

The image features a 3D cutaway of the ATLAS detector, showing its complex internal structure with various layers and components. A central point of interaction is depicted with a dense, starburst-like pattern of yellow lines, representing particle tracks. Two red lines extend from this central point towards the bottom left, where they meet a larger, more detailed starburst of yellow lines. To the right, several blue 3D rectangular blocks are arranged in a semi-circular pattern, with red lines connecting them to the central interaction point. The background is black, and the overall scene is illuminated with various colors including yellow, red, blue, and green.

# Latest Diboson Polarization Results from ATLAS

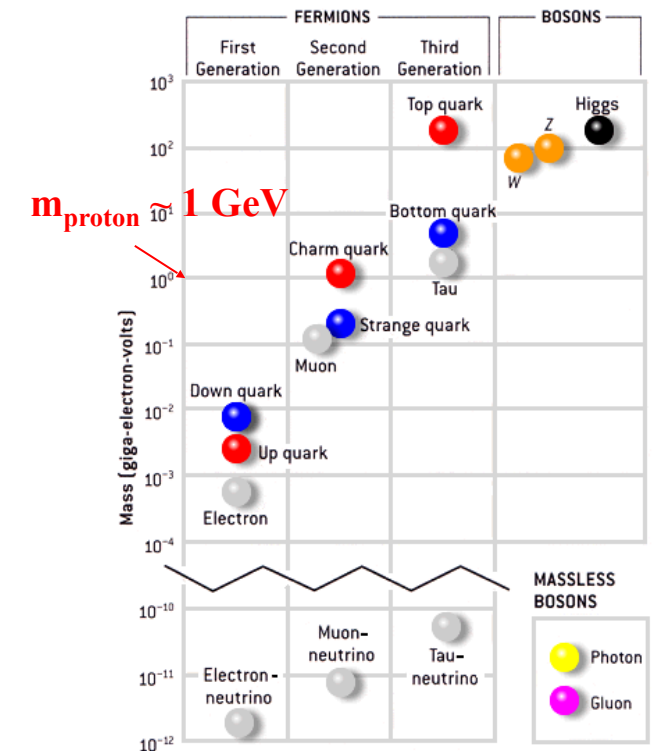
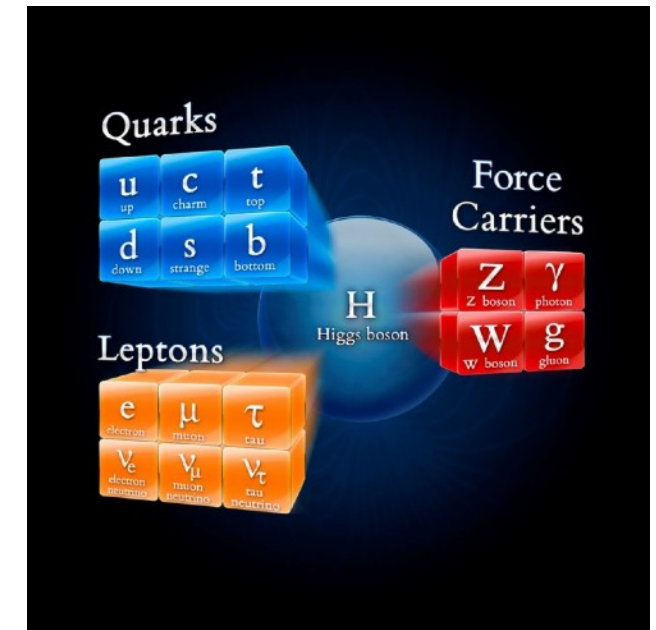
**Junjie Zhu**

**University of Michigan**

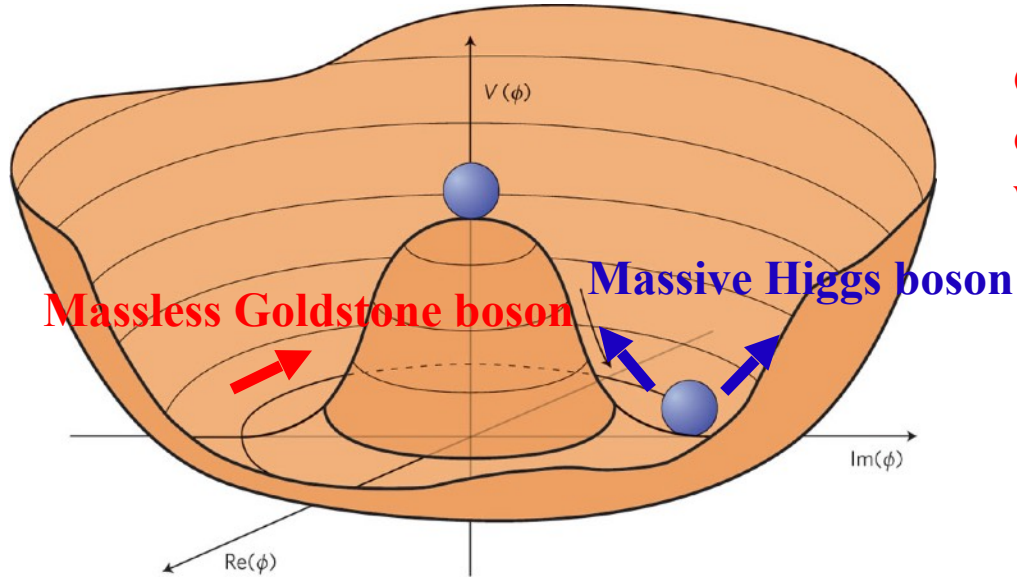
**May 14, 2024**

# Periodic table of SM particles

- All known elementary particles:
  - 12 matter particles – spin- $\frac{1}{2}$  fermions
    - 4 force carrier particles – spin-1 bosons (vector bosons)
      - Electromagnetic ( $\gamma$ ), weak ( $W^+/W^-$ ,  $Z$ ) and strong ( $g$ )
      - Electromagnetic and weak forces are unified to electroweak force
    - 1 Higgs particle – spin-0 boson (scalar boson)
- Mass puzzles:
  - Different particles have different masses, and their masses are dramatically different
  - $W$ ,  $Z$  and  $\gamma$  are electroweak force carriers, but have different masses
  - According to symmetries in the SM, all particles should be massless

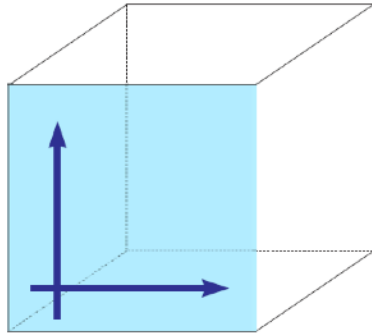


# Spontaneous symmetry breaking and the Higgs mechanism



Consider an example of a complex Higgs field (2 DOFs) with a non-zero vev

Two transverse modes of massless vector field:



