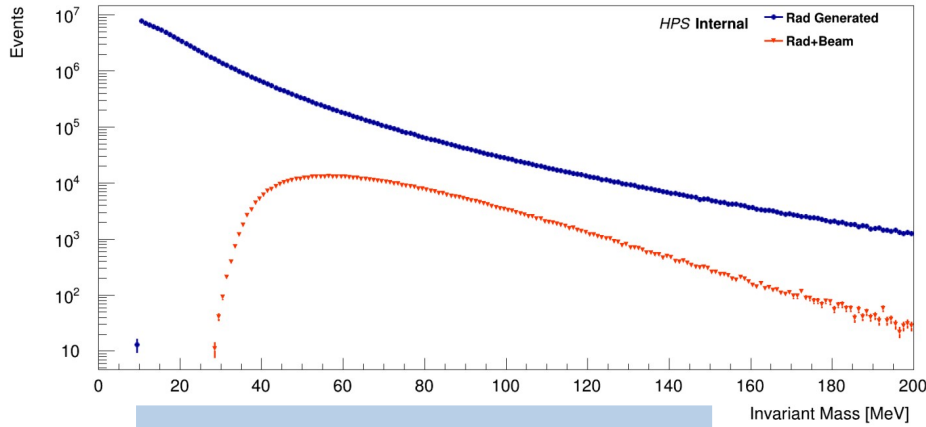
Generated

Systematic Uncertainty

- ~11% from Preselection cuts
- Need to study how acceptance changes with mis-alignments, and target position uncertainty *Sarah is producing these samples now!



Radiative Acceptance – Fit Polynomial



F-stat Test: [0.0, 445.8873264001735, 49.31428264707902, 222.16853689090675, 1705.0368133223403, 2287.5442058522844, 2.713528604174555, 239.05267186996403, 237.5954446109807, 121.49079724872668, 64.93822659490942]

6th

9th

*can stop fit at 140MeV

*also, might start at 40MeV instead



Expected Signal Calculation

$$N_{A'}(m_{A'}, \epsilon) = \frac{3\pi m_{A'} \epsilon^2}{2N_{\text{eff}=1} \alpha} \frac{f_{\text{rad}}(m_{A'})}{A_{\text{rad}}(m_{A'})} \frac{dN_{\text{CR}}}{dm_{\text{reco}}}$$

Total number of A's

*systematic studies will involve mis-alignments and target uncertainty

$$F(z) = \left(\frac{dN_{V_D}^{\text{selected}}}{dz_{\text{vtxtrue}}} \Big|_{z_{\text{vtx}}=z} \right) / \left(\frac{dN_{V_D}^{\text{generated}}}{dz_{\text{vtxtrue}}} \Big|_{z_{\text{vtx}}=z} \right)$$

Tight SELECTION acceptance \times efficiency for signal generated with constant lifetime out to 20cm in z

$$f_{V_D}(\epsilon, z) = \frac{\exp\left(\frac{z_{\text{target}} - z}{\gamma c \tau_{V_D}}\right)}{\gamma c \tau_{V_D}} F(z)$$

*F(z) uses truth z, so don't need to say z_{target}

Lifetime-weighted dark vector acceptance \times efficiency

$$N_{\text{sig}}(m_{A'}, \epsilon) = N_{A'} \int_{z_{\text{target}}}^{\infty} (BR(\rho_D) f_{\rho_D}(\epsilon, z) + BR(\phi_D) f_{\phi_D}(\epsilon, z)) dz$$

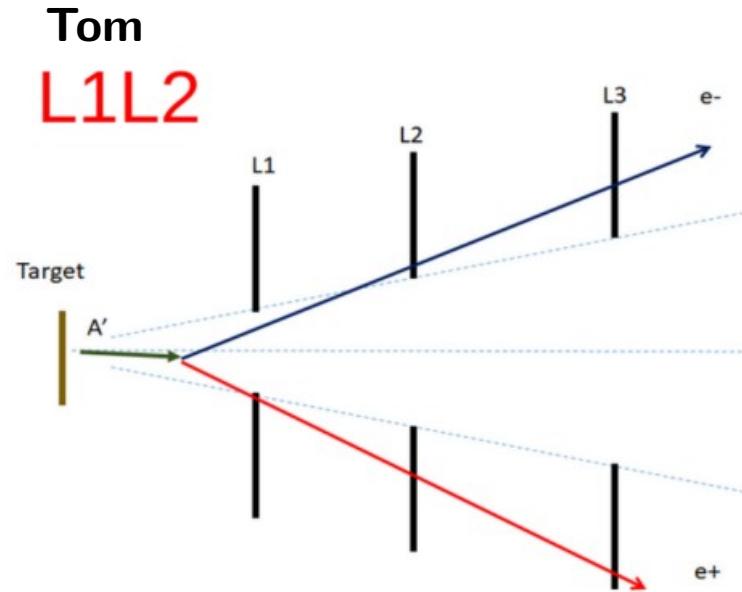
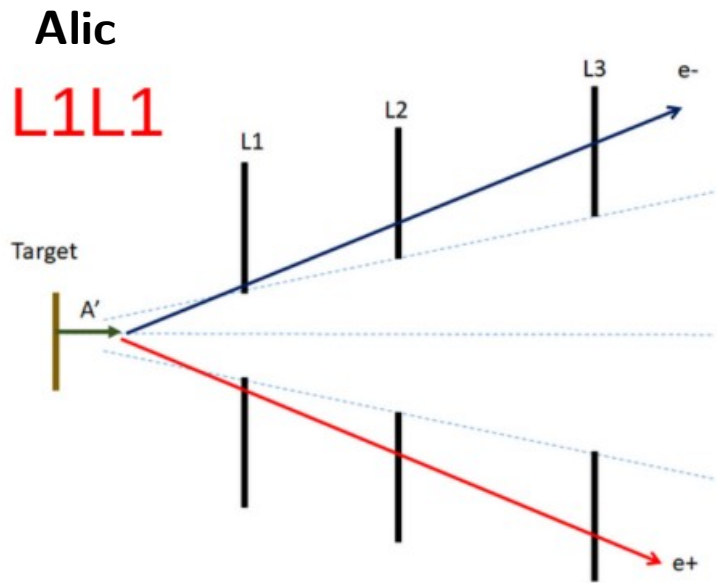
Full expected signal calculation



Tight Selection Variables

1. Target Projected Vertex Significance

L1L1 Hit Requirement

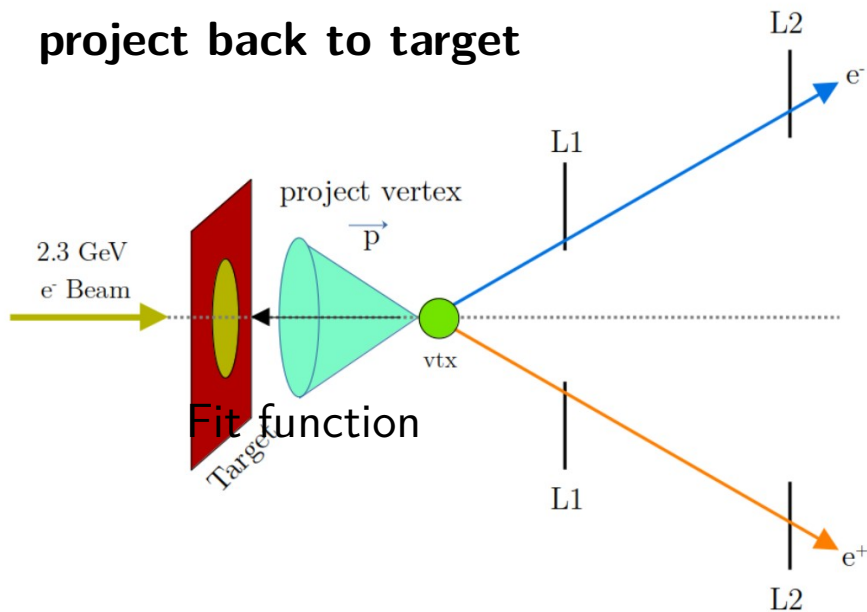


- Require axial+stereo hits in L1 and L2
- Gives best vertex resolution
- Restricted to shorter lifetimes than L1L2+L2L2

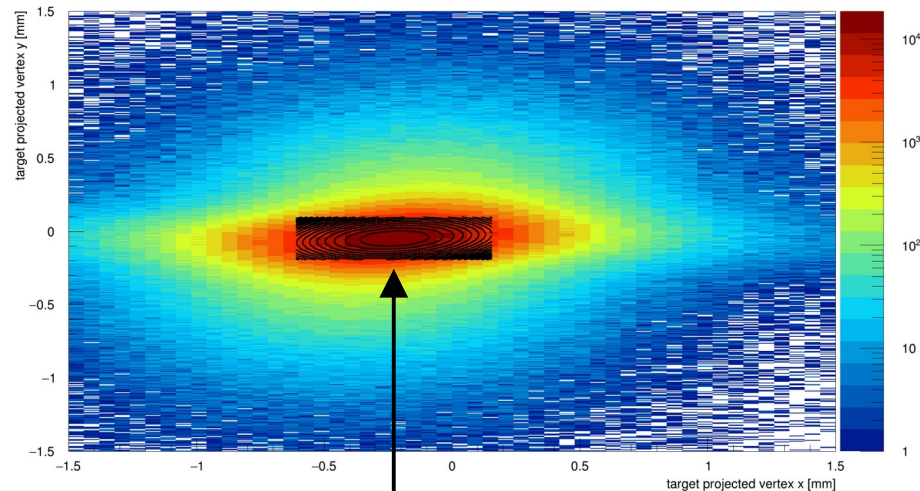
Target Projected Vertex Significance

*Use 1% of files ending in 0 from each run to fit run-dependent beamspot

Displaced vertex should project back to target



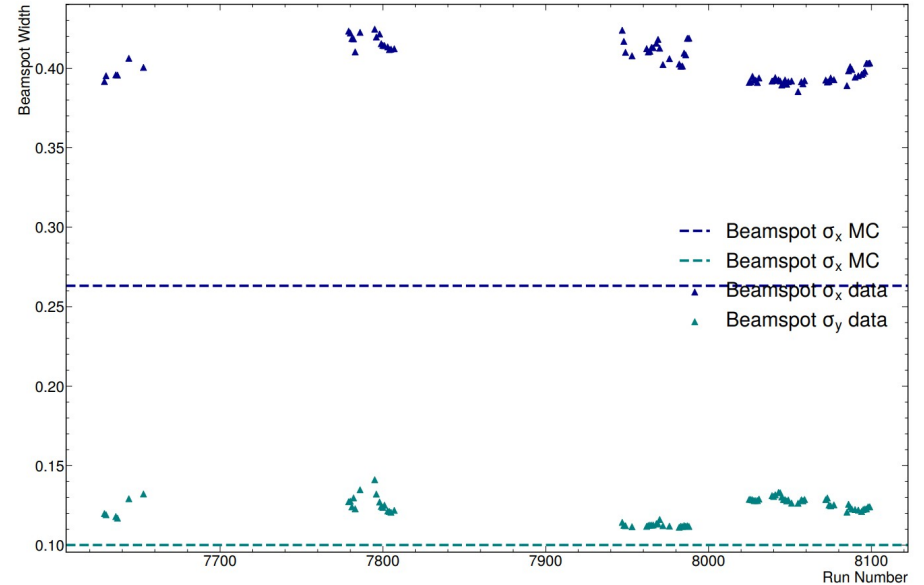
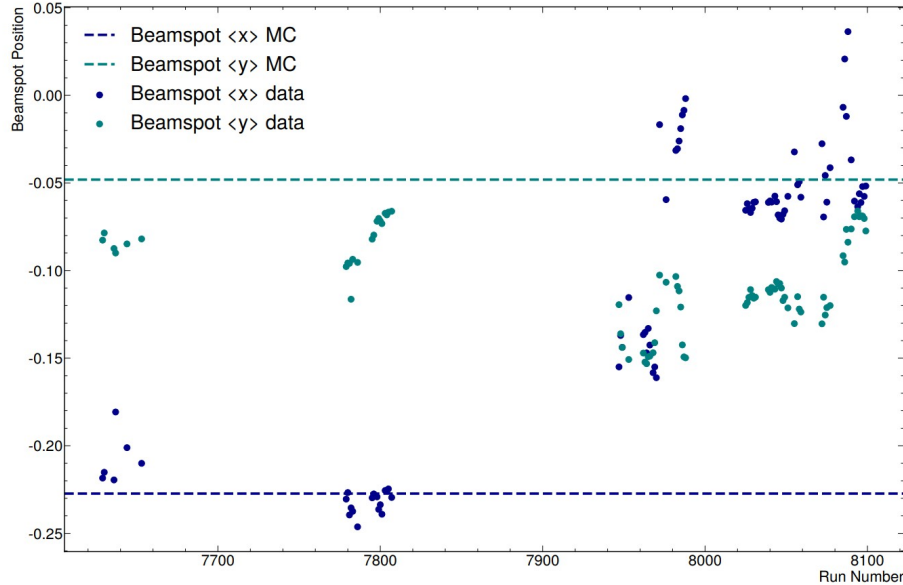
Preselection Unconstrained V0 Vertices
Projected to target z



$$f(x, y) = \exp\left(-\frac{(x_{\text{rot}} - \mu_{x_{\text{rot}}})^2}{2\sigma_{x_{\text{rot}}}^2} - \frac{(y_{\text{rot}} - \mu_{y_{\text{rot}}})^2}{2\sigma_{y_{\text{rot}}}^2}\right)$$

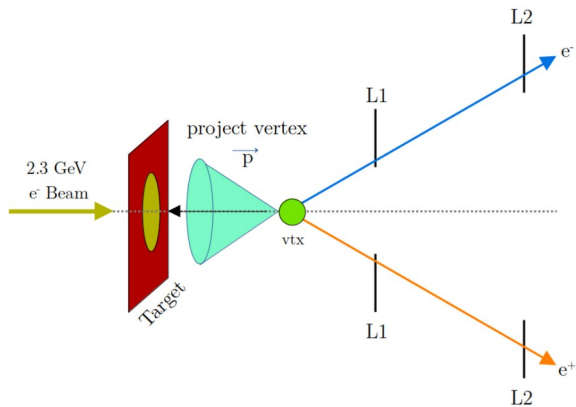
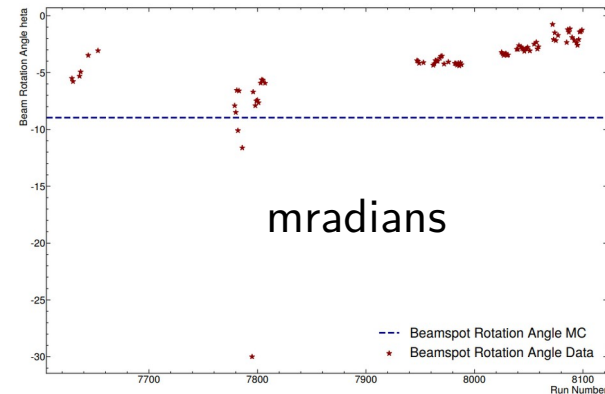
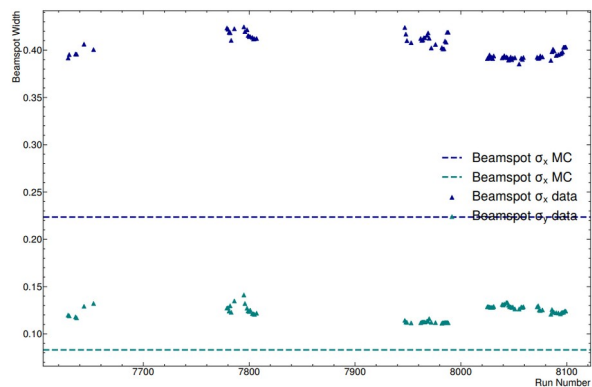
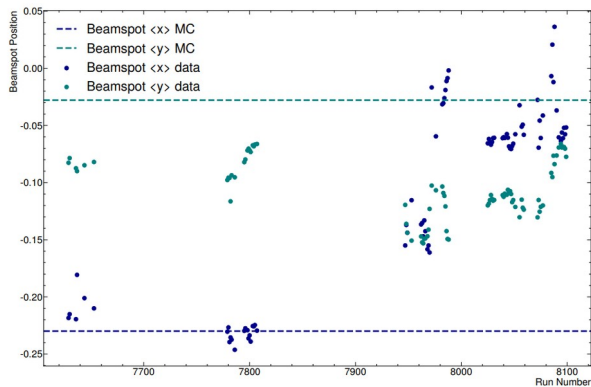


Run Dependent Beamspot – Unrotated Coordinates

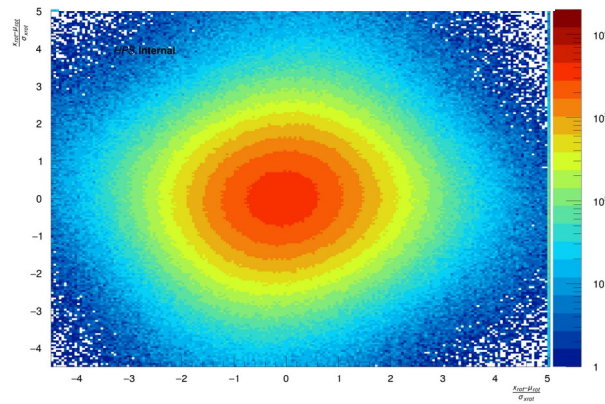


- *Why does the beamspot position change so much in data?
 - Machine control loves to mess with the beam
- Scale is mm, not crazy change
- Projection significance doesn't care, defined relative to beamspot parameters