Massless vector boson

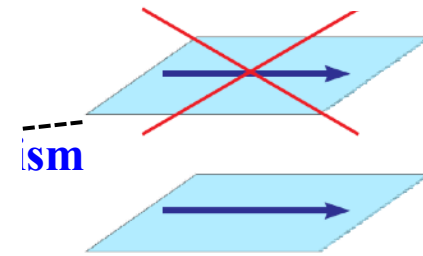
Complex scalar field (2 degrees of freedom):



Higgs field

SSB  
→

Massless Goldstone boson



Massive vector boson

Higgs boson

Only massive particles can have longitudinal modes → the original massless vector boson now becomes massive

# Spontaneous symmetry breaking and Higgs mechanism

4 massless vector bosons ( $W^+$ ,  $W^-$ ,  $Z$ ,  $\gamma$ )

$$4 \times 2 + 4$$

4 DOFs for the Higgs sector  
(the real Higgs field is a weak isospin doublet)

2 transverse modes

1 massive Higgs boson and 3 massless  
Goldstone bosons after SSB

**Higgs mechanism:** Massless Goldstone bosons are “eaten”  
by massless vector bosons and become their longitudinal modes

3 massive bosons ( $W^+$ ,  $W^-$ ,  $Z$ )    Massless  $\gamma$     the Higgs boson

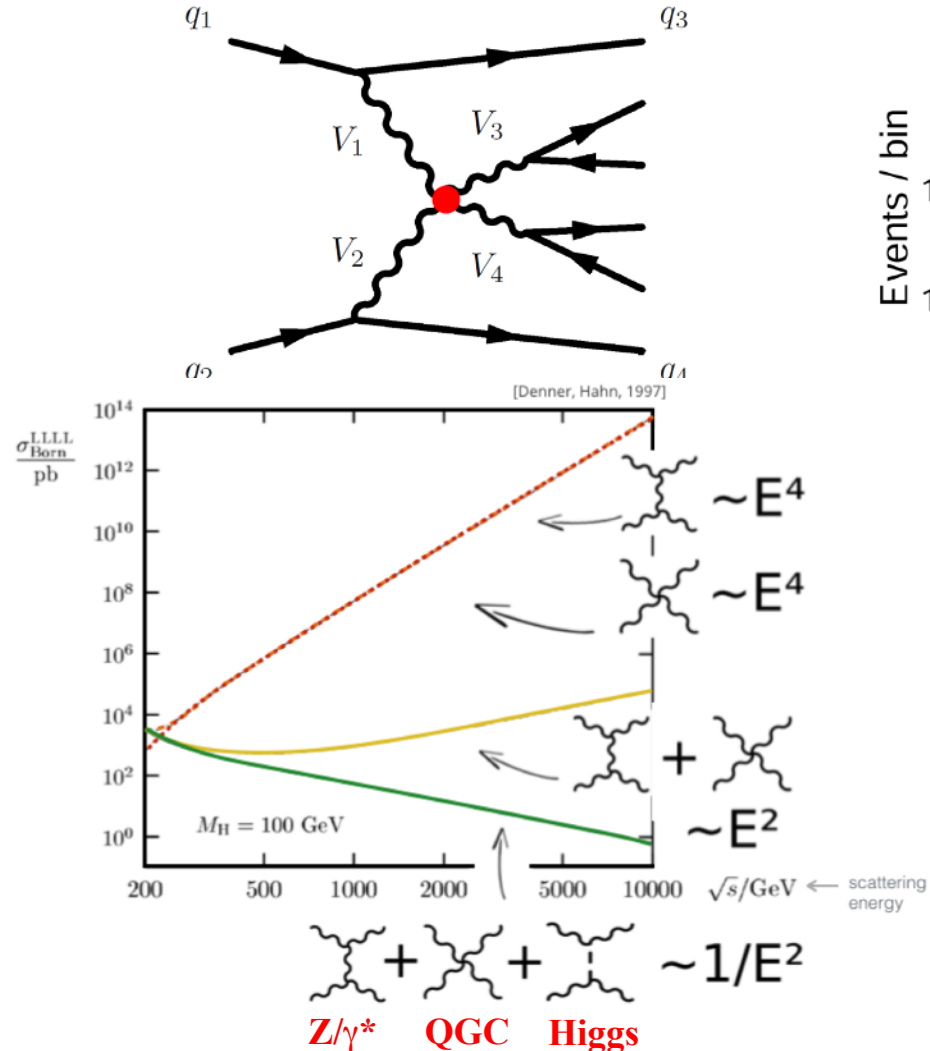
$$3 \times 3 + 2 + 1$$

2 transverse modes +  
1 longitudinal mode

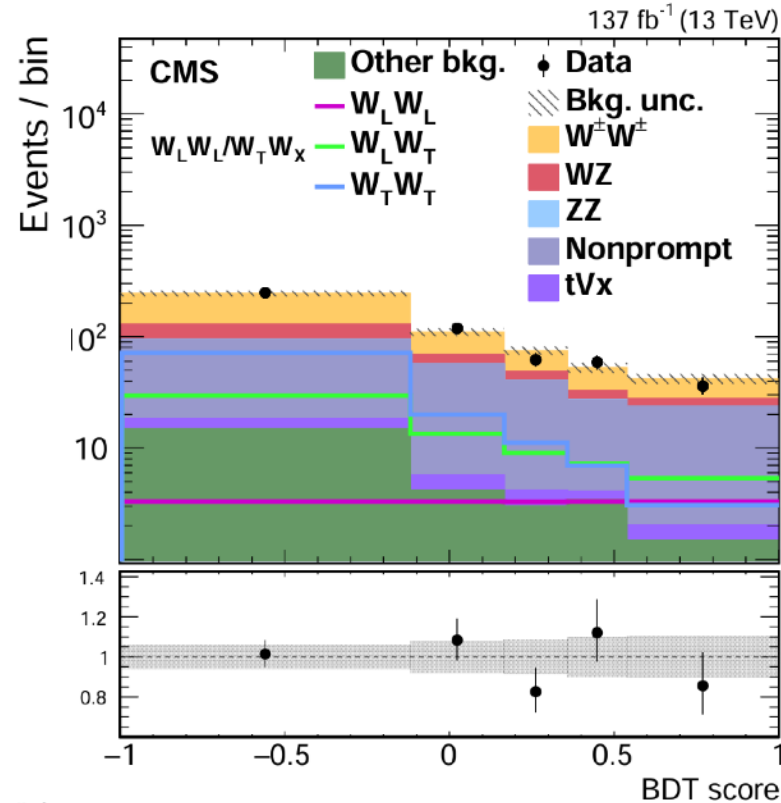
- Masses of matter particles (Fermions) come from the Yukawa coupling between the particle and the Higgs field

# Vector boson scattering

- Studies of polarized electroweak bosons are gaining interest in both experimental and theoretical communities these days: mainly **VBS** and **diboson (VV, VH)** processes
- VBS**: unitarity conservation in scattering of the longitudinal modes of W/Z bosons ( $V_L V_L \rightarrow V_L V_L$ )



PLB 812 (2021) 136018



16  $W_L W_L$  events expected with a total background of 506 events

Diboson polarization measurements at ATLAS:

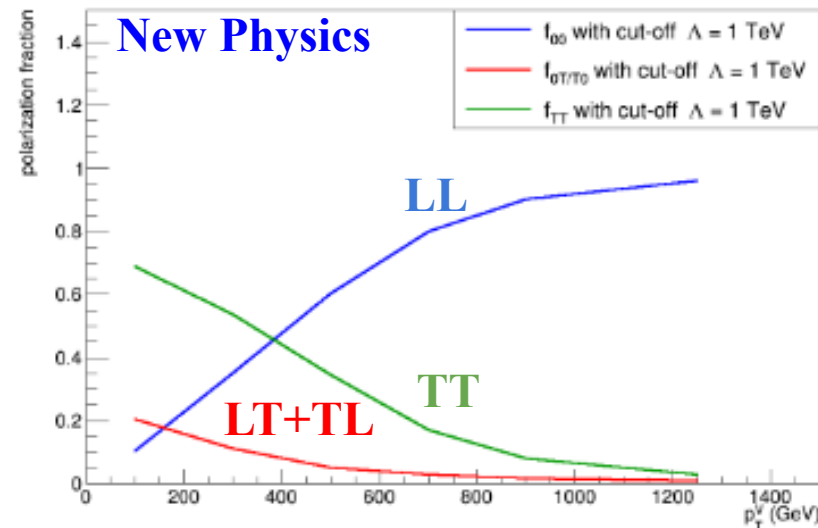
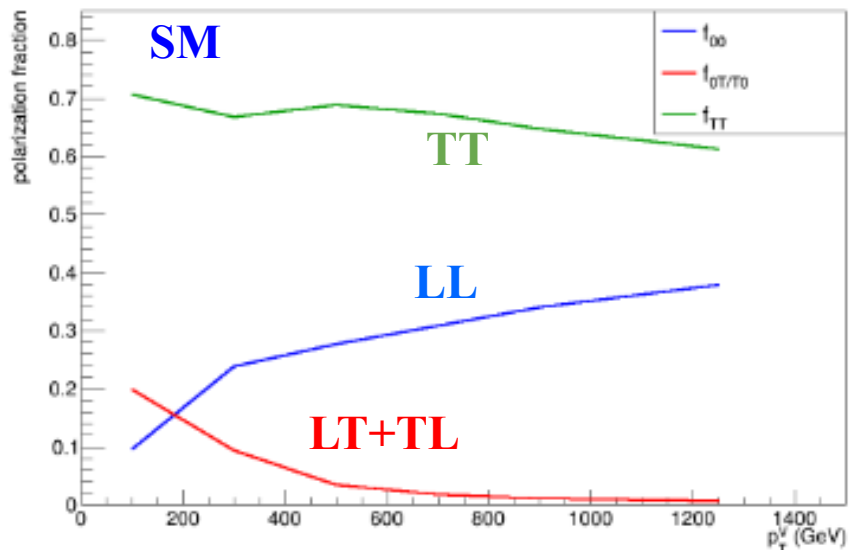
- $pp \rightarrow \square ZZ$  (140 fb<sup>-1</sup>, 13 TeV)
  - Inclusive phase space (JHEP 12 (2023) 107)
- $pp \rightarrow \square WZ$  (140 fb<sup>-1</sup>, 13 TeV)
  - Inclusive phase space (PLB 843 (2023) 137895)
  - High-energy phase space and Radiation Amplitude Zero (arXiv:2402.16365, submitted to PRL)

# Sensitivity to new physics

- New physics might couple preferentially to some polarization states
- **LL events are often more sensitive to new physics**
  - High-energy behavior of amplitudes with different diboson helicity configurations:

		SM	BSM	
<b>LL</b>	$q_{L,R}\bar{q}_{L,R} \rightarrow V_L V_L(h)$	$\sim 1$	$\sim E^2/M^2$	JHEP 2018, 111 (2018) Dim-6 EFT operator
	$q_{L,R}\bar{q}_{L,R} \rightarrow V_{\pm} V_L(h)$	$\sim m_W/E$	$\sim m_W E/M^2$	
<b>TT</b>	$q_{L,R}\bar{q}_{L,R} \rightarrow V_{\pm} V_{\pm}$	$\sim m_W^2/E^2$	$\sim E^2/M^2$	1/E <sup>2</sup> dependence in SM, E <sup>2</sup> dependence with BSM
	$q_{L,R}\bar{q}_{L,R} \rightarrow V_{\pm} V_{\mp}$	$\sim 1$	$\sim 1$	

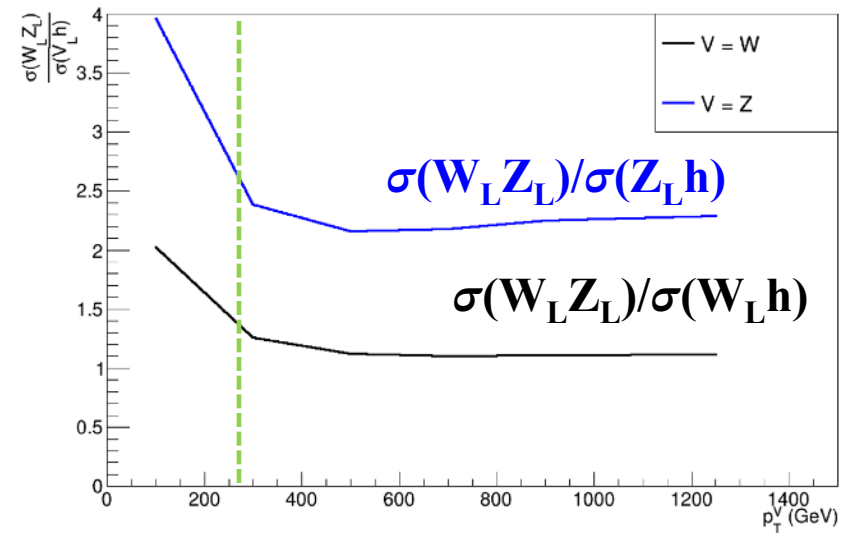
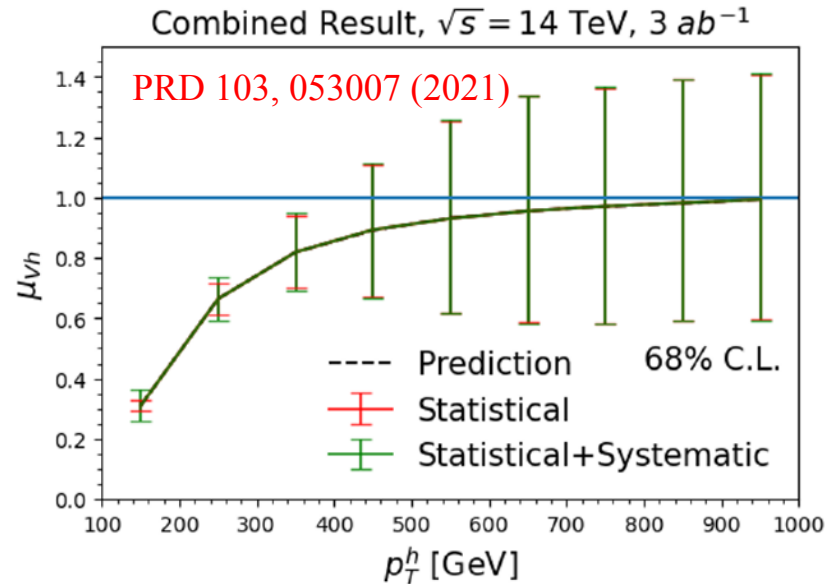
PRD 99, 055001 (2019)