Run Dependent Beamspot – Rotated Coordinates



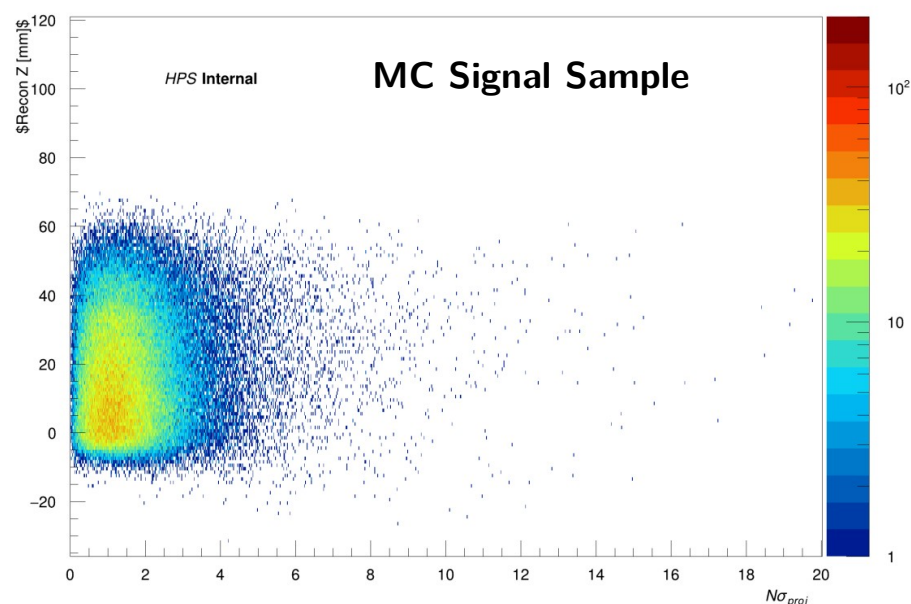
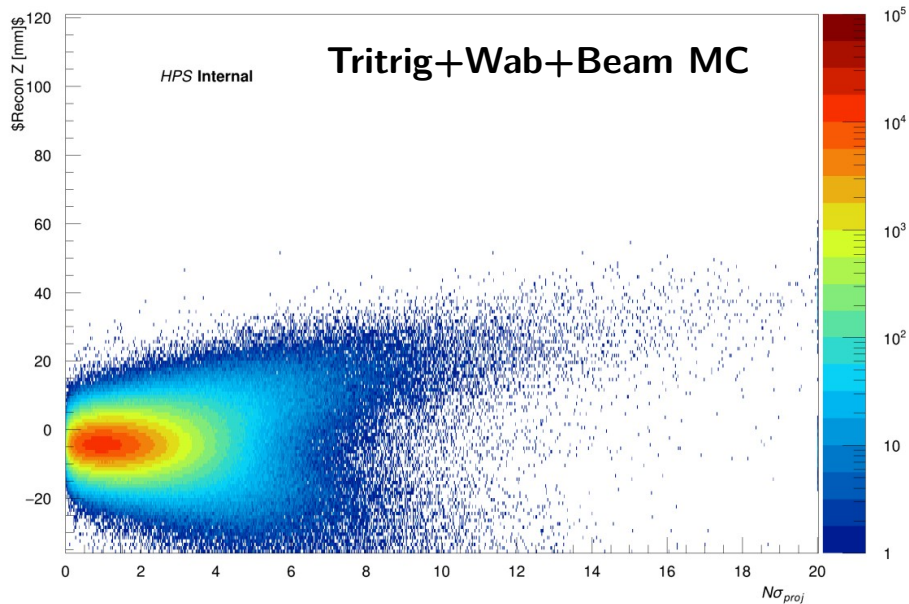
$$(N_{\sigma_{x_{rot}}}, N_{\sigma_{y_{rot}}}) = \left(\frac{x_{rot} - \mu_{x_{rot}}}{\sigma_{x_{rot}}}, \frac{y_{rot} - \mu_{y_{rot}}}{\sigma_{y_{rot}}} \right)$$



- Project vertex to target
- Rotate coordinates using fitted beamspot angle
- Use fitted beamspot to get significance



Target Projected Vertex Significance

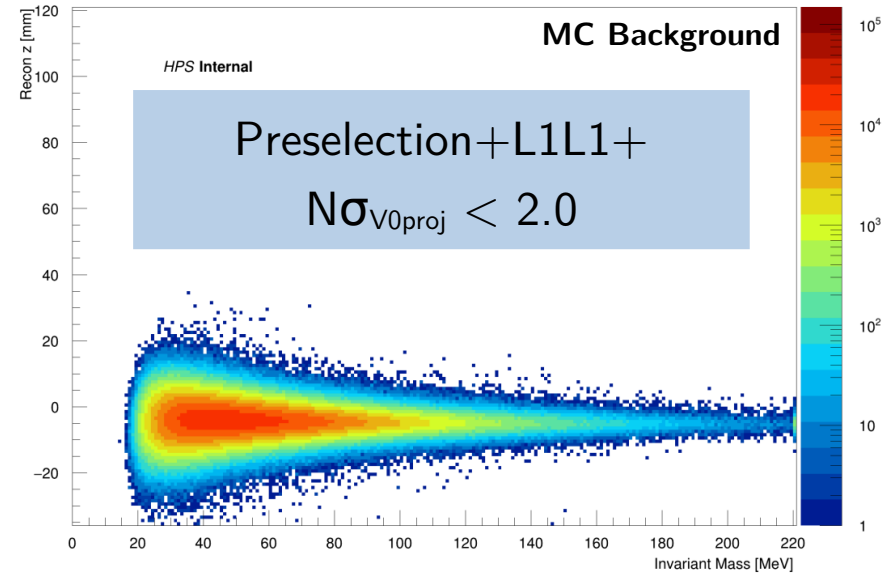
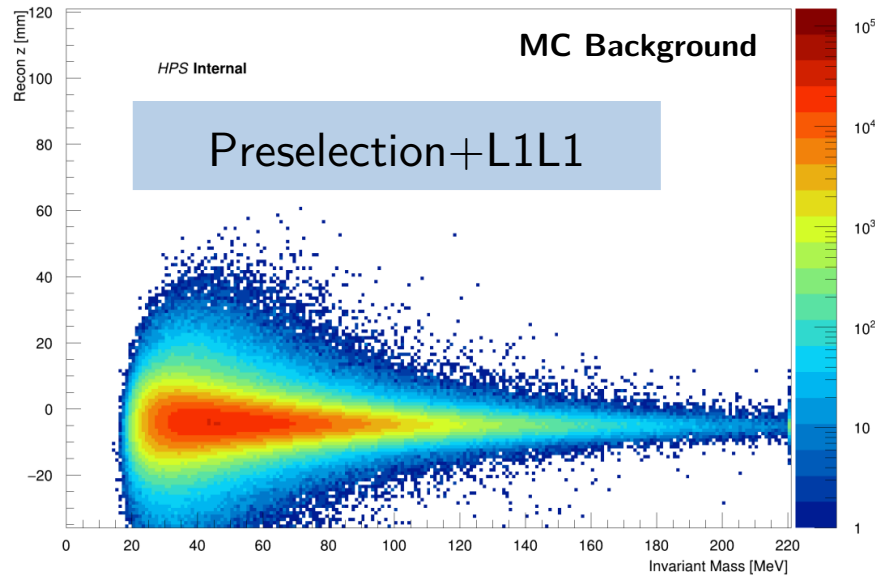


Combine x and y significance into single cut variable
“Target Projected Vertex Significance”

$$N\sigma_{V0_{proj}} = \sqrt{N_{\sigma_{Xrot}}^2 + N_{\sigma_{Yrot}}^2}$$



Target Projected Vertex Significance

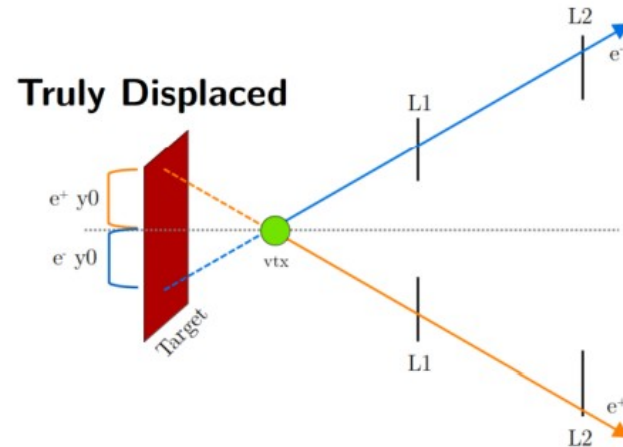
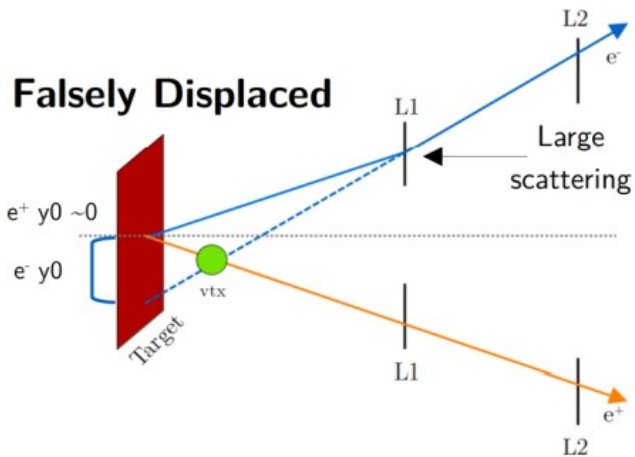
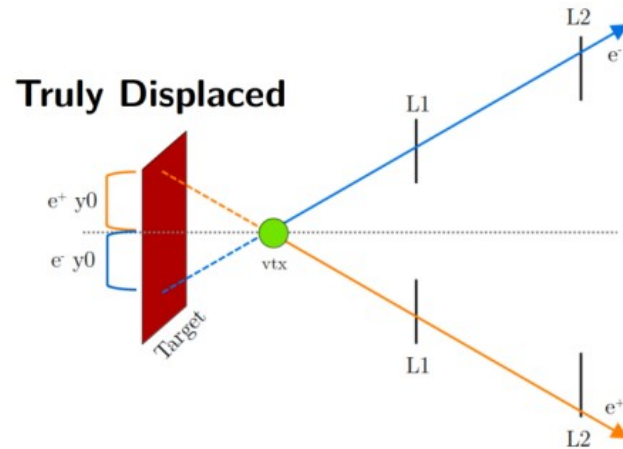
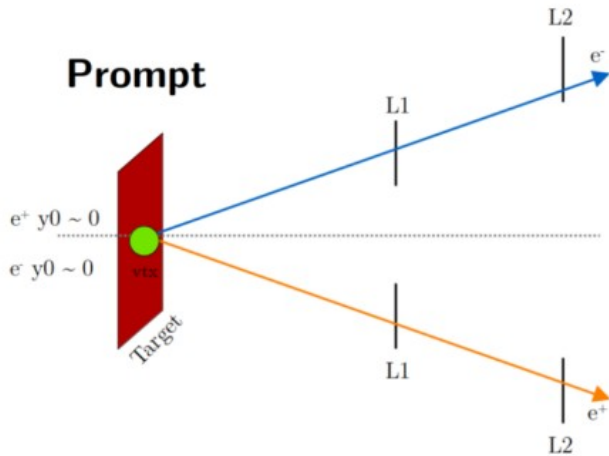


Tight Selection Variables

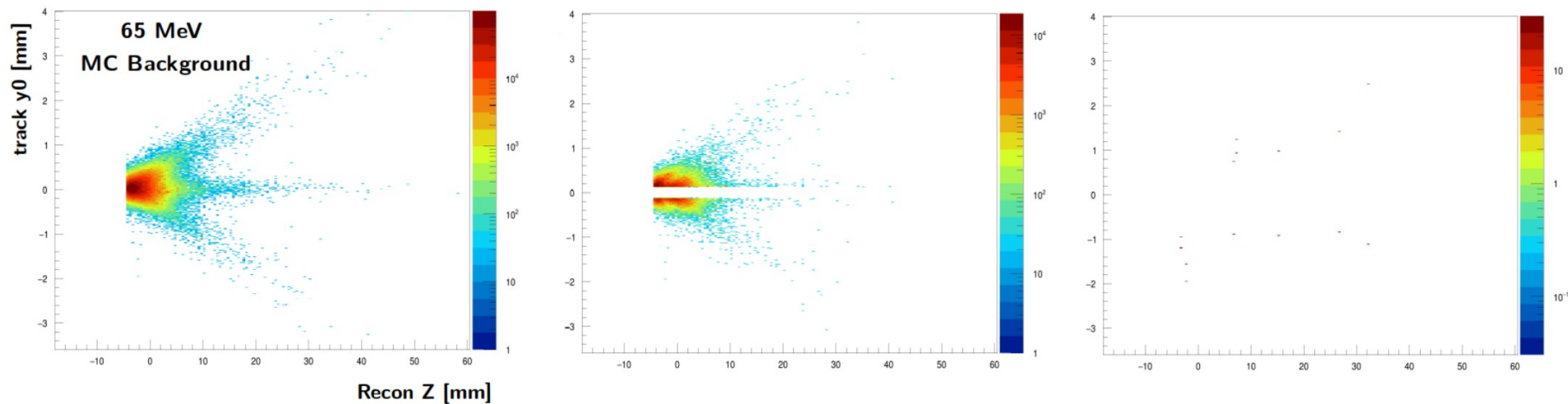
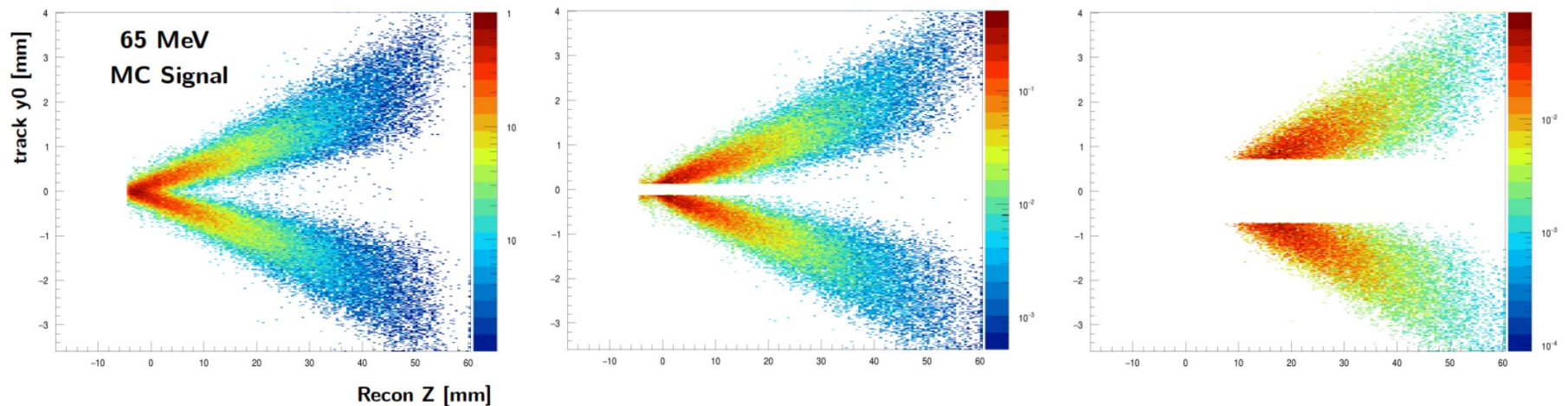
2. Vertical Impact Parameter