Interesting to measure  $f_{LL}$  at high energies

# “Electroweak restoration” and Goldstone boson equivalence theorem

- The LHC is exploring physics at the scale electroweak symmetry is broken
- Possible to probe not only the breaking of but also the restoration of electroweak symmetry



- At high energies, SM particles are essentially massless, equivalent to the Higgs vev going to zero  $\rightarrow$  EW symmetry is restored
- Measure unfolded  $pp \rightarrow Wh$  and  $pp \rightarrow Zh$  cross sections as a function of the Higgs boson  $p_T$
- Compare to the theoretical calculation of  $pp \rightarrow G^0 h$  and derive  $\mu_{vH}$
- At high energies, the longitudinal mode of a massive vector boson is equivalent to the Goldstone boson (Goldstone boson equivalence theorem)
- $\sigma(W_L Z_L)/\sigma(W_L h) \rightarrow 1$  and  $\sigma(W_L Z_L)/\sigma(Z_L h) \rightarrow 2$
- EW symmetry restoration  $\leftrightarrow$  convergence of the Goldstone boson equivalence theorem
- Interesting to measure  $\sigma(W_L Z_L)$ ,  $\sigma(W_L h)$ ,  $\sigma(Z_L h)$ , and their ratios at high energies

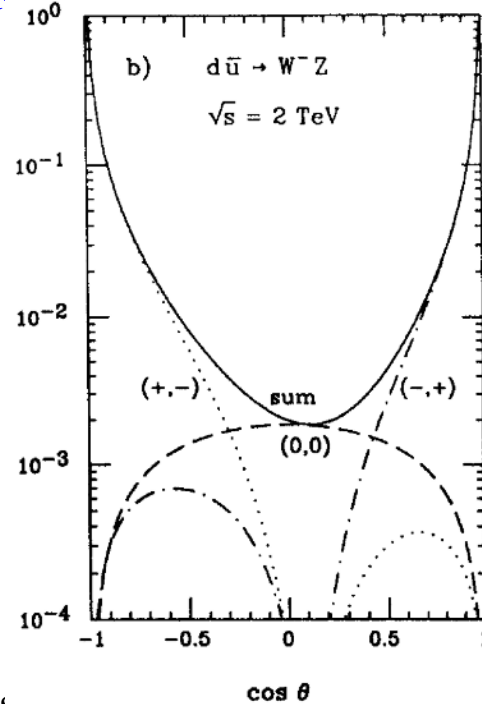
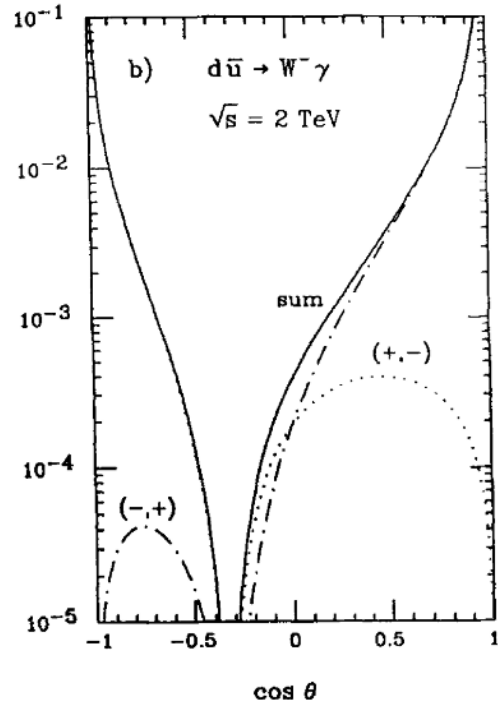
# Radiation amplitude zero

- RAZ: due to destructive interferences between different Feynman diagrams, the production cross section is exactly 0 at LO for the following angles:

- $f_1 \bar{f}_2 \rightarrow W\gamma$ :  $\cos \theta = \frac{Q_1 + Q_2}{Q_1 - Q_2}$  (PRL 43, 746 (1979))

- $f_1 \bar{f}_2 \rightarrow WZ$ :  $\cos \theta_0 = \frac{\alpha}{\beta} \left( \frac{g_-^{f_1} + g_-^{f_2}}{g_-^{f_1} - g_-^{f_2}} \right)$  (PRL 72, 3941 (1994)) for  $M (\pm, \mp)$

where only  $t$ - and  $u$ -channels contribute



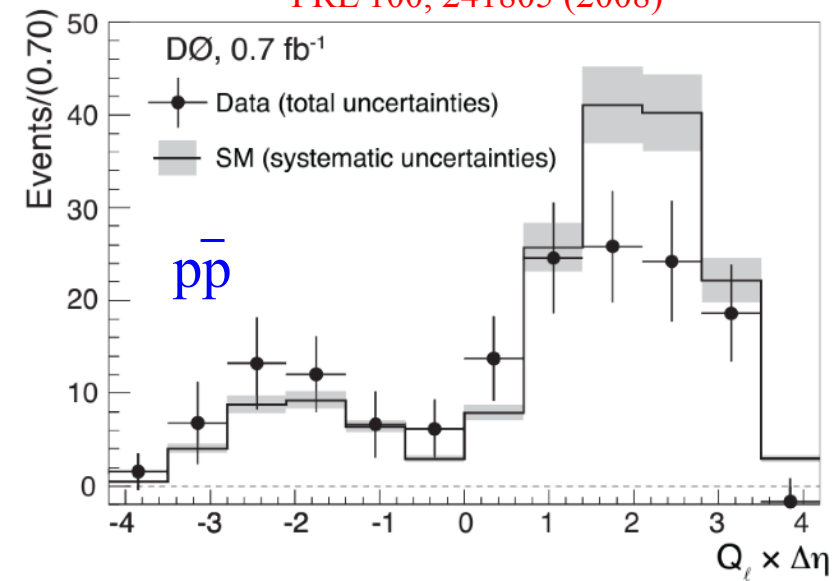
PRL 72 (1994) 3941

$\theta$  is the angle between the W boson and the incident fermion (d)