Vertical Impact Parameter Cut

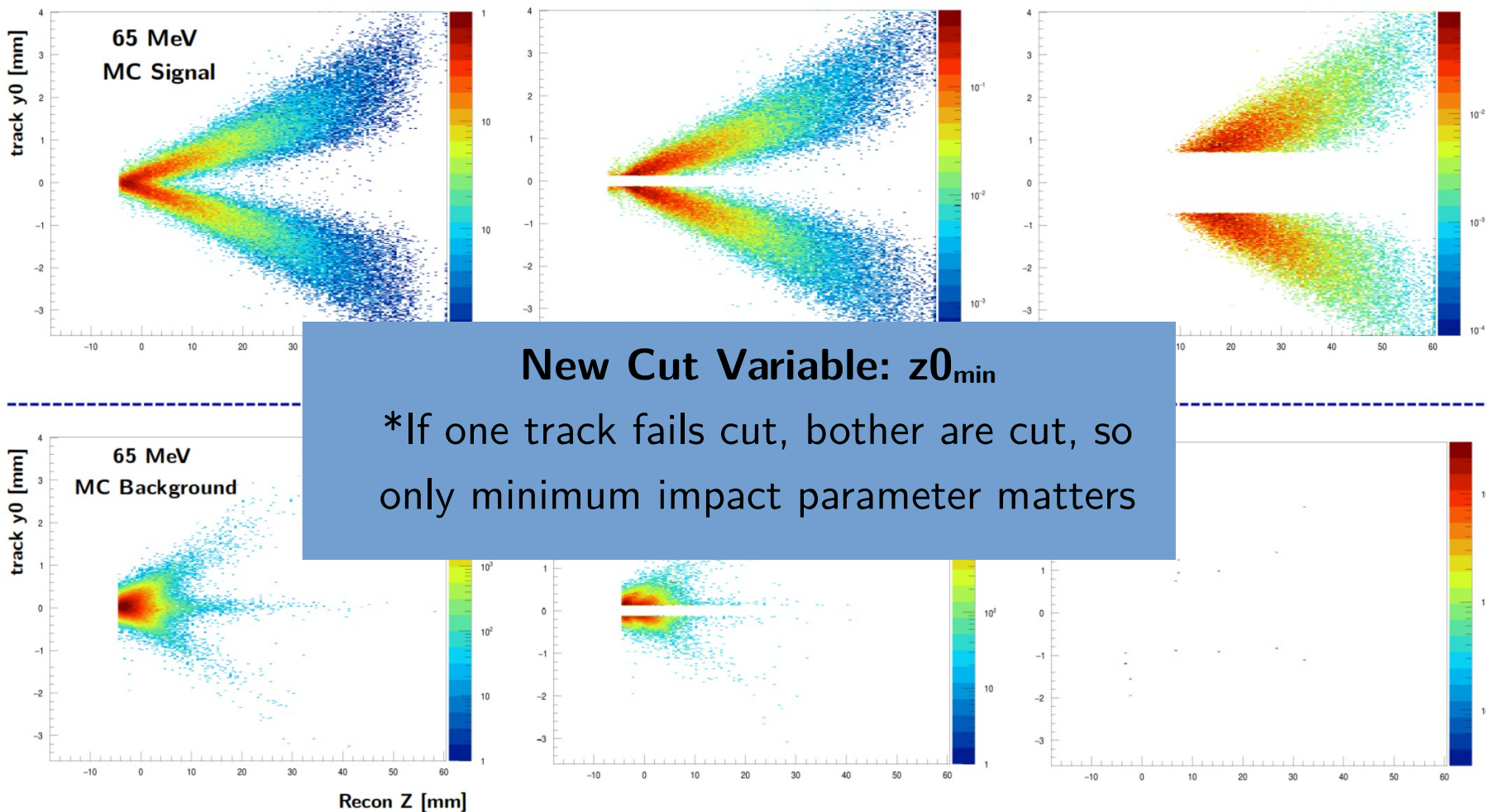
$*y_0 = z_0$



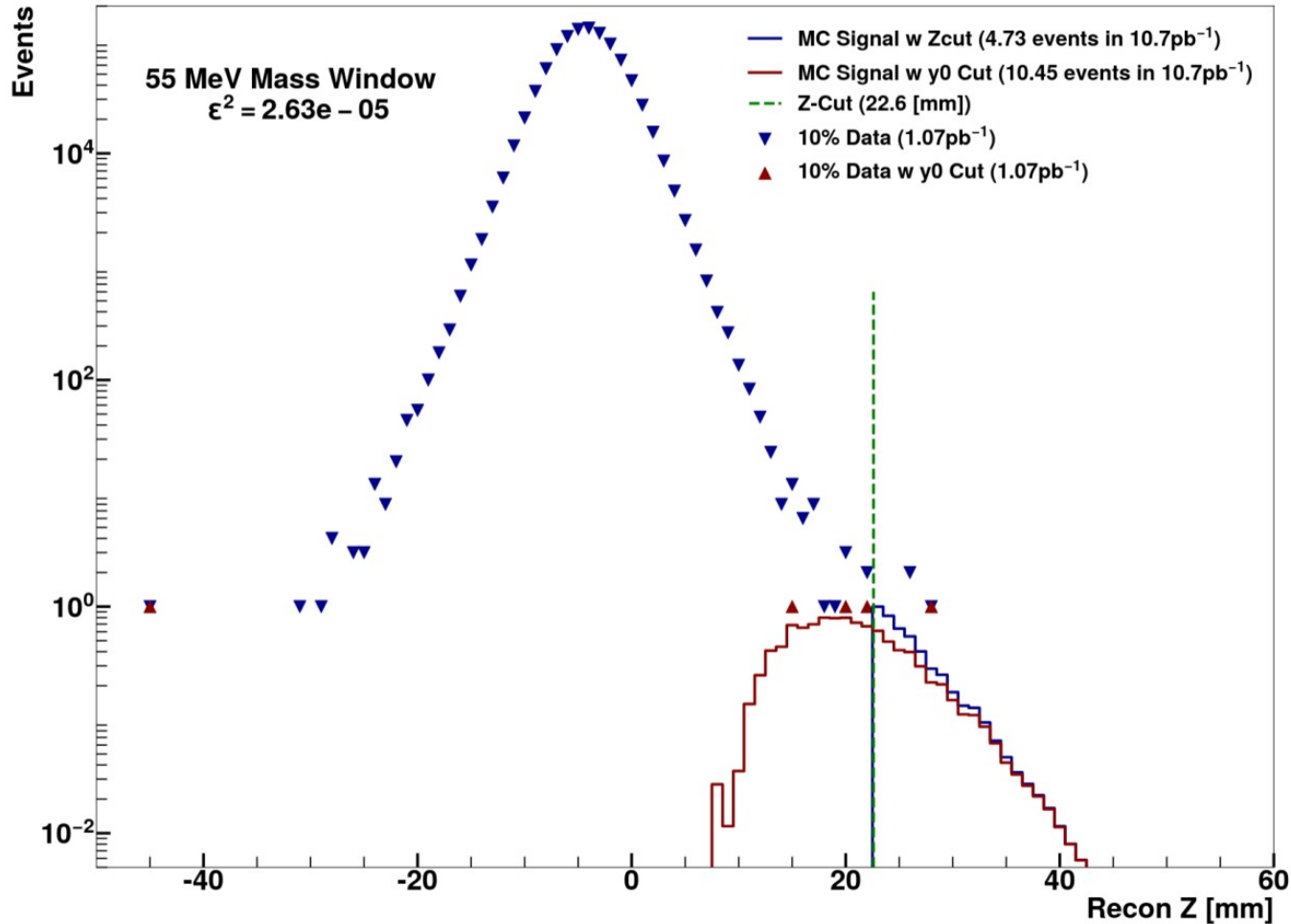
Vertical Impact Parameter Cut



Vertical Impact Parameter Cut



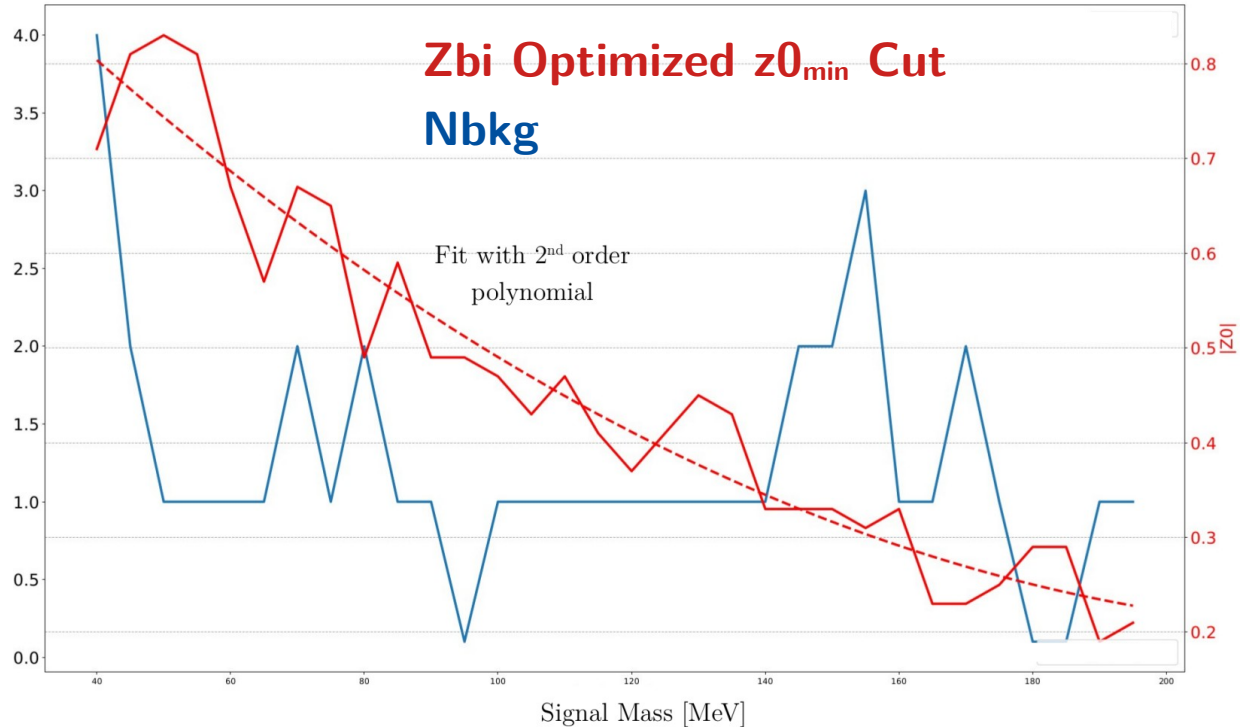
Vertical Impact Parameter Cut vs Zcut Analysis



*calculated using full expected signal calc.

Vertical Impact Parameter Cut Optimization

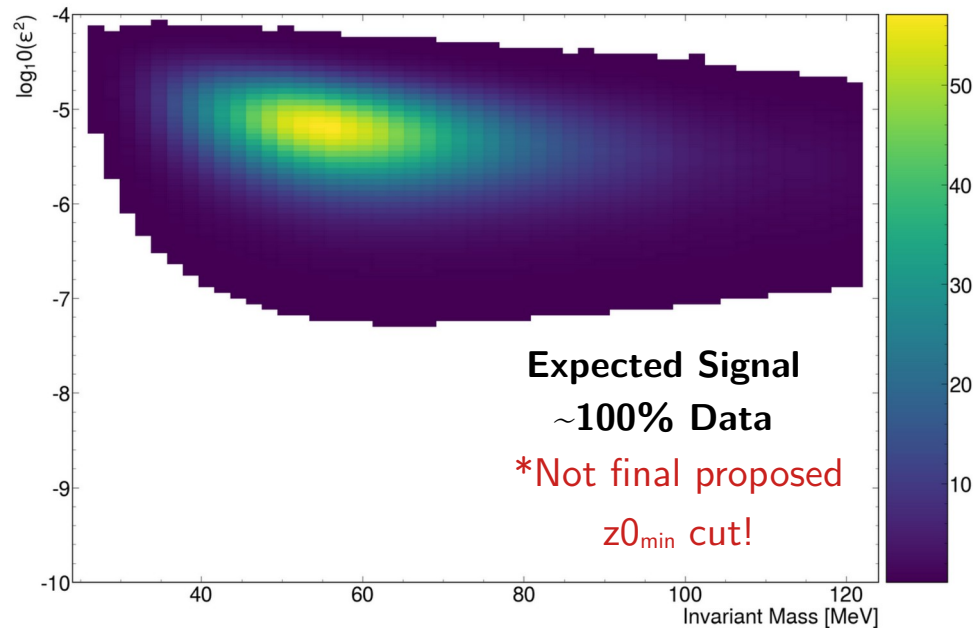
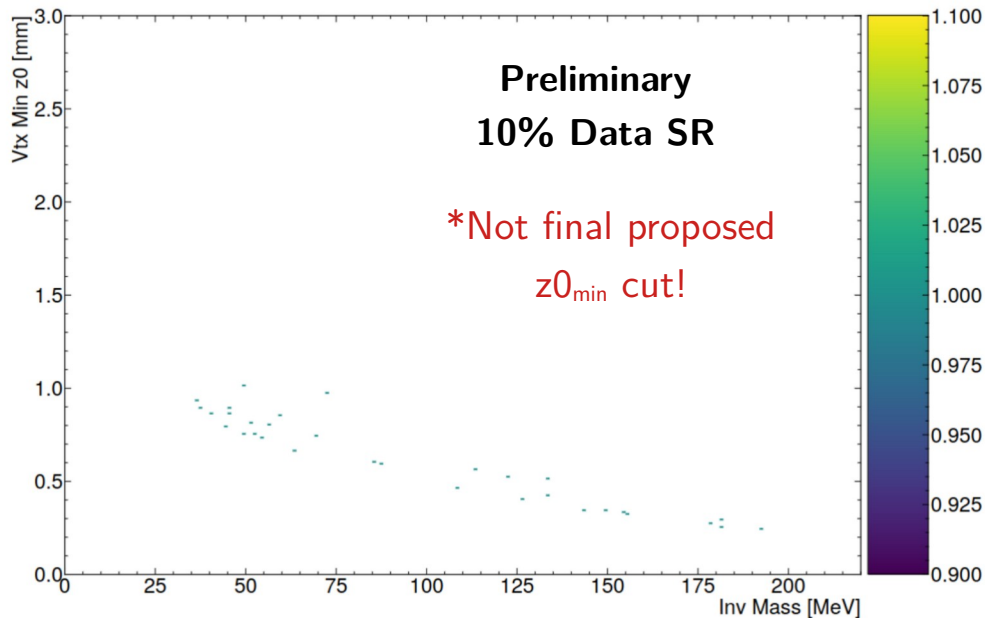
- $z0_{\min}$ shape optimized using **10% Data SR ONLY**
- Cut is function of invariant mass, fit with 2nd order polynomial
- ***This is not the final proposed cut...tighten later (+0.1mm) to protect from large fluctuations in bkg in 100% data SR**



$$z0_{\min}(m) > 1.0762 - 7.44534 \times 10^{-3}m + 1.58746 \times 10^{-5}m^2$$



Preliminary Tight Selection

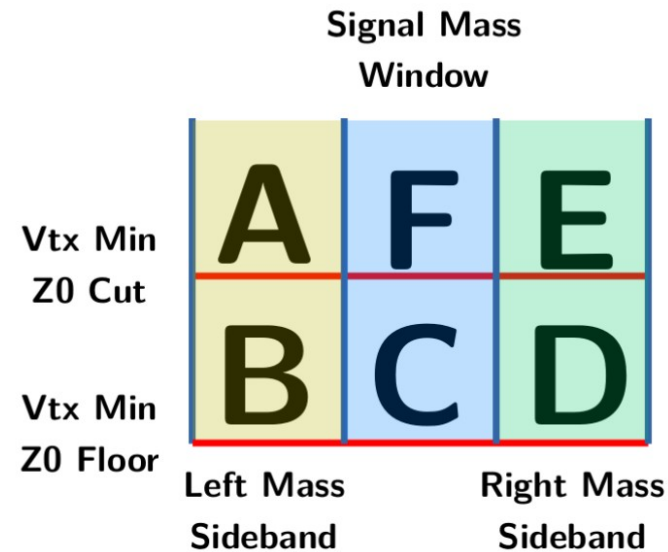
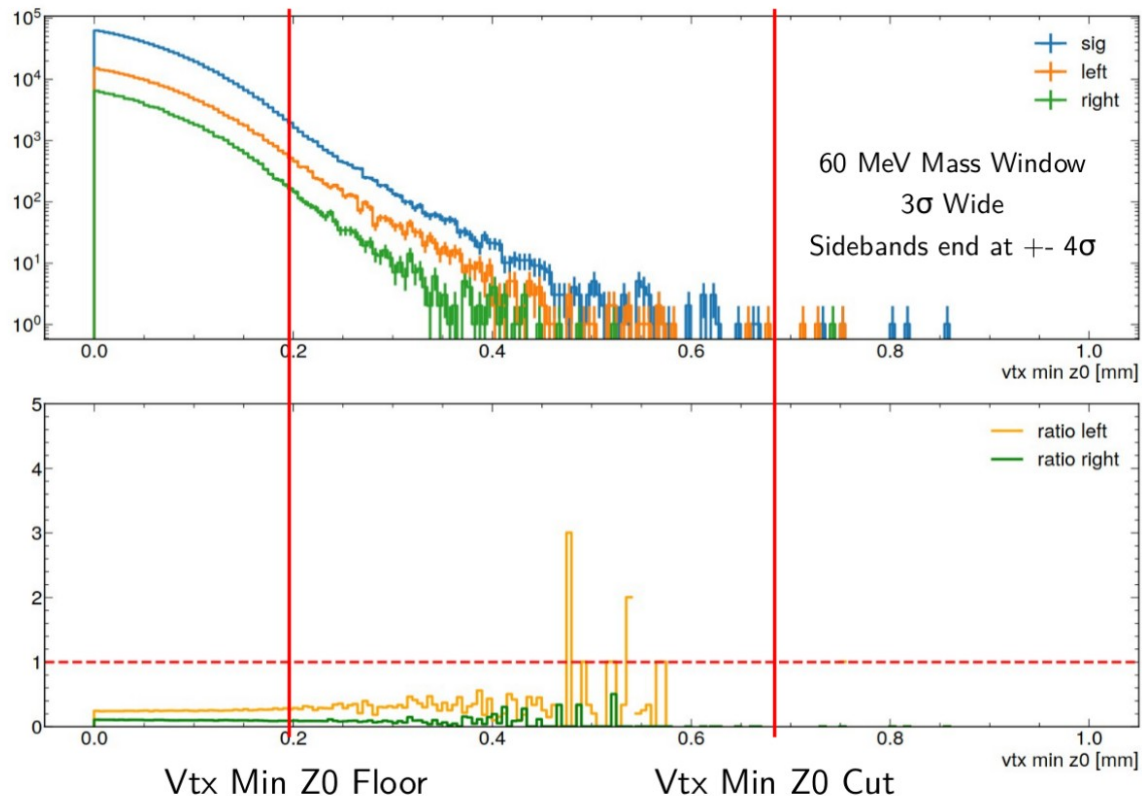


Cut	Condition
Layer 1 Requirement	e^- and e^+ have L1 axial+stereo hit
Layer 2 Requirement	e^- and e^+ have L2 axial+stereo hit
Target Projected Vertex Significance Cut (V_{0proj})	$V_{0proj} < 2.0$
Target Z Cut	$z_{vtx} > -4.3$ [mm]
Impact Parameter Cut	$z^{min}(m) > 1.0762 - 7.44534 \times 10^{-3}m + 1.58746 \times 10^{-5}m^2$



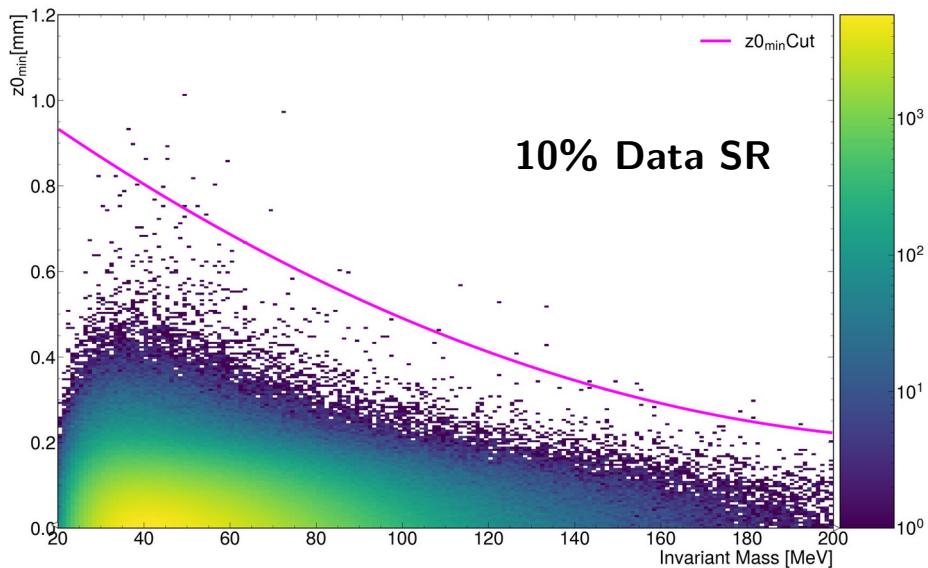
Signal Search: Background Estimation

Background Estimation Method

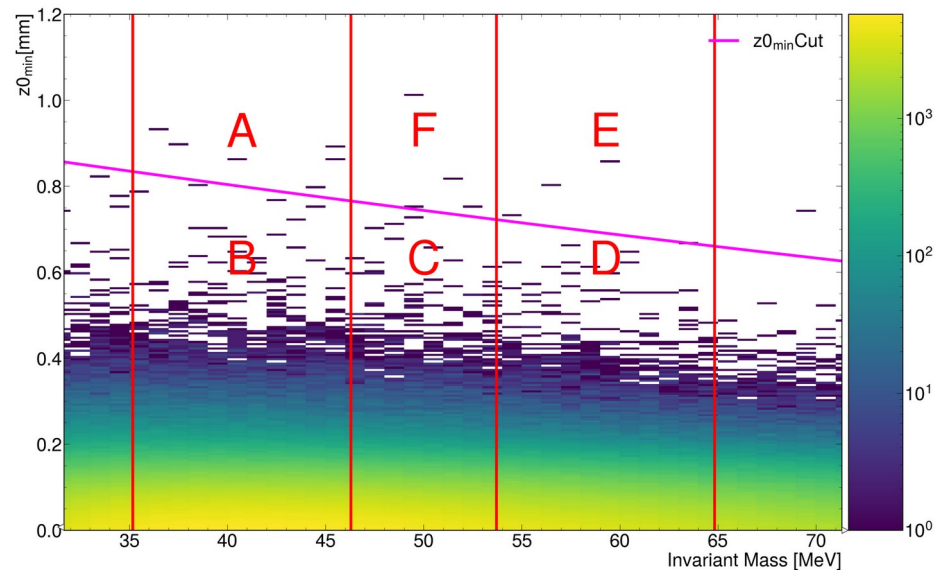


$$(A+E)/(B+D)*C = F$$

Background Estimation Method



A bit of a correlation between $z0_{\min}$ and Invariant Mass overall



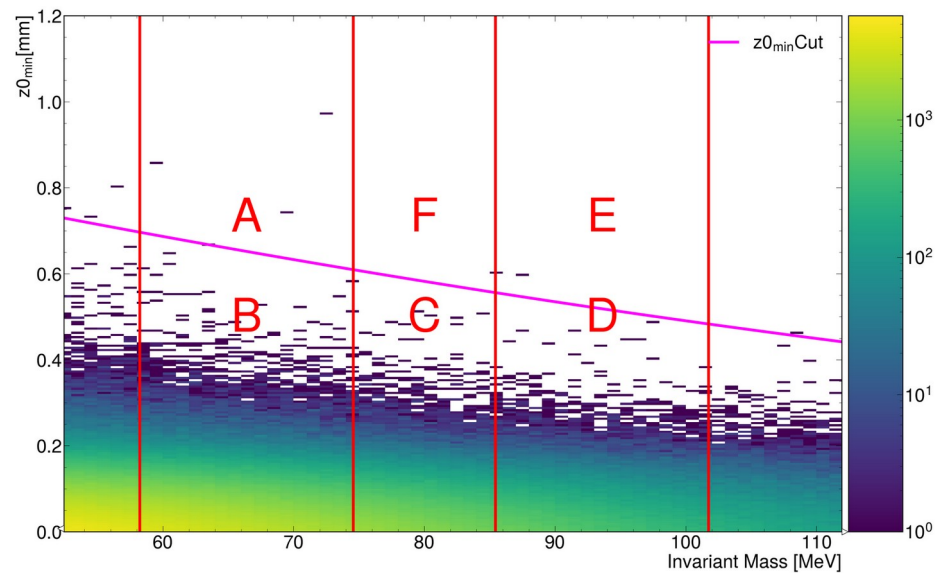
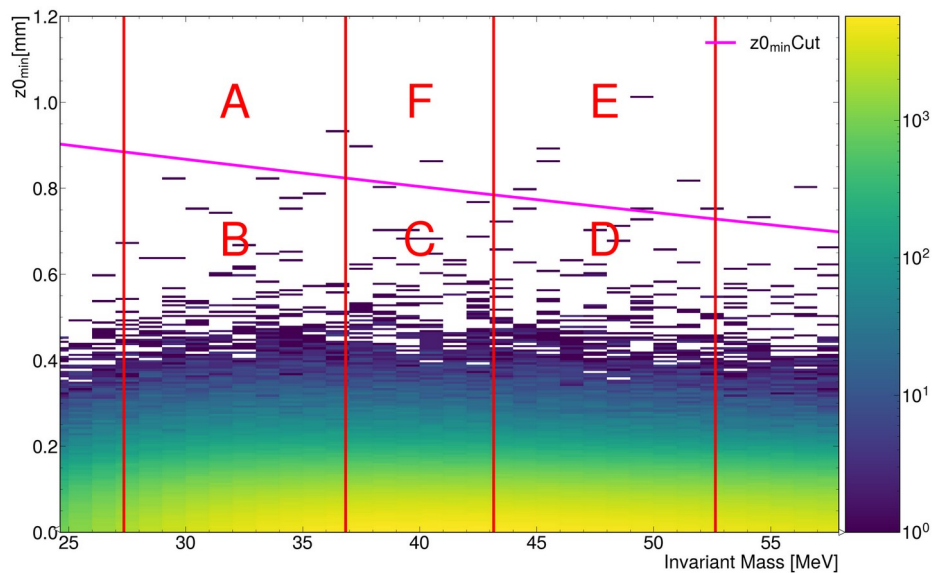
$z0_{\min}$ versus mass is \sim uncorrelated in narrow region centered on search window



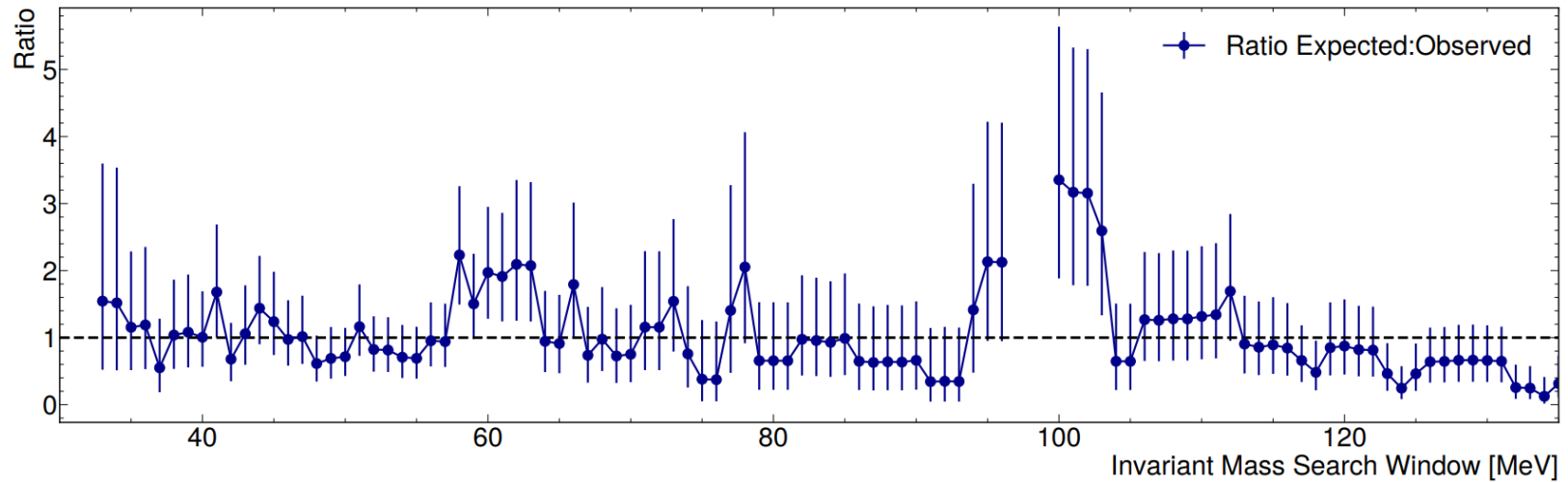
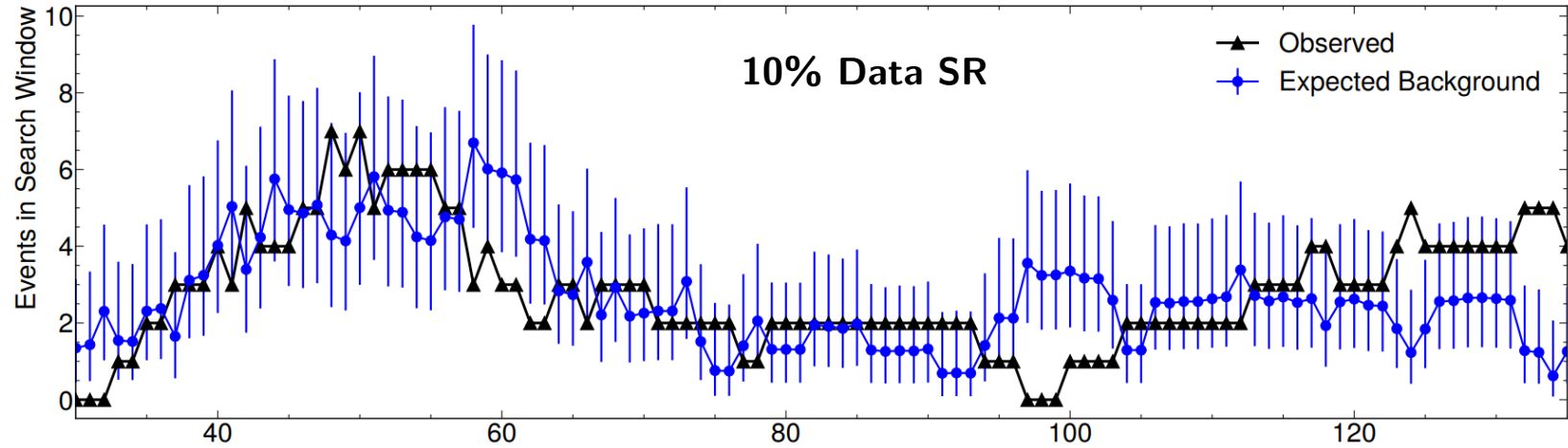
Background Estimation Method

*Two different search windows

Using left and right mass sidebands tends to cancel the small linear correlation on either side



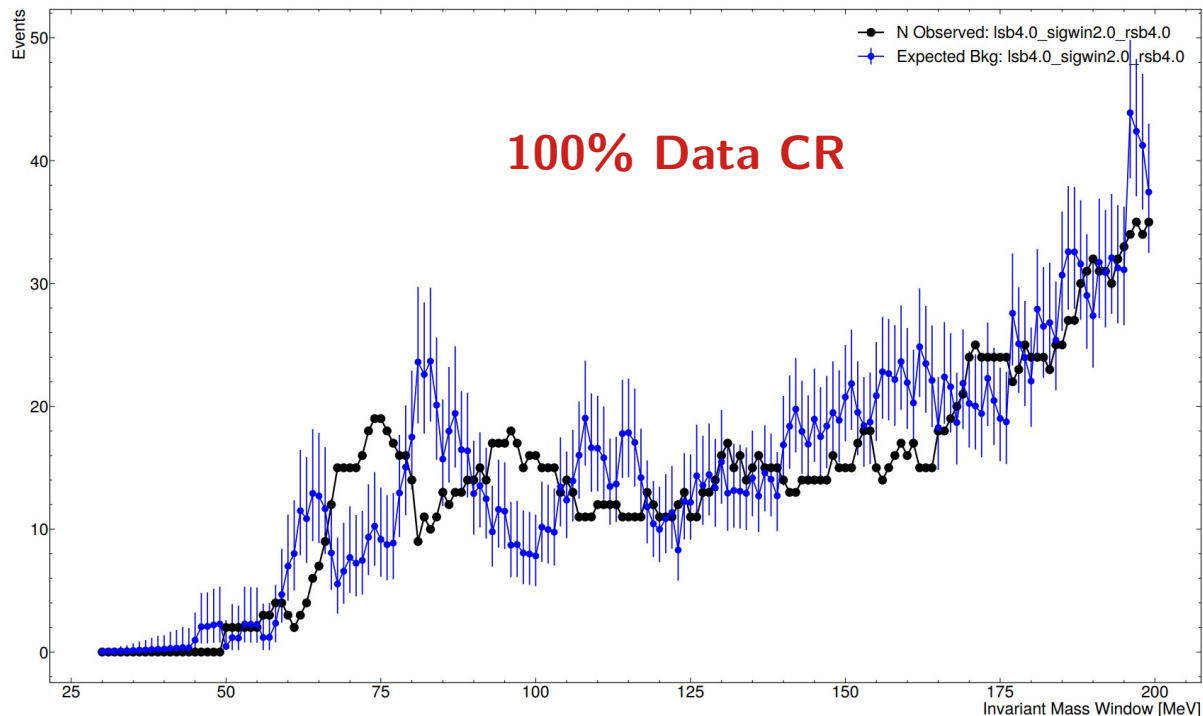
Background Estimation Method



Background Estimation Method

- **ONLY use 100% data CR** to evaluate how well background estimate reflects observed events
- Totally blind to 100% data SR
- **NO cuts are based on this study**

- *Larger statistics in this sample is convenient to test the ABCD mass sideband and search window size impact on background estimate quality
- *High psum vs low psum doesn't matter



Signal Search: Data Significance

Calculating P-Value using MC Toys

- Bkg-only test statistic is random sample of Poisson with mean bkg b

$$f(x) = \frac{b^k}{x!} e^{-b} \quad b = \left(\frac{A + E}{B + D} \right) C$$

- b calculated by sampling 3 parent distributions

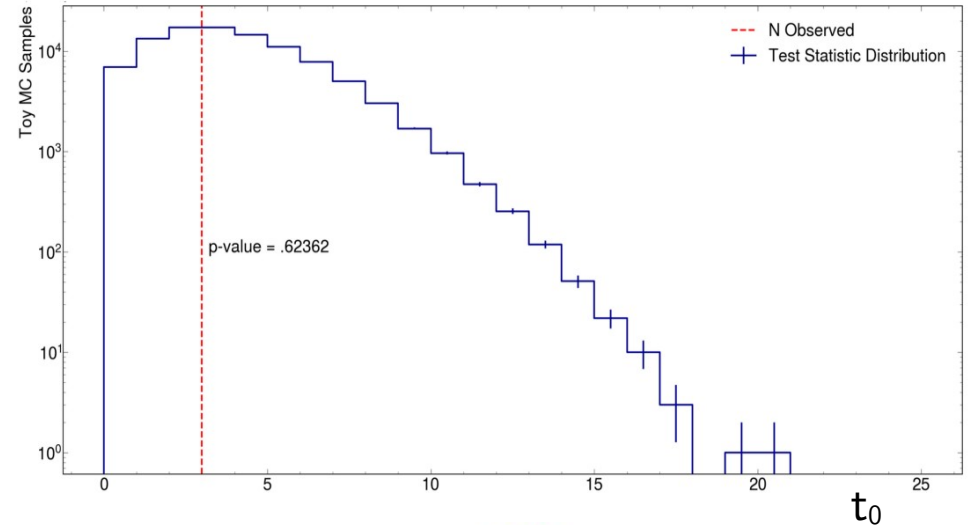
$$(B + D) \sim \mathcal{N}(B + D)$$

$$C \sim \mathcal{N}(C) \quad * \sigma_{\text{Normal}} = \text{sqrt}(N)$$

$$(A + E) \sim \text{Poisson}(A + E)$$

```
poisson_low_err = lambda n : np.sqrt(n - 0.25) if n >= 0.25 else 0.0  
poisson_up_err = lambda n : np.sqrt(n+0.75) + 1
```

- Build t_0 distribution using MC Toys (~100 million +)



$$P_{\text{local}} = \int_{t_{\text{obs}}}^{\infty} f(t_0) dt_0$$

Calculating P-Value using MC Toys

- **Bkg-only test statistic** is random sample of Poisson with mean bkg b

$$f(x) = \frac{b^k}{x!} e^{-b} \quad b = \left(\frac{A + E}{B + D} \right) C$$

- **Sample from 3 parent distributions**

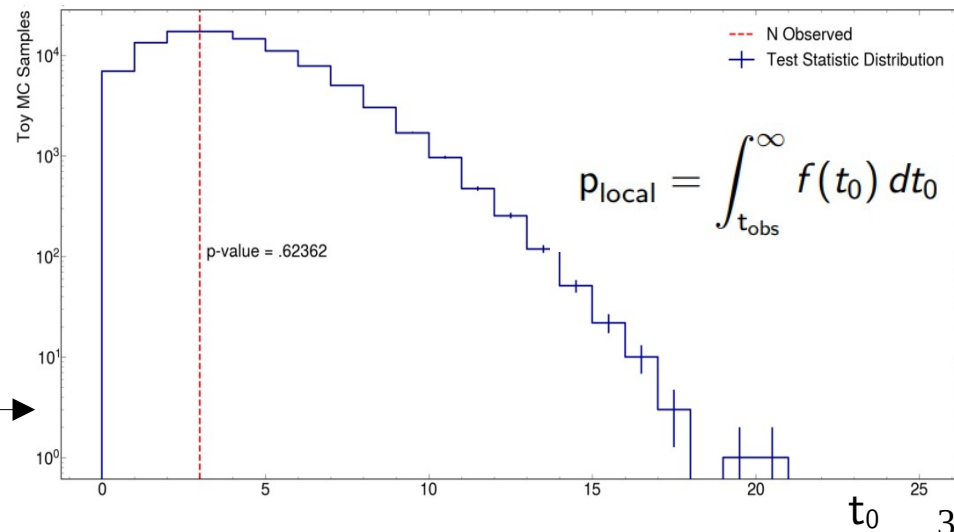
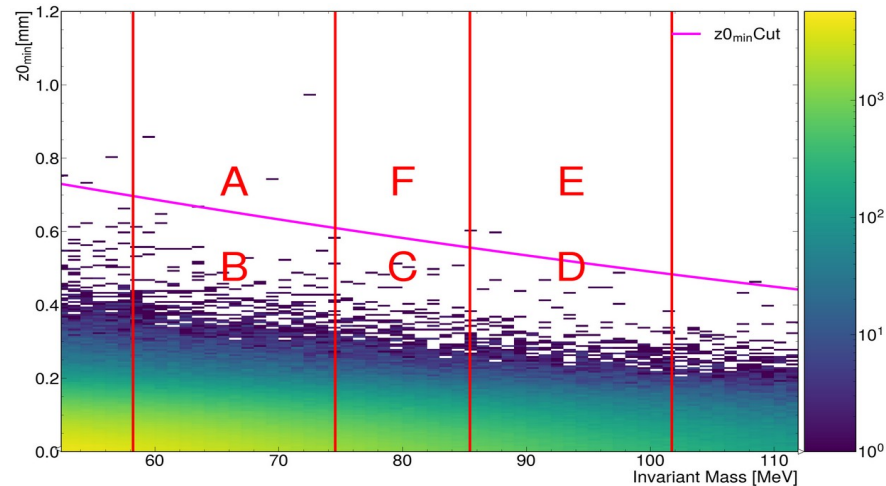
$$(B + D) \sim \mathcal{N}(B + D)$$

$$C \sim \mathcal{N}(C) \quad * \sigma_{\text{Normal}} = \text{sqrt}(N)$$

$$(A + E) \sim \text{Poisson}(A + E)$$

```
poisson_low_err = lambda n : np.sqrt(n - 0.25) if n >= 0.25 else 0.0
poisson_up_err = lambda n : np.sqrt(n+0.75) + 1
```

- **Build t_0 distribution using MC Toys**
(~100 million +)