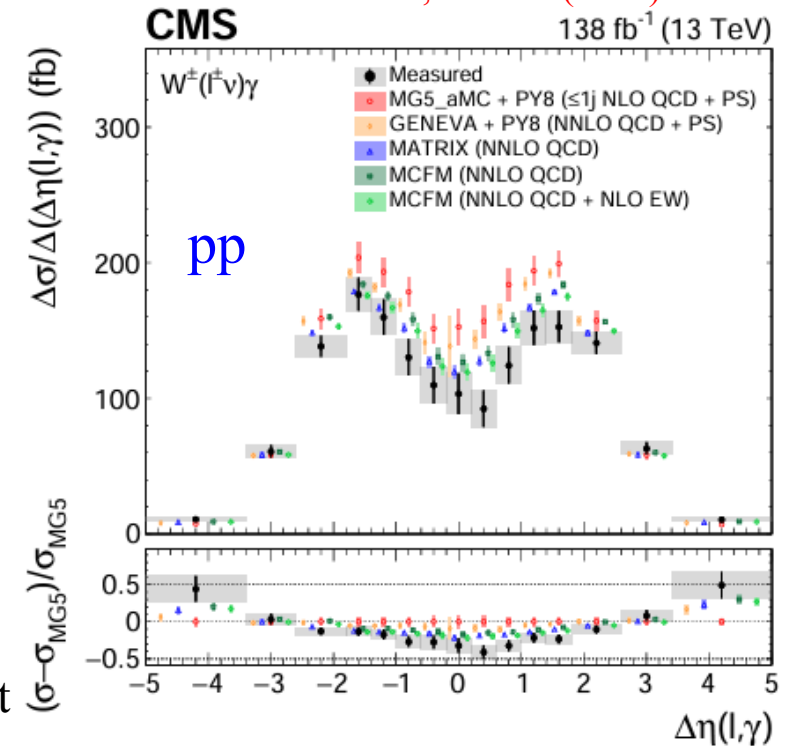
- RAZ effects have been observed experimentally for  $W\gamma$  by D0 and CMS
- Hard to observe this effect in  $WZ$  production, need to select TT events
- Higher-order corrections and non-SM couplings would eliminate the RAZ effect

PRL 100, 241805 (2008)

8



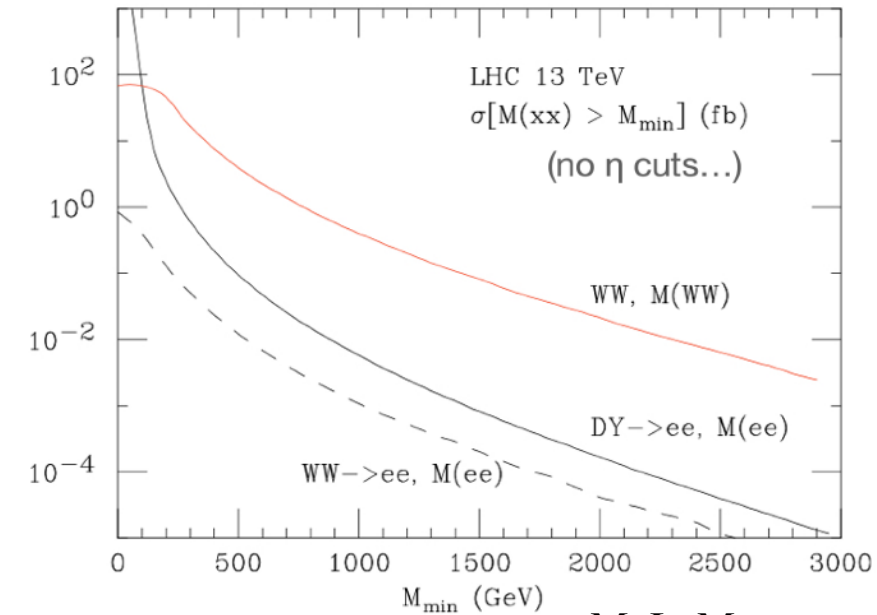
PRD 105, 052003 (2022)





# Energy vs accuracy

- Diboson processes are in general important processes to study at LHC
  - Clean final states
  - Relatively large cross sections at high energies
  - Precise measurements to test SM predictions and higher-order corrections
  - Higgs measurements with  $H \rightarrow WW^*$ ,  $H \rightarrow ZZ^*$ ,  $H \rightarrow \gamma\gamma$ ,  $H \rightarrow Z\gamma$
  - Sensitive to new physics (aTGC, resonances, ...)
    - LEP: a precision of 0.1% at 100 GeV can set a new physics scale of  $\Lambda^2 = 10 \text{ TeV}^2$
  
- LHC: to set the same new energy scale, only need to have a precision of 10% at 1 TeV

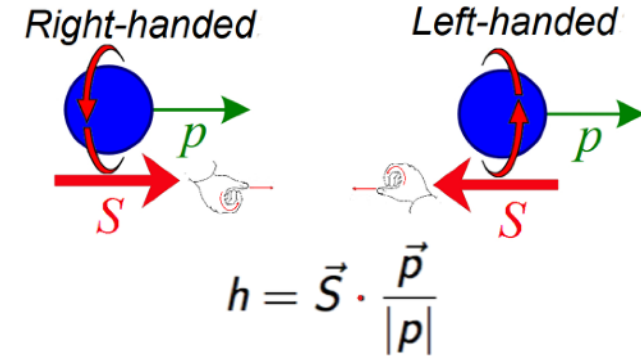


M. L. Mangano

# How to measure the polarization of a weak boson

## Polarization of a particle:

- Polarization describes the alignment of a particle's spin with its momentum. Quantified using the helicity variable:
  - Transversal polarization (T or  $\pm$ ): the spin and momentum are (anti-)aligned ( $h=1, -1$ )
  - Longitudinal polarization (L or 0): spin in parallel with the momentum ( $h=0$ )