Calculating P-Value using MC Toys

- **Bkg-only test statistic** is random sample of Poisson with mean bkg b

$$f(x) = \frac{b^k}{x!} e^{-b} \quad b = \left(\frac{A + E}{B + D} \right) C$$

- **Sample from 3 parent distributions**

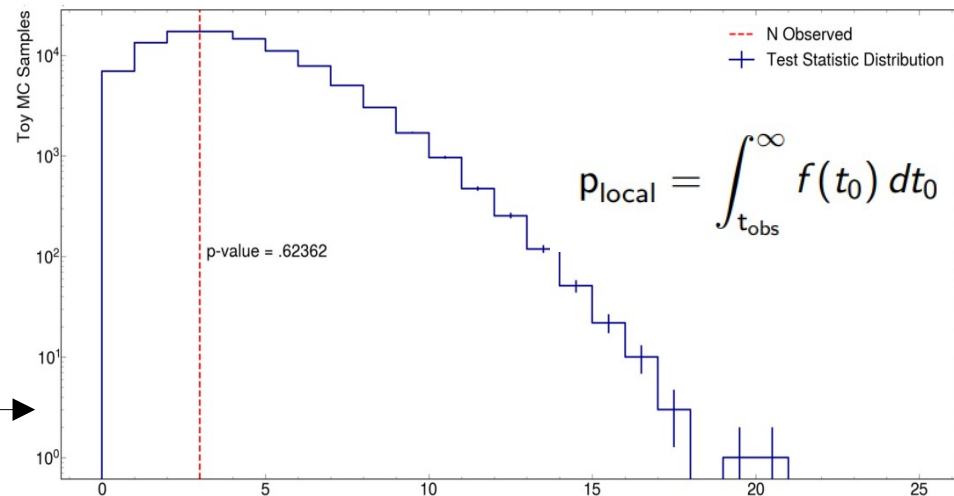
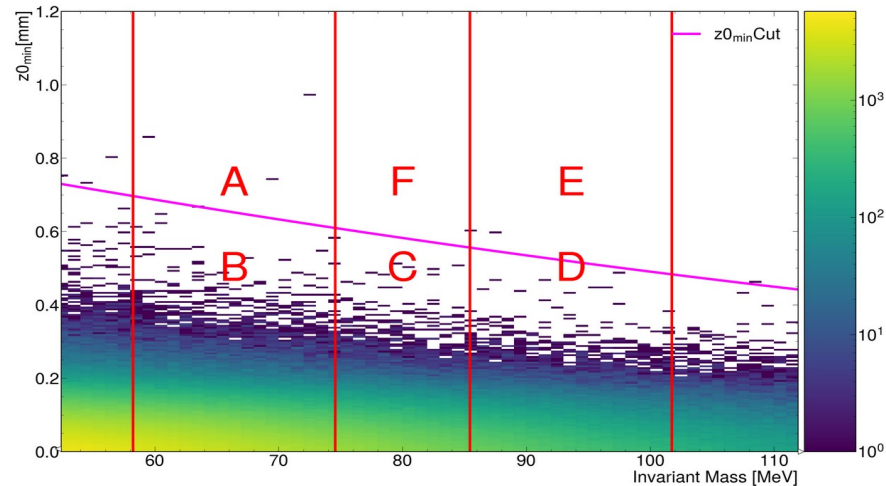
$$(B + D) \sim \mathcal{N}(B + D)$$

$$C \sim \mathcal{N}(C) \quad * \sigma_{\text{Normal}} = \text{sqrt}(N)$$

$$(A + E) \sim \text{Poisson}(A + E)$$

```
poisson_low_err = lambda n : np.sqrt(n - 0.25) if n >= 0.25 else 0.0
poisson_up_err = lambda n : np.sqrt(n+0.75) + 1
```

- **Build t_0 distribution using MC Toys**
(~100 million +)



Calculating P-Value using MC Toys

- **Bkg-only test statistic** is random sample of Poisson with mean bkg b

$$f(x) = \frac{b^k}{x!} e^{-b} \quad b = \left(\frac{A + E}{B + D} \right) C$$

- b calculated by **sampling 3 parent distributions**

$$(B + D) \sim \mathcal{N}(B + D)$$

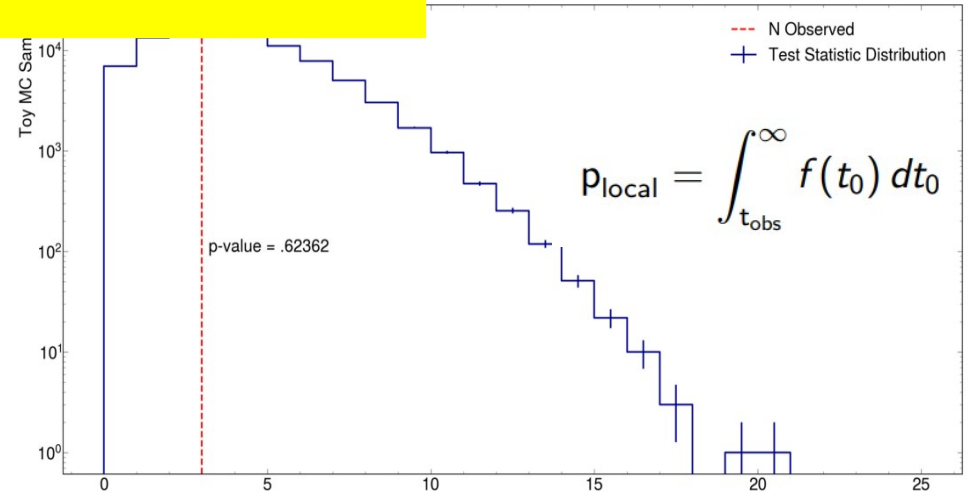
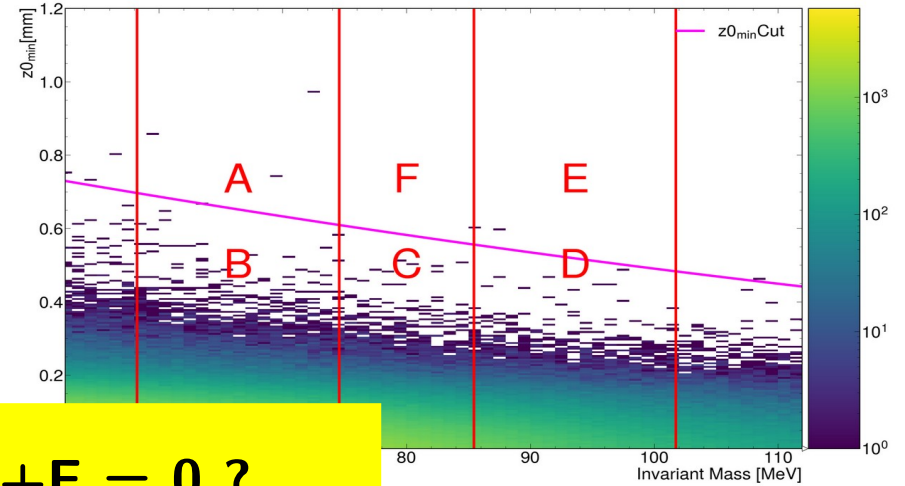
$$C \sim \mathcal{N}(C) \quad * \sigma_{\text{Normal}} = \text{sqrt}(N)$$

$$(A + E) \sim \text{Poisson}(A + E)$$

```
poisson_low_err = lambda n : np.sqrt(n - 0.25) if n >= 0.25 else 0.0
poisson_up_err = lambda n : np.sqrt(n+0.75) + 1
```

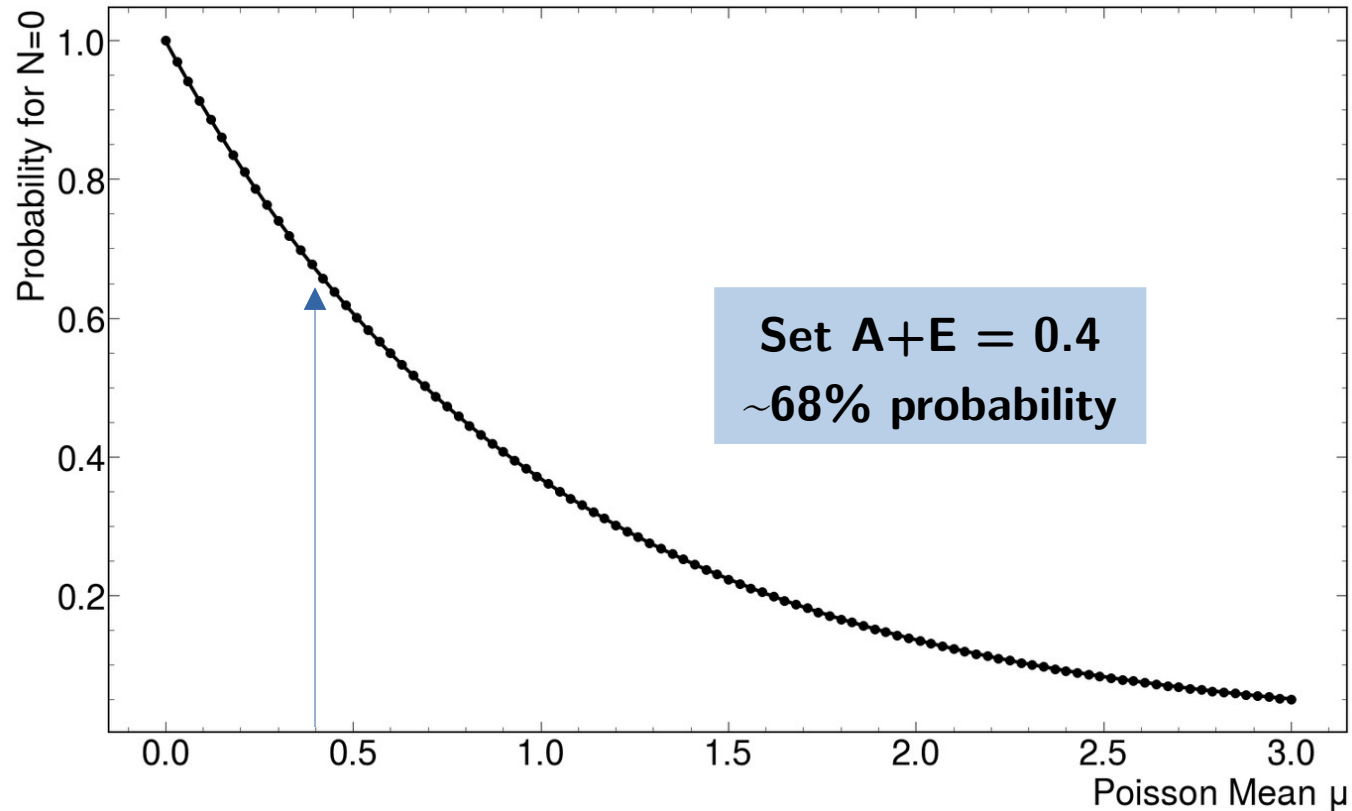
- **Build t_0 distribution using MC Toys** (~100 million +)

What if $A+E = 0$?



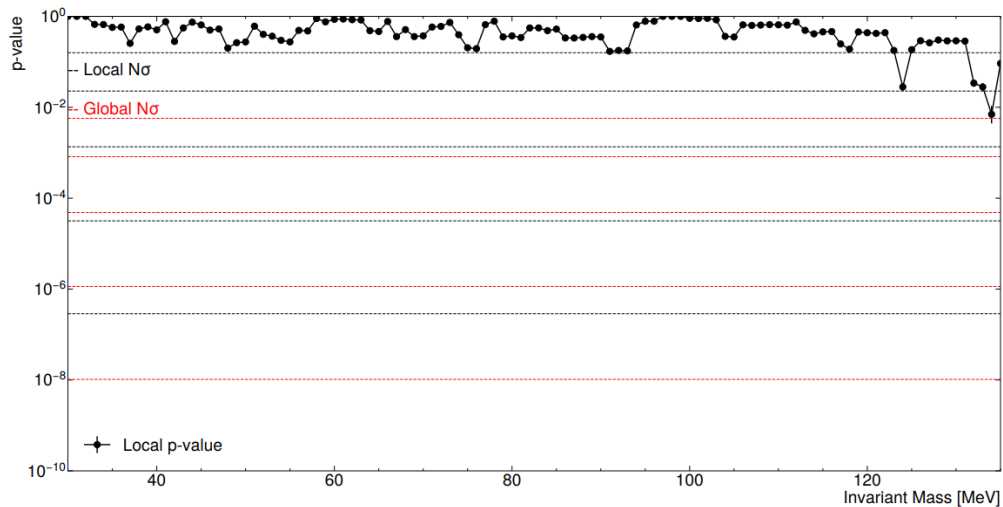
Error when $A+E = 0$?

- If $A+E = 0$, we can't build a Poisson distribution for the toys
- We could just force $A+E = 1$, but that's very conservative

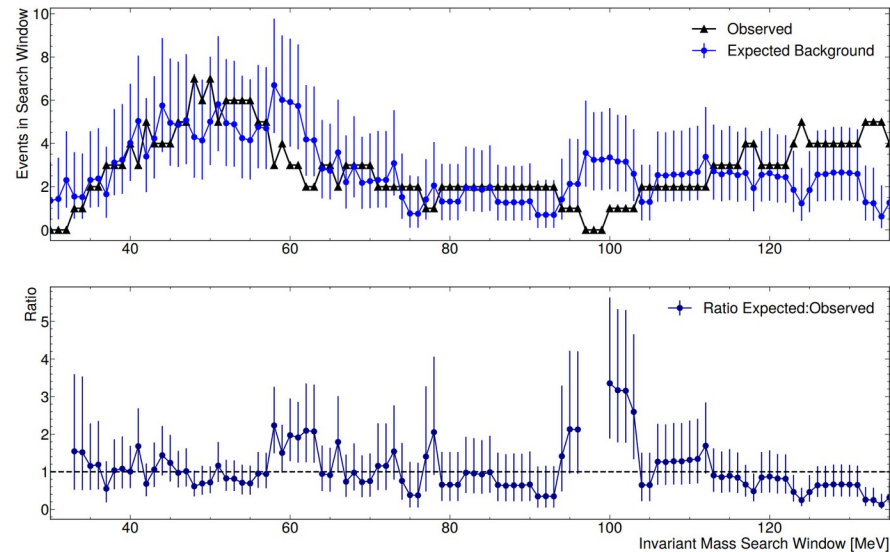


Calculating P-Value using MC Toys

Preliminary
10% Data SR

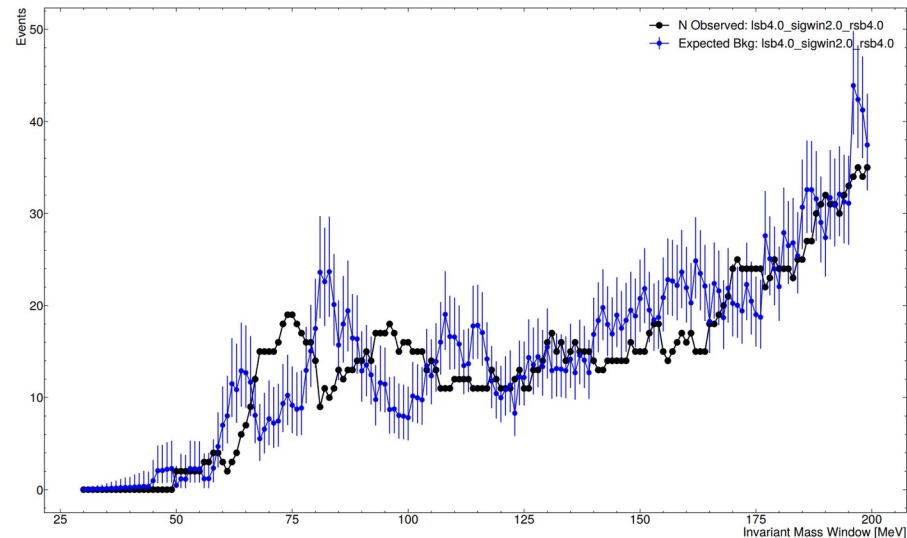
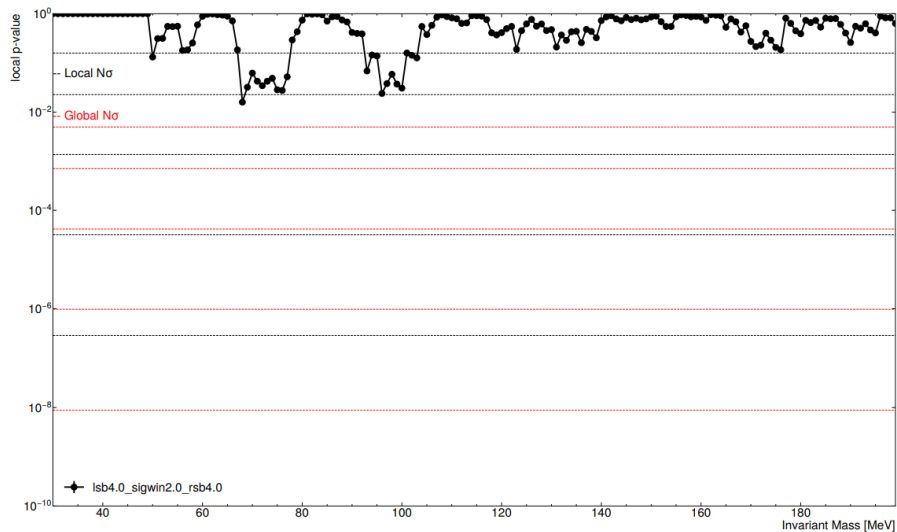


$$L_{corr} \approx \frac{m_{max} - m_{min}}{\sigma_{avg}}$$



Calculating P-Value using MC Toys

Preliminary *Just used as a sanity check
100% Data CR for higher statistics



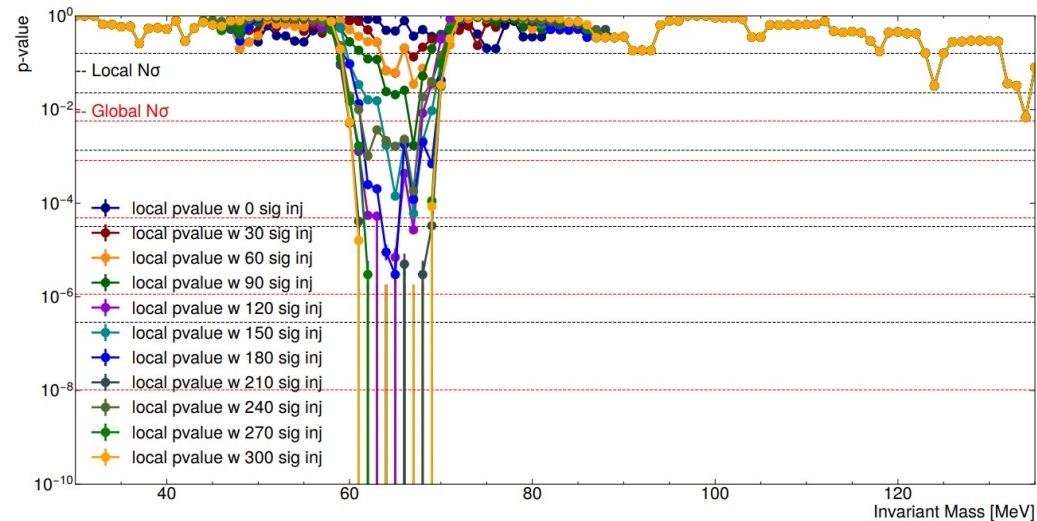
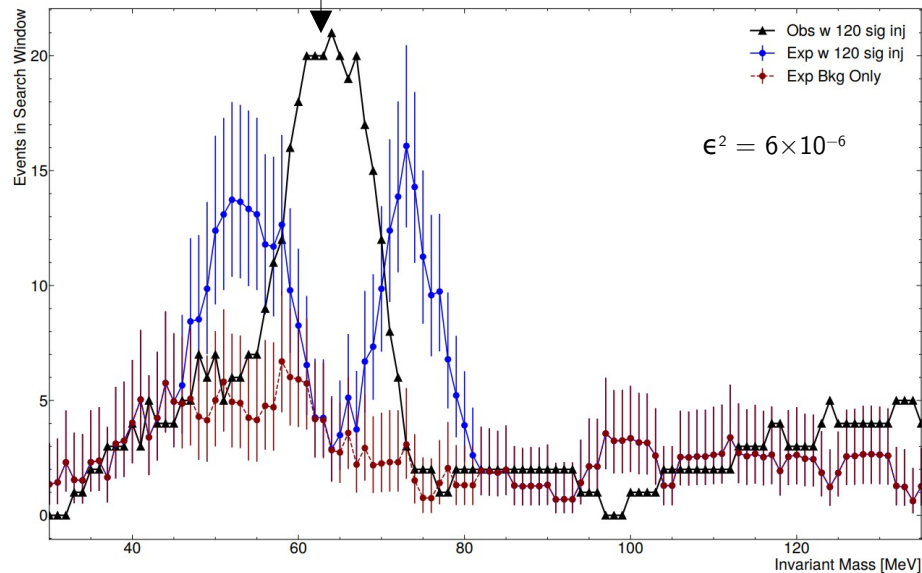
$$L_{corr} \approx \frac{m_{max} - m_{min}}{\sigma_{avg}}$$



Signal Injected P-Values

MC Signal injected at 64 MeV

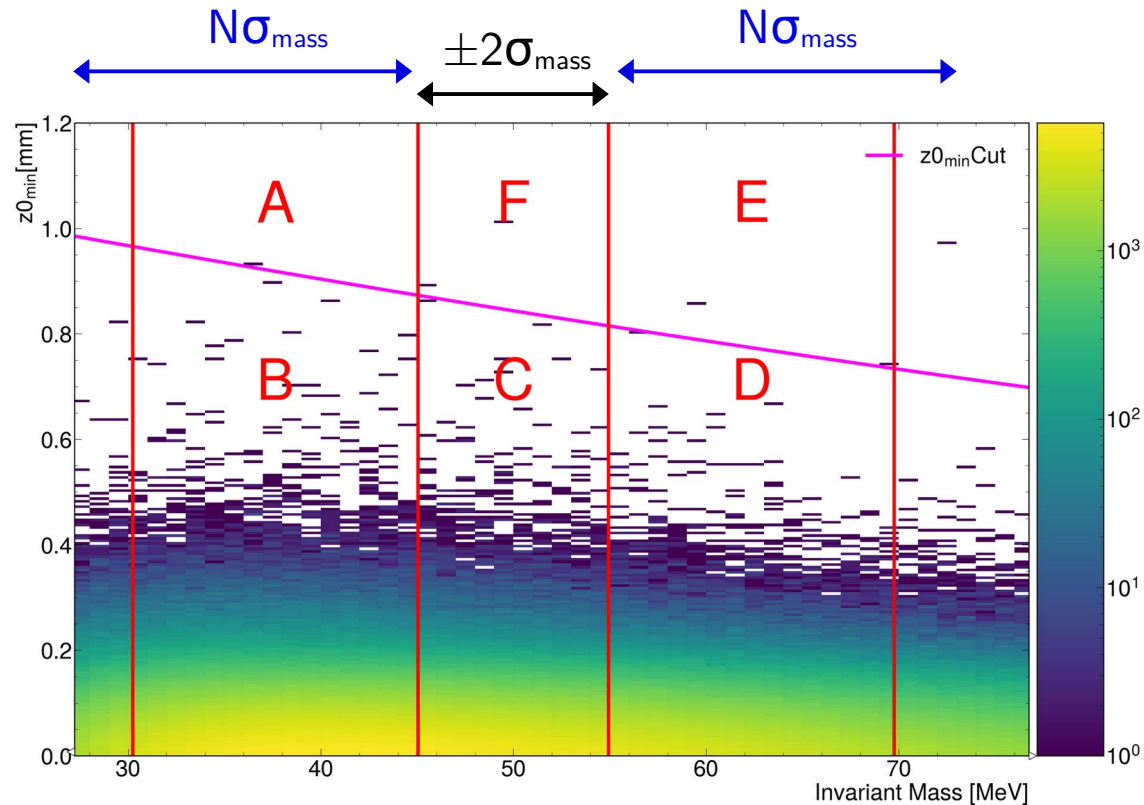
Preliminary
10% Data SR



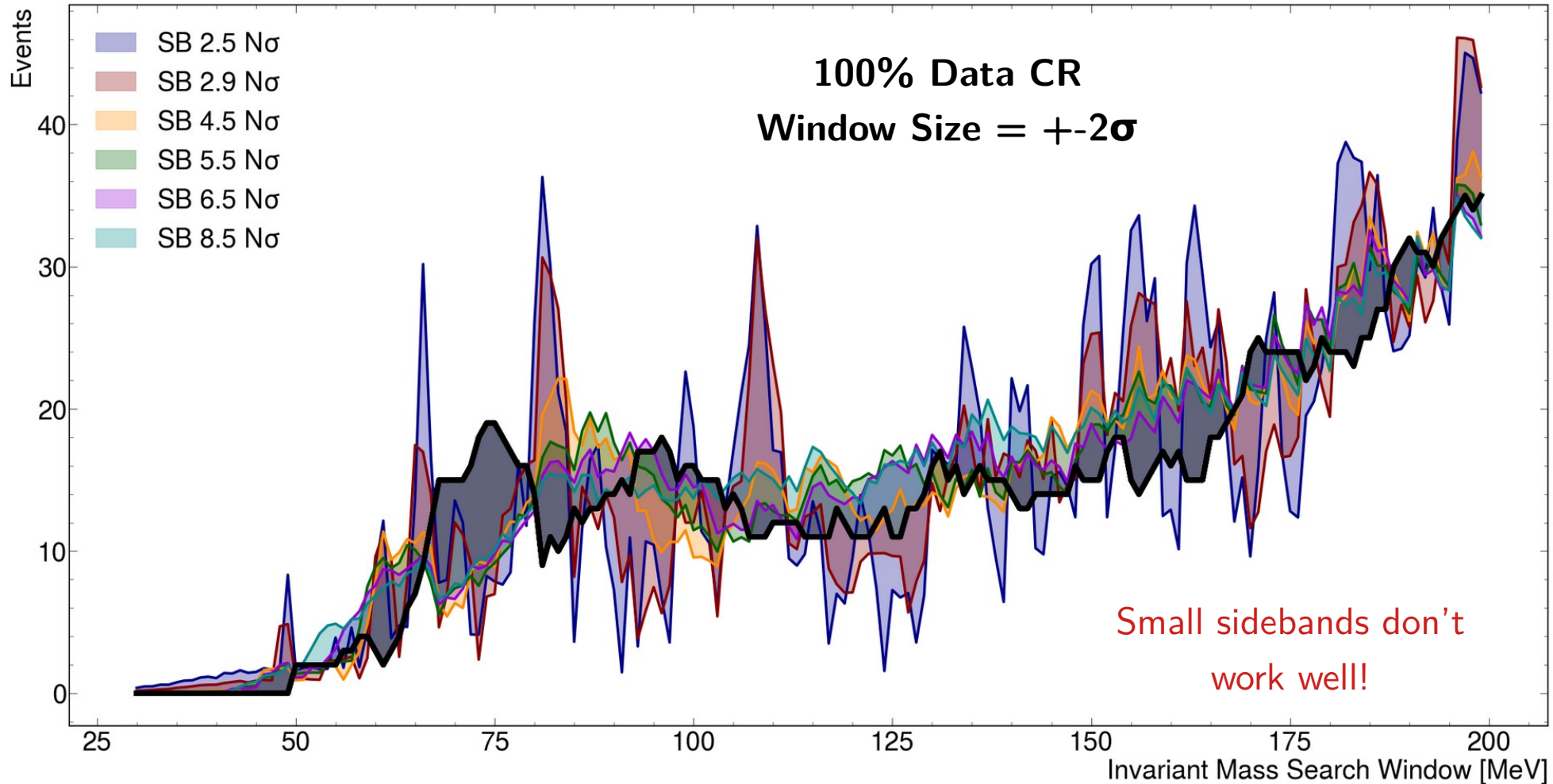
*Sanity check to see if p-values show evidence for signal



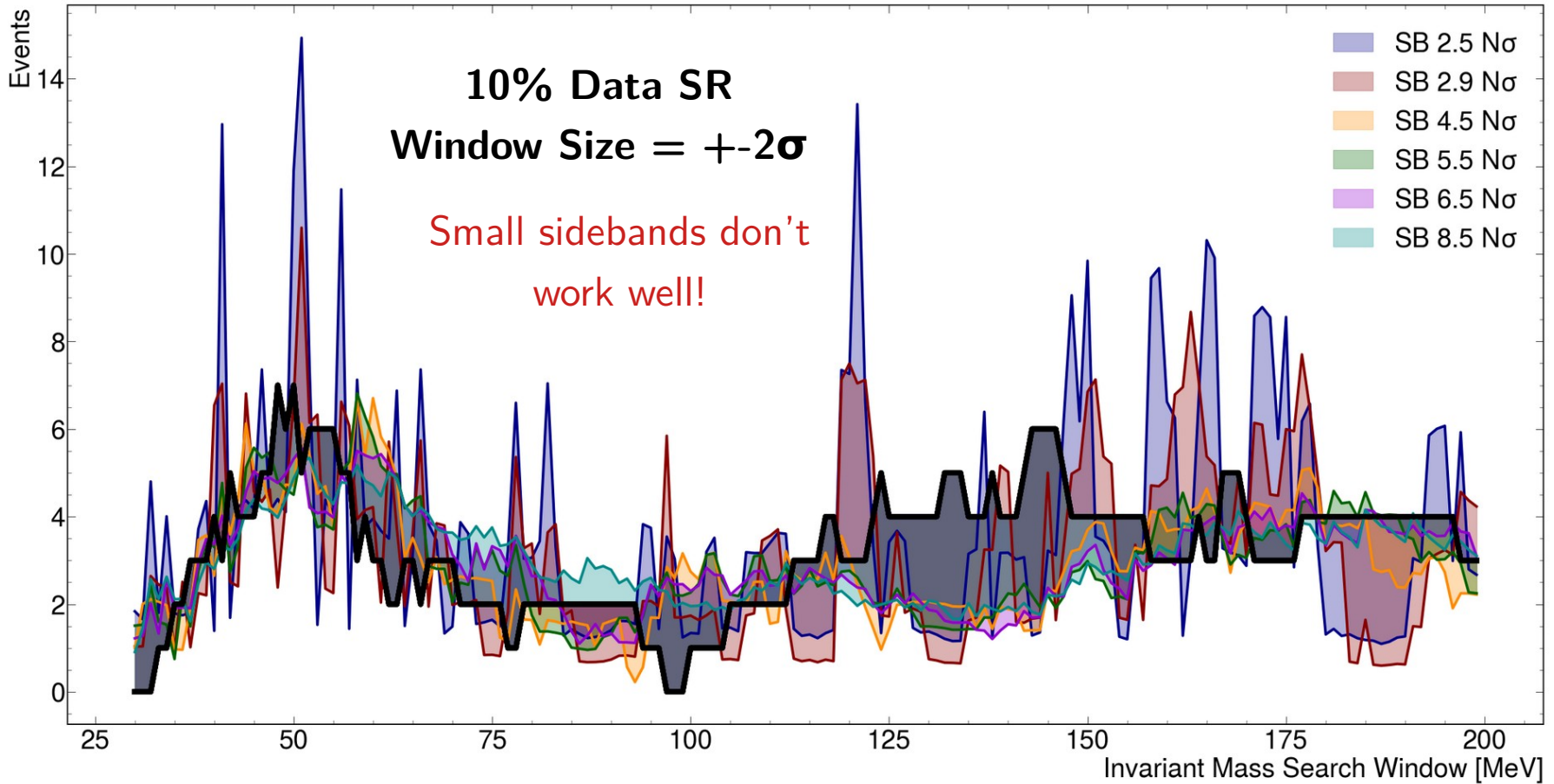
Optimize ABCD Mass Sidebands: $\pm 2\sigma$ Search Window



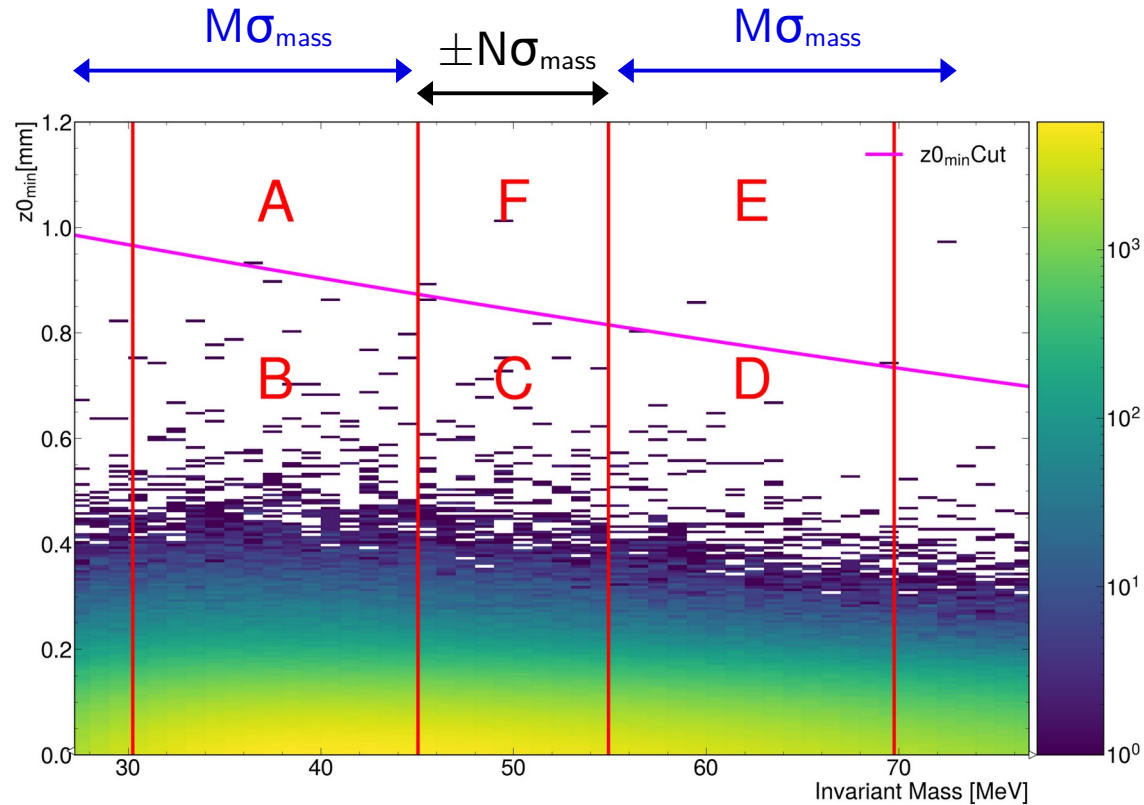
Optimize ABCD Mass Sidebands: $\pm 2\sigma$ Search Window



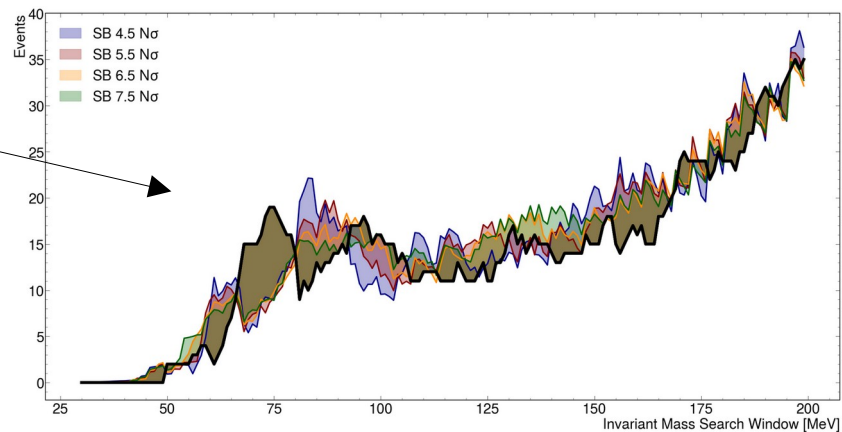
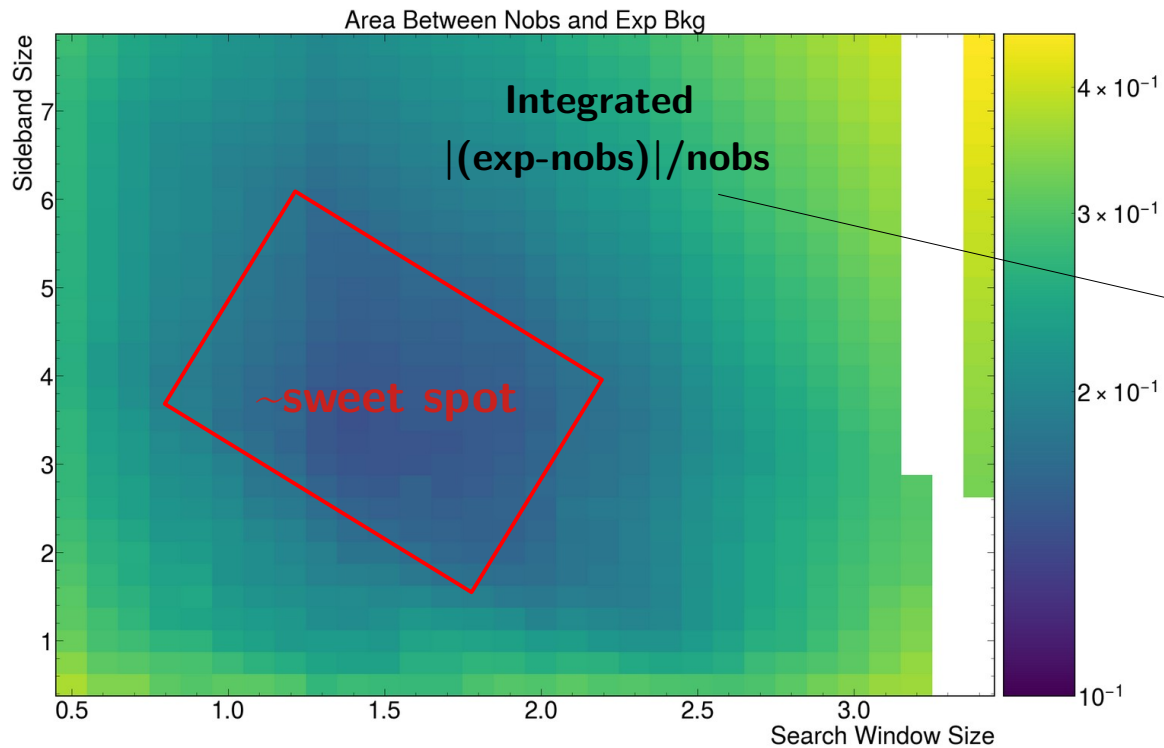
Optimize ABCD Mass Sidebands: $\pm 2\sigma$ Search Window