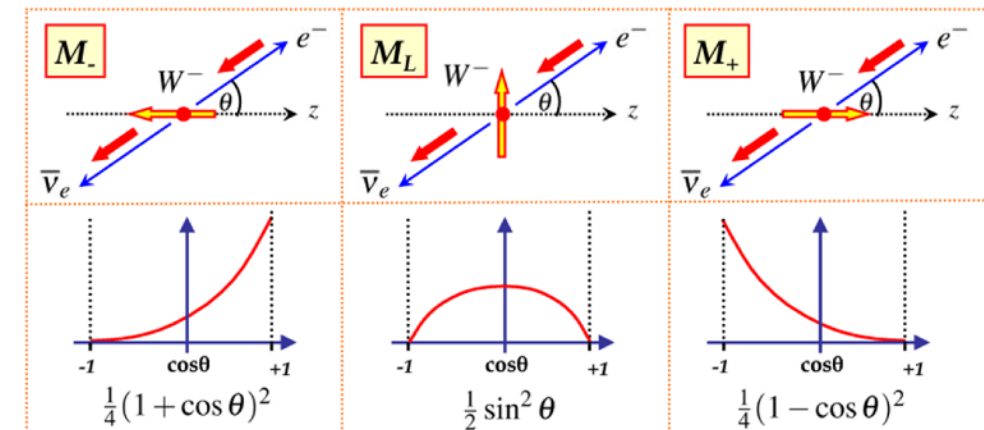


## A caveat:

- Polarization measurements are frame dependent
- For all measurements we need to define a frame (there is not an universally preferred frame)

## How to measure the polarizations of the weak bosons?

- **Weak bosons are their own polarimeters**
- Parity violation in weak interactions  $\rightarrow$  polarization has effects on the decay products
- Angular variables between the bosons and the decay products are typically used to measure the weak boson polarizations
- Perform fits to data distributions using **polarized templates**



Left-handed

Longitudinal

Right-handed

# Polarized samples

## Monte Carlo generators (LO QCD calculations so far)

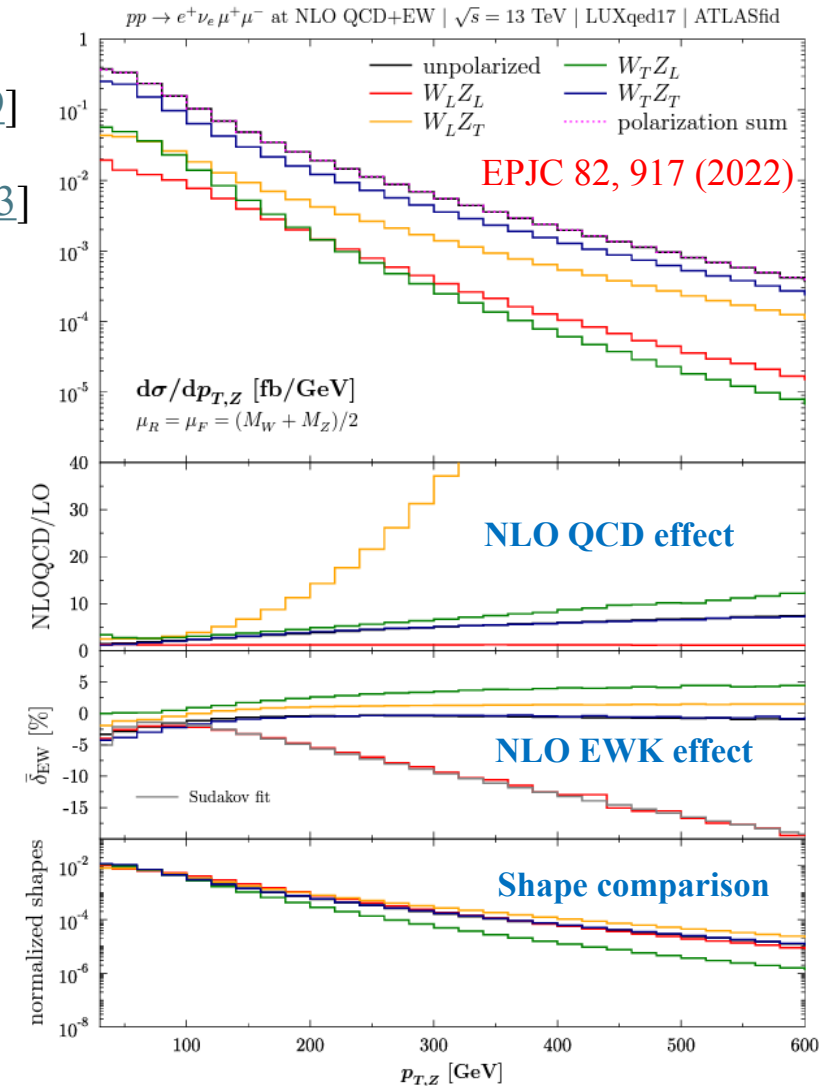
- PHANTOM:  $2 \rightarrow \square$  6 processes @LO+PS [Ballestrero et al. 2008]
- MadGraph: arbitrary processes @ LO, PS matching, multi-jet merging (Franzosi et al. 2019)
- POWHEG-Box-RES: diboson processes @NLO QCD+PS [Pelliccioli et al. 2023]
- Sherpa: arbitrary processes @nLO QCD, PS matching, multi-jet merging [Hoppe et al. 2023]
- MadGraph has been the one used by ATLAS to generate polarized samples

## Fixed order calculations

- The interference effect is often on the order of a few percent
- Large NLO QCD and electroweak corrections:
  - QCD corrections: 1.3 – 2.7 depending on polarization states and the frame used
  - EW corrections: often negative and its magnitude increasing with energy due to the double and single-Sudakov logarithms in the virtual contribution
- No MC event generation

## Getting polarized templates is a challenge

- **Reweighting technique** and/or **MC generators** are used to include higher-order effects and to estimate systematic uncertainties



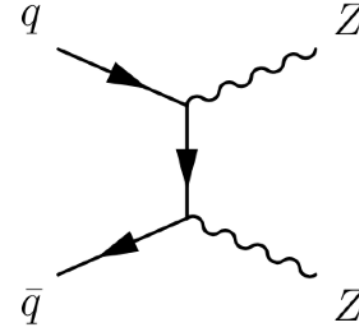
**Inclusive ZZ polarization measurement**  
**JHEP 12 (2023) 107**