Optimize ABCD Mass Sidebands AND Search Window Size



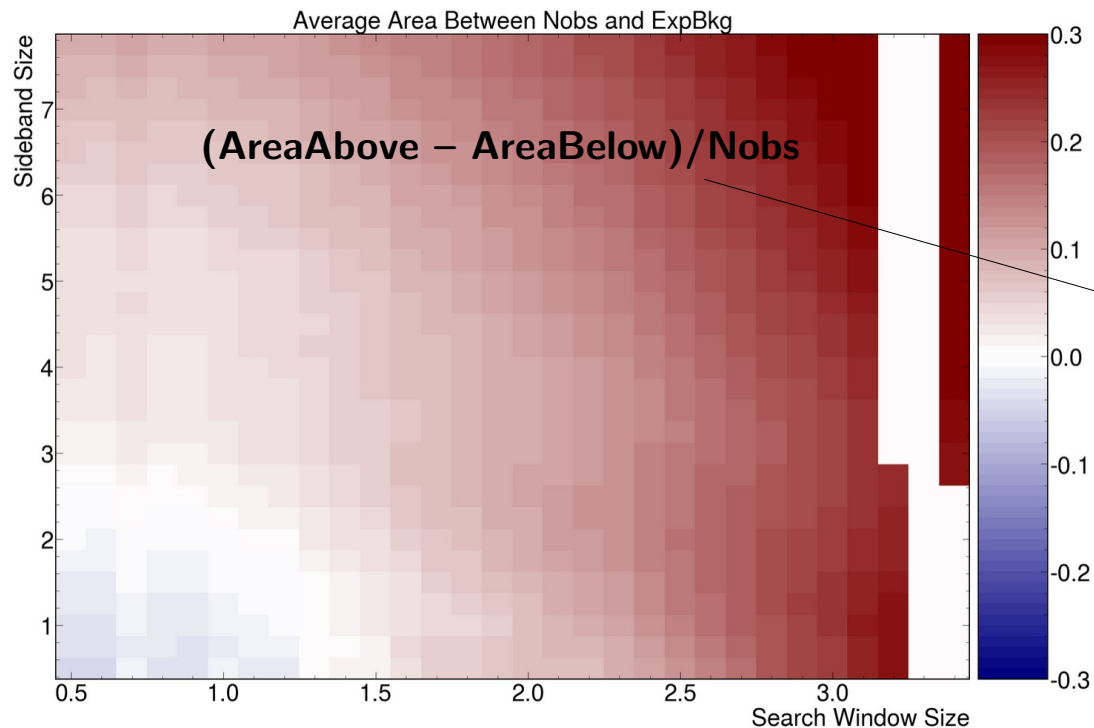
Scaled Area Between Observed and Expected



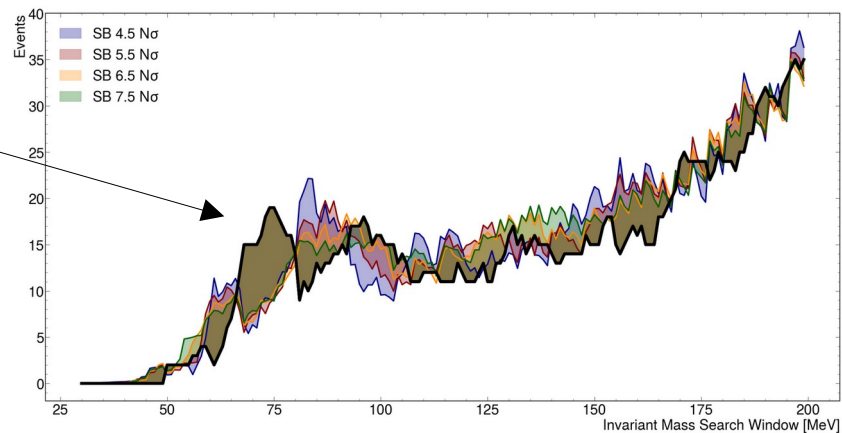
*Looks like Sideband width of 4σ
works for search windows $\pm 1-2.5\sigma$



Scaled Averaged Area Above and Below



*Search window too large
systematically overestimates bkg

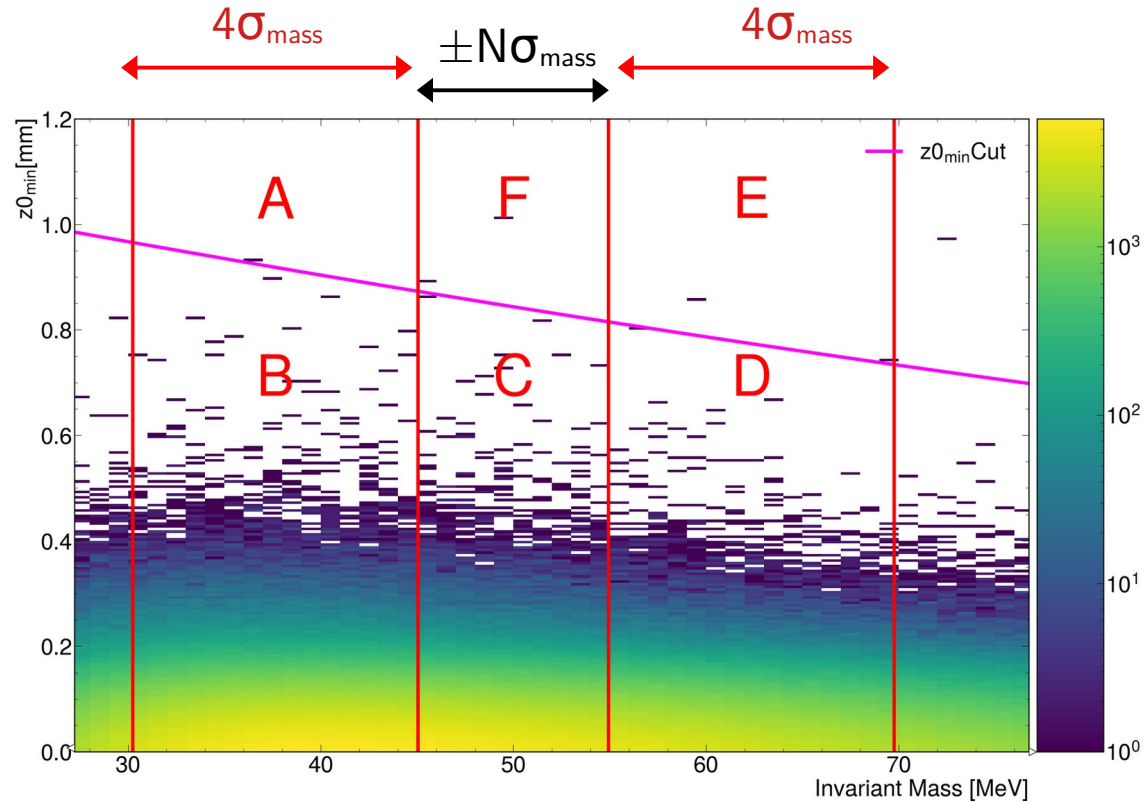


*Looks like **Sideband width of 4σ**
works for search windows $\pm 1-2.5\sigma$

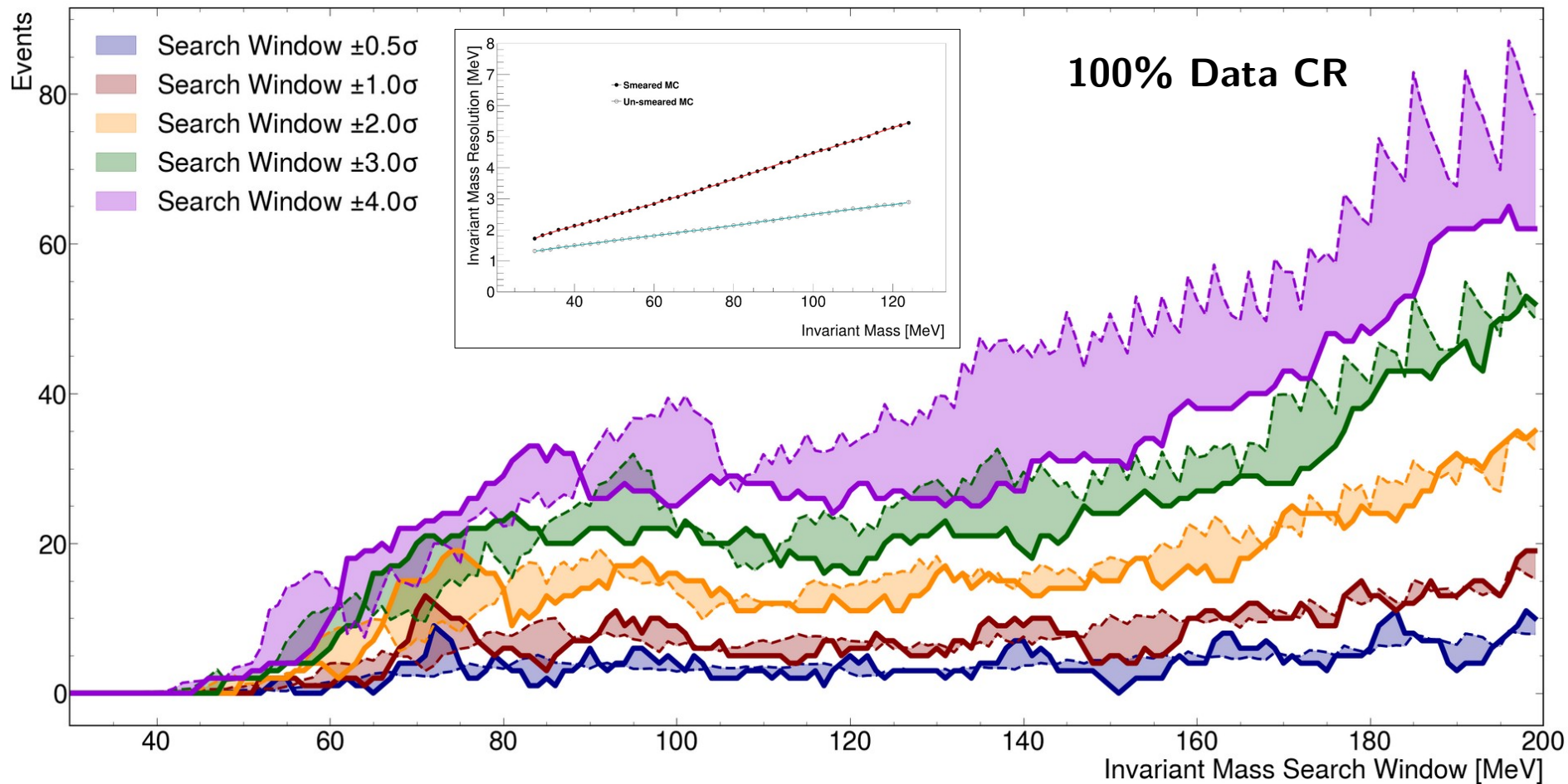


Optimize Search Window Size

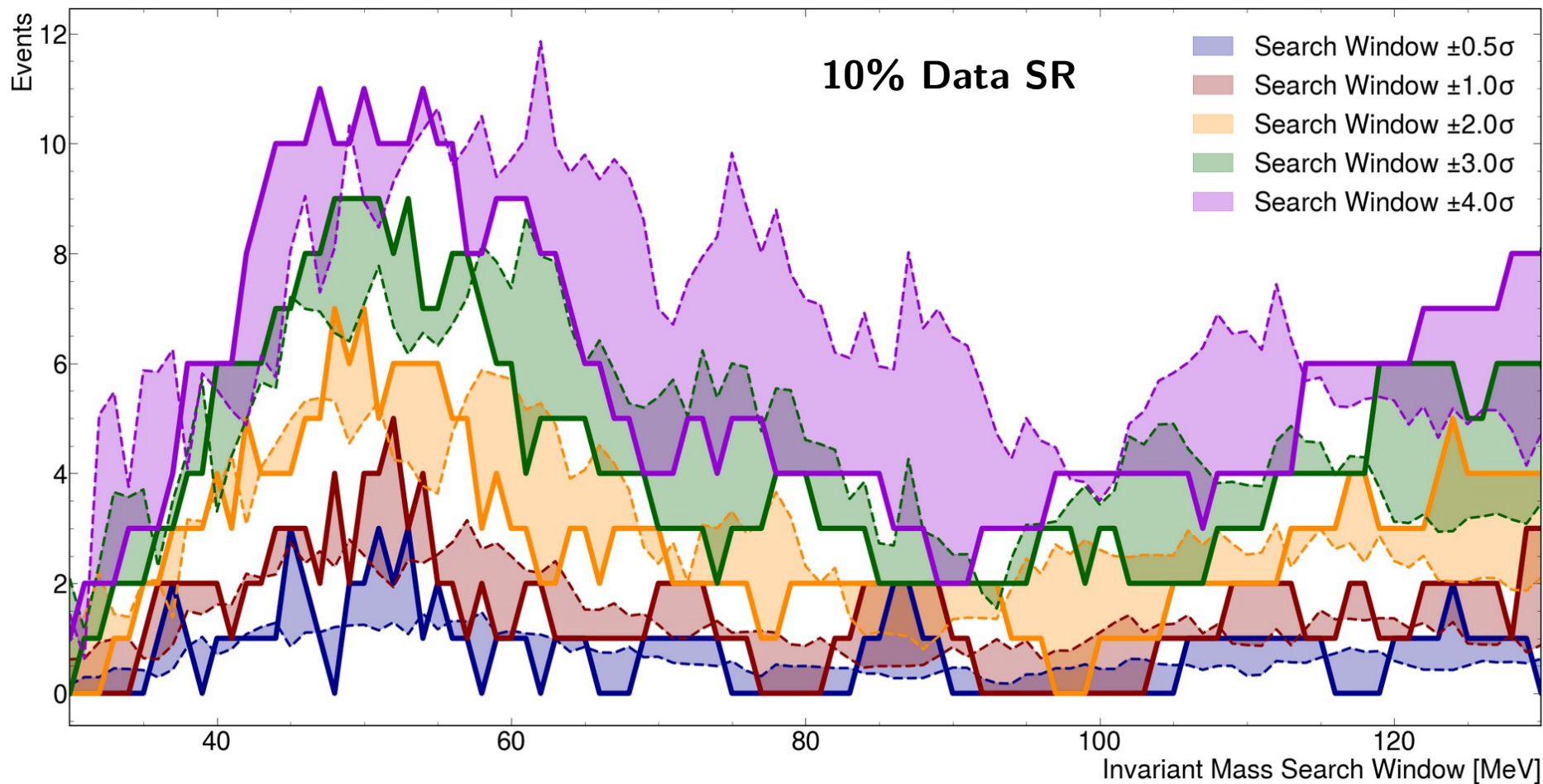
ABCD Mass Sideband = 4σ



Scan Signal Window – 100% CR Data

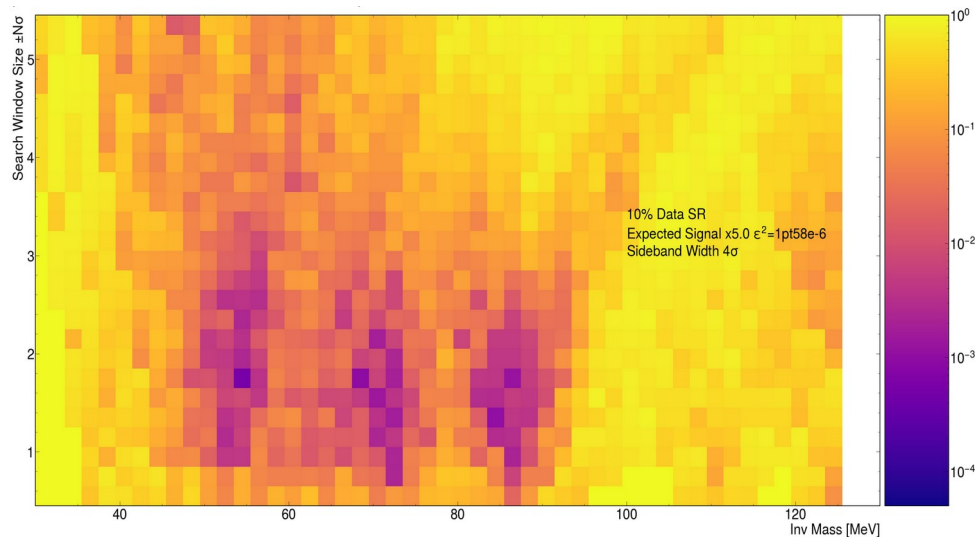
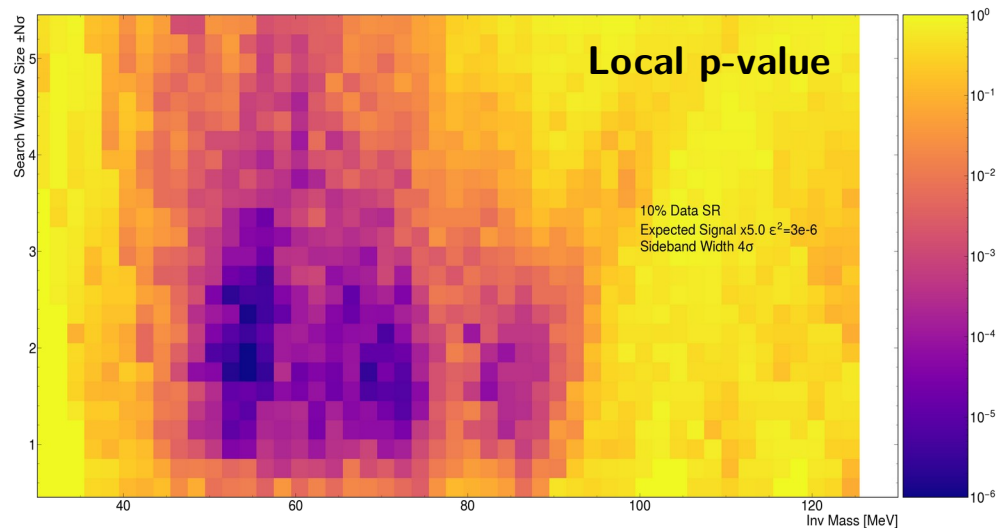