# Event selection

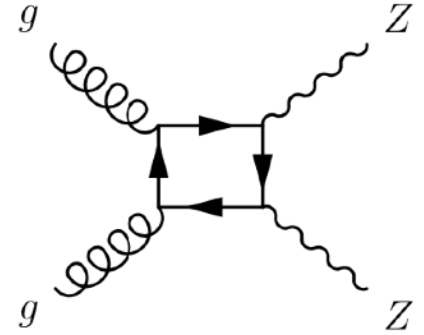
- Four isolated charged leptons with two SFOS lepton pairs consistent with the decay of a Z boson, and  $m_{4l} > 180$  GeV

Category	Requirement
Event Preselection	Fire at least one lepton trigger $\geq 1$ vertex with 2 or more tracks
Four-lepton signature	At least 4 leptons ( $e, \mu$ )
Lepton kinematics	$p_T > 20$ GeV for leading two leptons
Lepton separation	$\Delta R_{ij} > 0.05$ for any two leptons
$J/\psi$ -Veto	$m_{ij} > 5$ GeV for all SFOS pairs
Trigger matching	Baseline leptons matched to at least one lepton trigger
Quadruplet formation	At least one quadruplet with 2 Same-Flavor, Opposite-Sign (SFOS) pairs (the quadruplet having the smallest $ m_{Z_1} - m_{Z_{pole}}  +  m_{Z_2} - m_{Z_{pole}} $ is chosen)
On-shell ZZ pair	$m_{4l} > 180$ GeV
On-shell Z boson	$ m_{ij} - m_Z  < 10$ GeV

qq-initiated



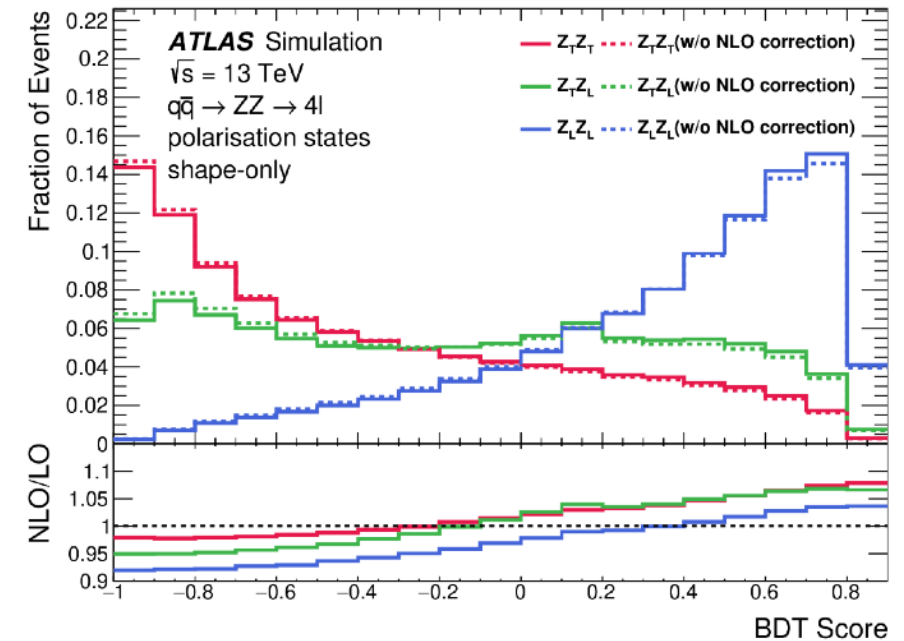
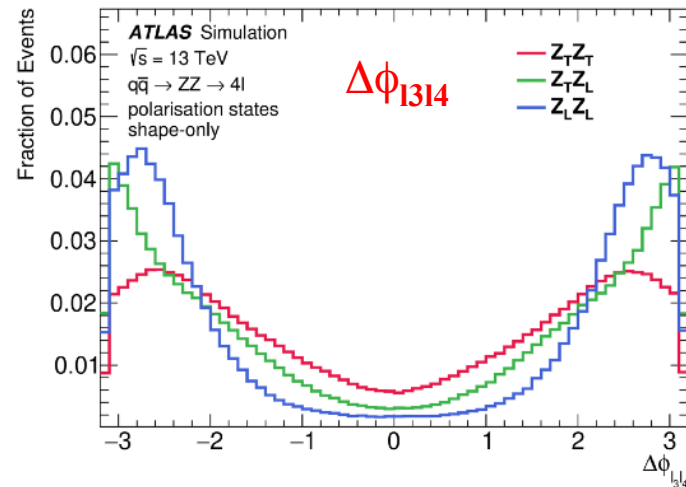
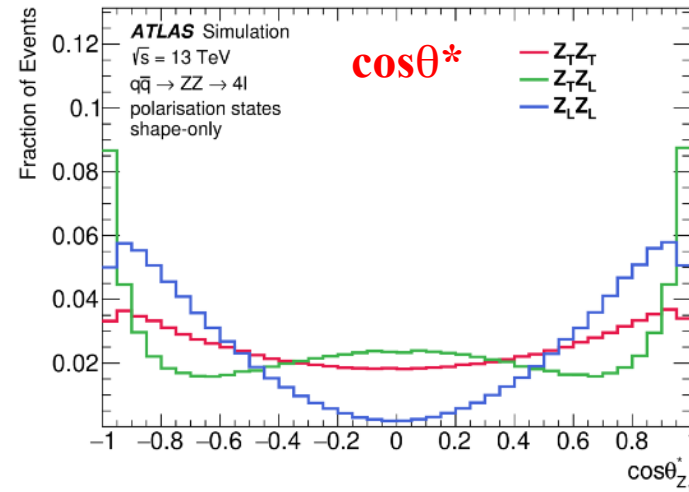
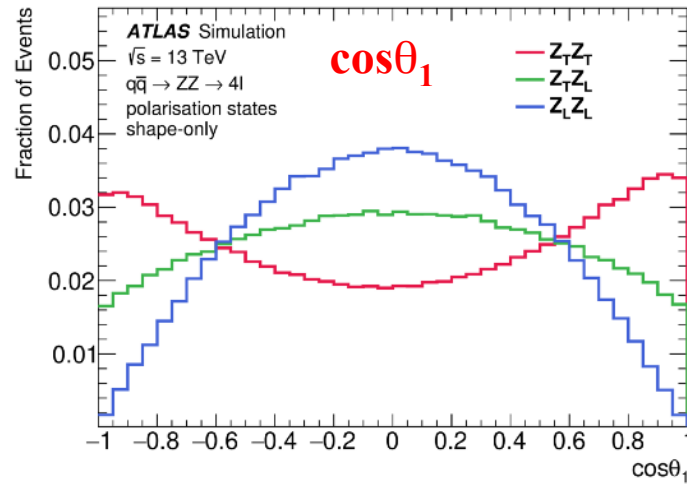
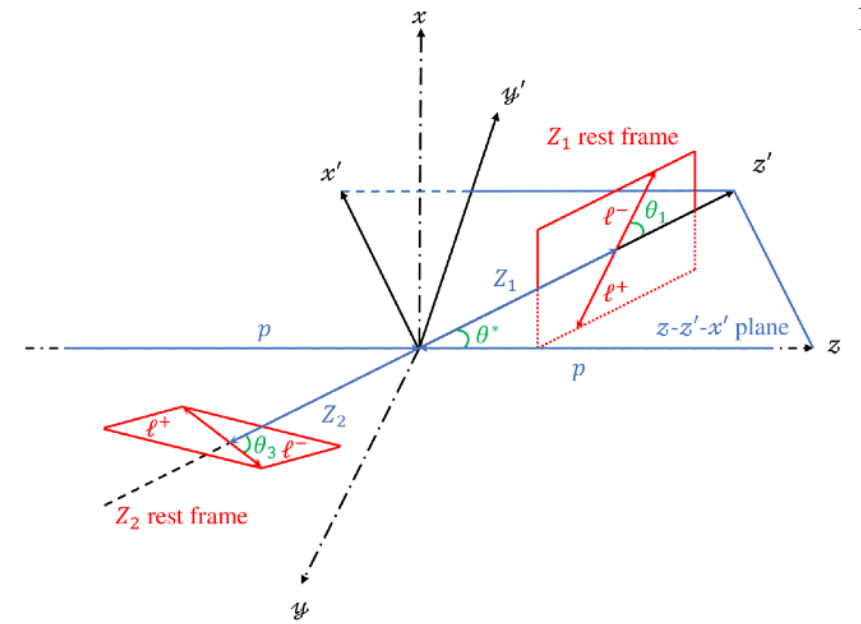
gg-initiated