Scan Signal Window – 10% Data



MC Injected Signal – 10% Data

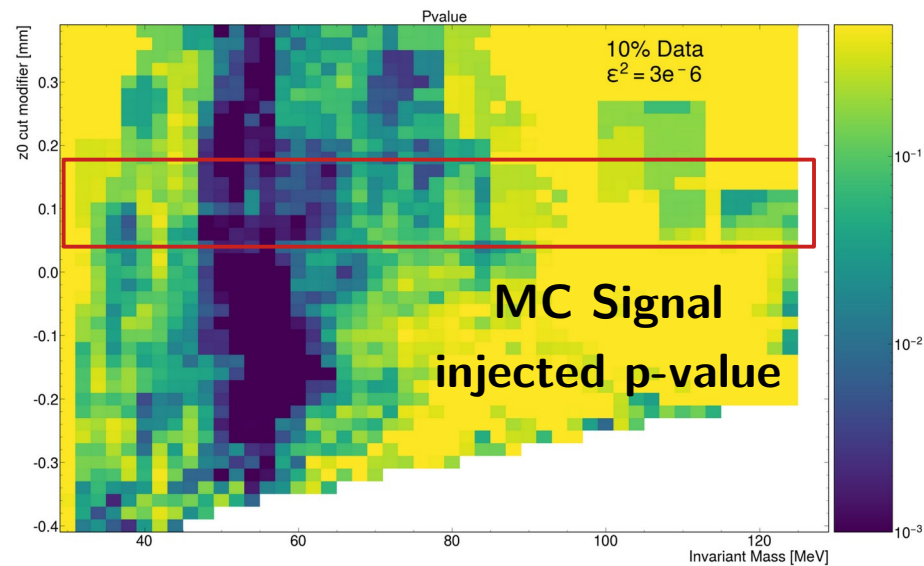
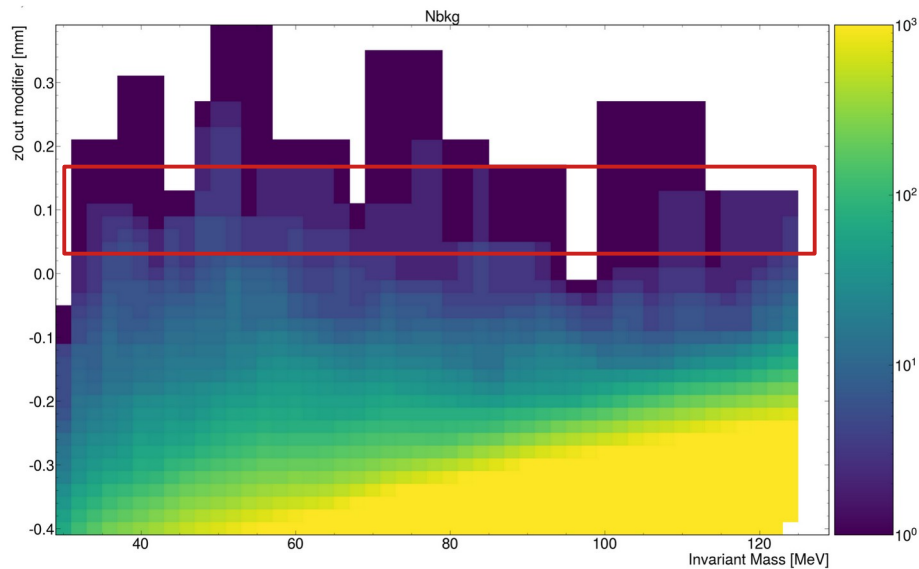
- Check impact of shrinking search window by measuring change in sensitivity
- Inject MC Signal at each mass
- Search window range $1.5\text{-}2.5\sigma$ results in similar sensitivity
- Confirmed for different values of ϵ^2
- Decide to use **Search Window = $\pm 1.5\sigma$**
- *Already shown the bkg estimate looks good for this search window size with **ABCD Mass Sideband Width = 4σ**



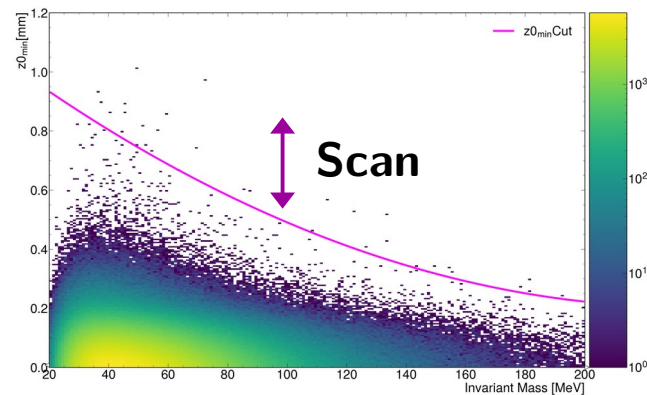
Further Tighten the $z0_{\min}$ Cut?

- *This cut was optimized on 10% Data SR
- *Want to protect against large statistical fluctuations when unblinding 100% Data SR

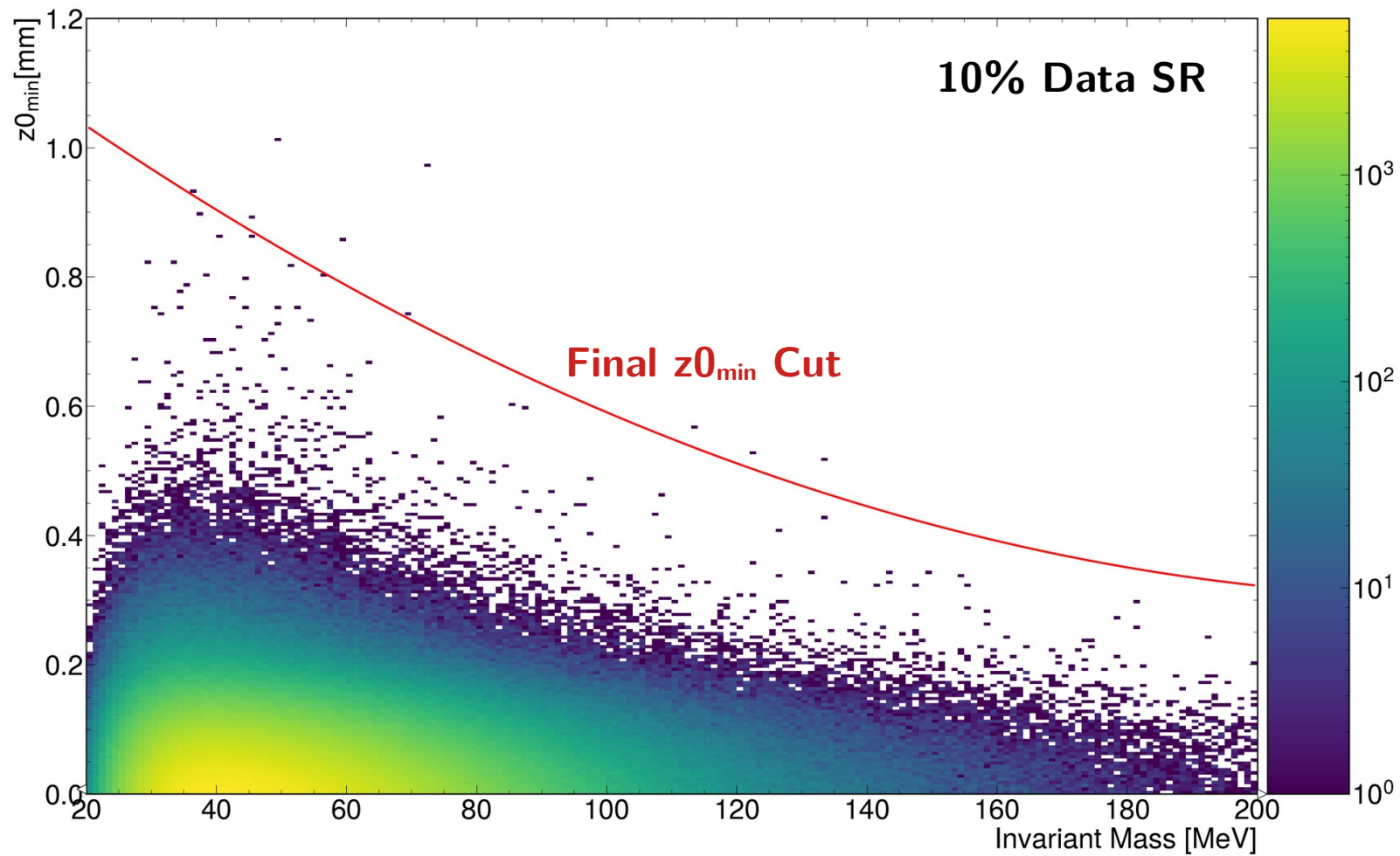
Tightening $z0_{\min}$ Cut



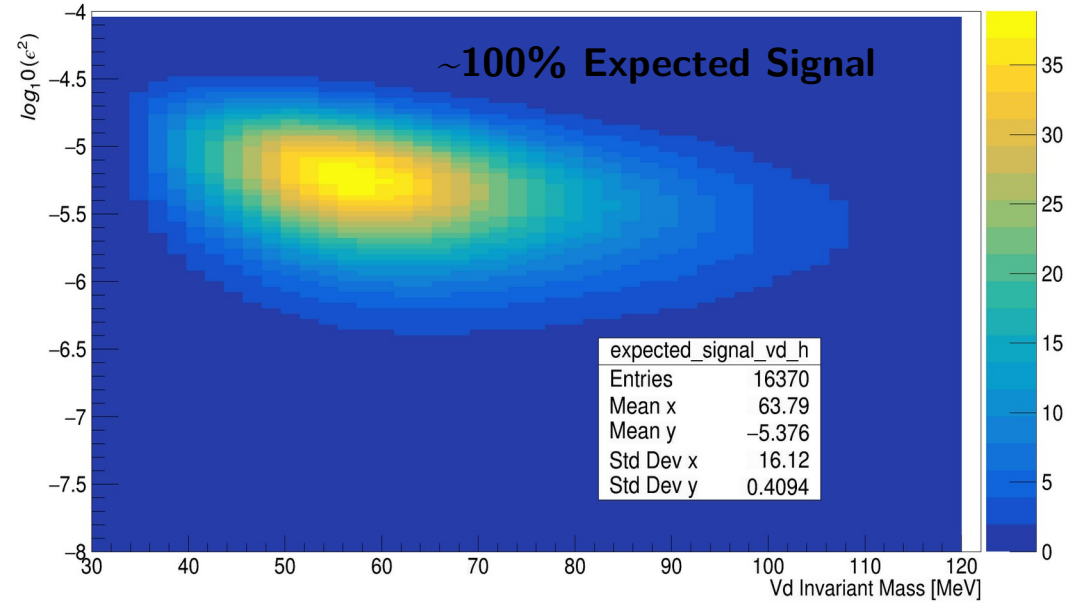
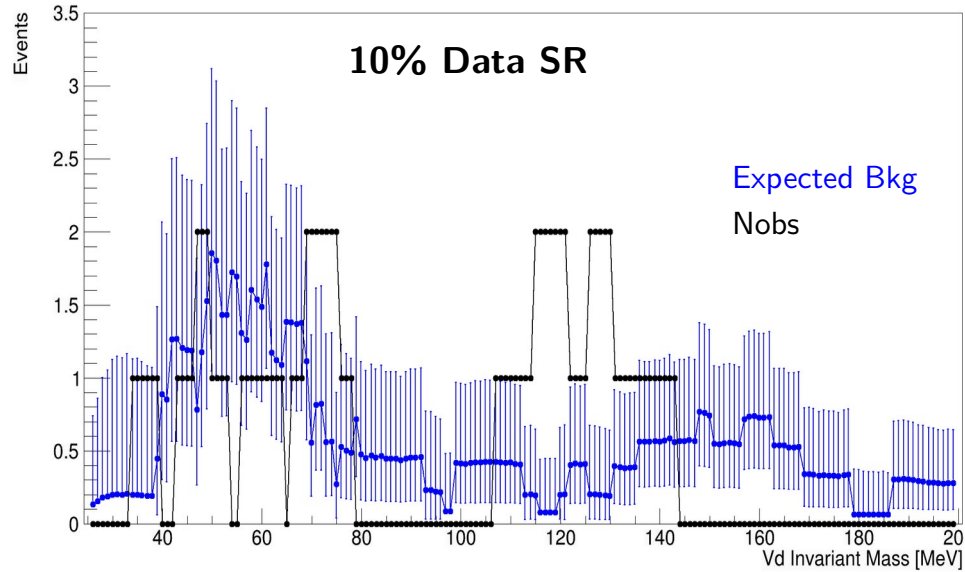
*Keep optimized shape,
tighten cut by simply adding
 $+N$ [mm] to cut polynomial



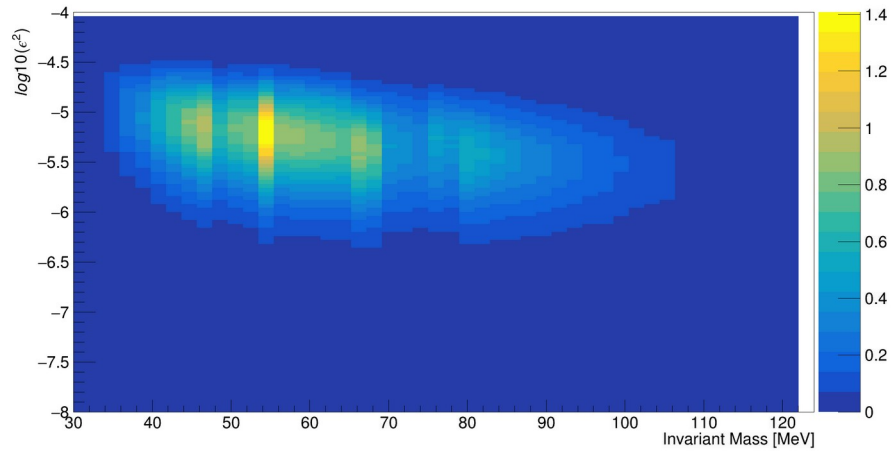
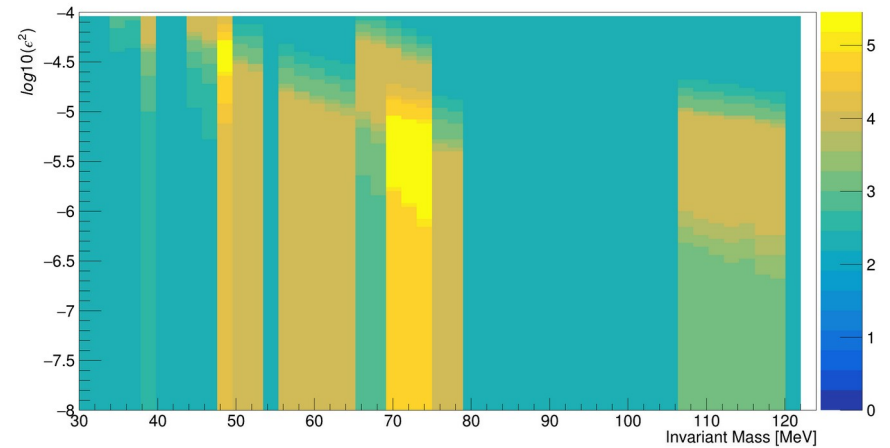
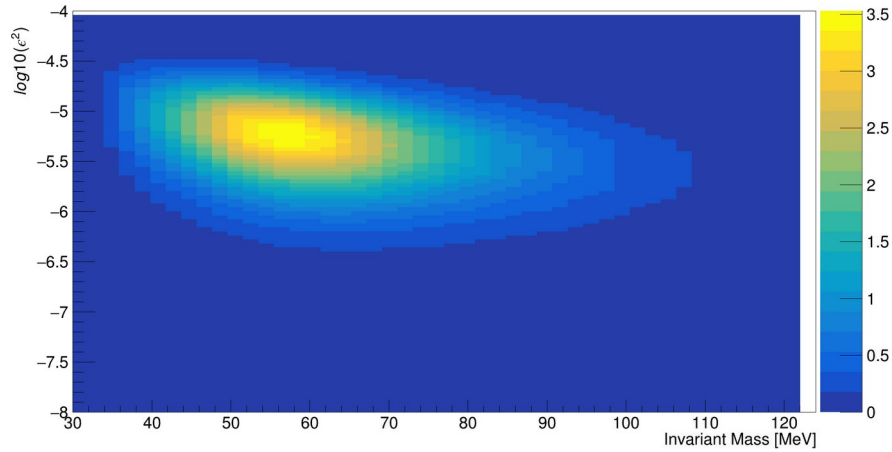
Tightening $z_{0\min}$ Cut



Final Selection - Background and Expected Signal



OIM Results for 10% Data



- Small region of exclusion in 10% data already

Backup

Preselection N-1 Cutflow Efficiency

	Data Eff	Tritrig-Beam Eff	WAB-Beam Eff	Tritrig-WAB-Beam Eff	40 MeV Signal Eff	100 MeV Signal Eff
$ e^- \text{Track}_t < 6.0 \text{ ns}$	1	1	1	1	1	1
$ e^+ \text{Track}_t < 6.0 \text{ ns}$	1	1	1	1	1	1
$\Delta_t(\text{Cluster}_{e^-}, \text{Cluster}_{e^+}) < 1.45 \text{ ns}$	0.96	0.99	0.99	0.99	0.98	0.98
$e^- \Delta_t(\text{Track}, \text{Cluster}) < 4.0 \text{ ns}$	0.99	1	1	1	1	1
$e^+ \Delta_t(\text{Track}, \text{Cluster}) < 4.0 \text{ ns}$	0.99	1	0.99	1	1	1
$e^- \text{Track} \chi^2 / n.d.f. < 20.0$	0.99	1	1	1	0.99	0.99
$e^+ \text{Track} \chi^2 / n.d.f. < 20.0$	0.98	1	0.98	0.99	0.99	0.99
$p_{e^-} < 1.75 \text{ GeV}$	1	1	1	1	1	1
$N_{2dhits} e_{\text{Track}}^- > 7.0$	1	1	1	1	0.93	0.98
$N_{2dhits} e_{\text{Track}}^+ > 7.0$	0.98	1	0.94	0.98	0.93	0.97
$Vt \chi^2 < 20.0$	0.83	0.97	0.65	0.86	0.97	0.97
$p_{e^-+e^+} < 2.4 \text{ GeV}$	0.99	1	0.99	1	1	1

Table 4: “n-1” cut efficiency. The efficiency of the cut under consideration is calculated assuming that all other cuts applied correspond to an efficiency of 1.