ZZ	$Z_L Z_L$	189.3	$\pm$ 8.7	<b>~6%</b>
	$Z_T Z_L$	710	$\pm$ 29	<b>~23%</b>
	$Z_T Z_T$	2170	$\pm$ 120	<b>~70%</b>
	Interference	33.7	$\pm$ 2.8	<b>~1%</b>
Non-prompt		18.7	$\pm$ 7.1	
Others		20.0	$\pm$ 3.7	
Total		3140	$\pm$ 150	
Data		3149		

# Variables used for polarization measurements

- The ZZ rest frame is used
- Five angular variables ( $\cos\theta_1$ ,  $\cos\theta_3$ ,  $\cos\theta^*_{Z1}$ ,  $\Delta\phi_{1112}$ , and  $\Delta\phi_{1314}$ ) are used to train a BDT variable to separate  $Z_L Z_L$  from  $Z_T Z_X$



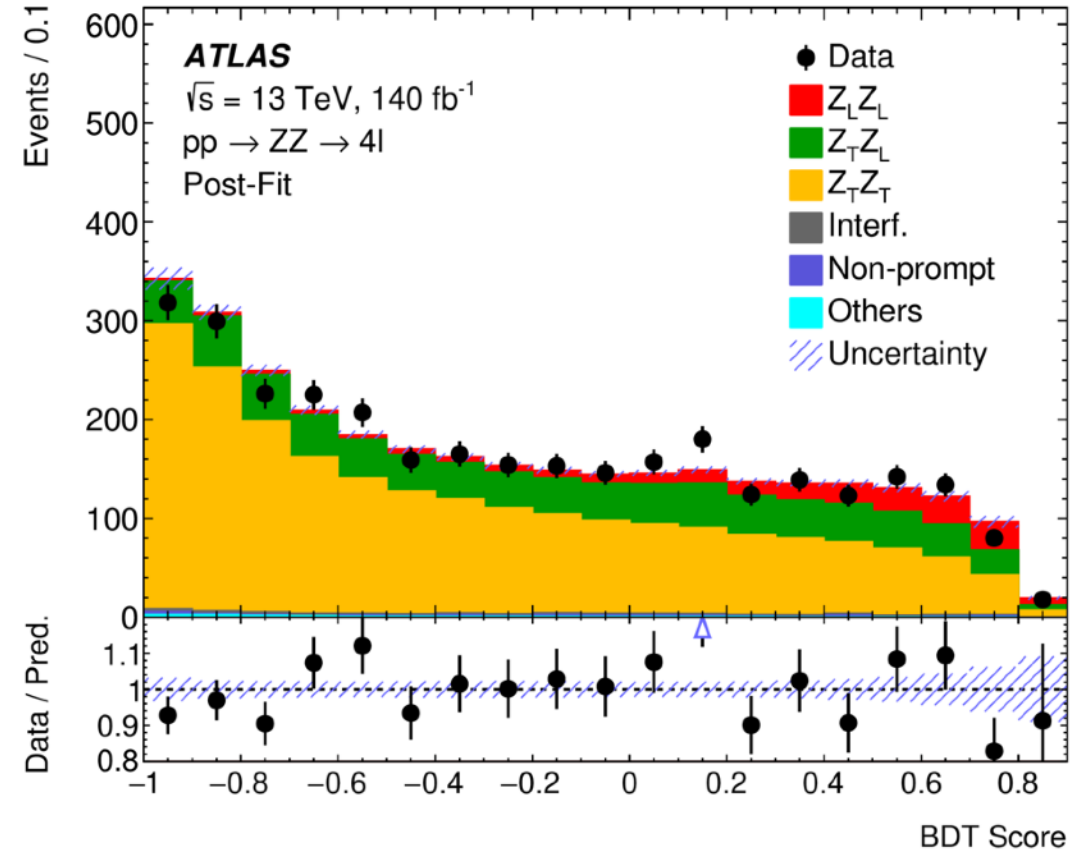
# Template fitting

## Template challenges:

- Polarized templates available with MadGraph for qq-initiated and EW ZZjj but not for gg-initiated diagrams
- NLO EW+QCD corrections and the gg-initiated contributions are available for ZZ at particle level with MoCaNLO (arXiv:2107.06579)
- A reweighting method using 1D and 2D distributions to:
  - Incorporate NLO EQ+QCD corrections to the MadGraph simulation for each polarization state
  - Obtain polarized templates from the unpolarized Sherpa gg-initiated MC sample
  - Include the interference effects among different polarization states

## Fitting for joint polarization fractions:

- Fitted using two parameters:  $\mu_{LL}$  and  $\mu_{TX}$
- Obs. significance on  $\mu_{LL}$  at  $4.3\sigma$  ( $3.8\sigma$  expected)  $\rightarrow$  First evidence of  $Z_L Z_L$  production
- $Z_L Z_L$  cross section measured to be  $2.45 \pm 0.56(\text{stat}) \pm 0.21(\text{syst})$  fb, consistent with the prediction of  $2.10 \pm 0.09$  fb



**Inclusive WZ polarization measurement**  
**PLB 843 (2023) 137895**

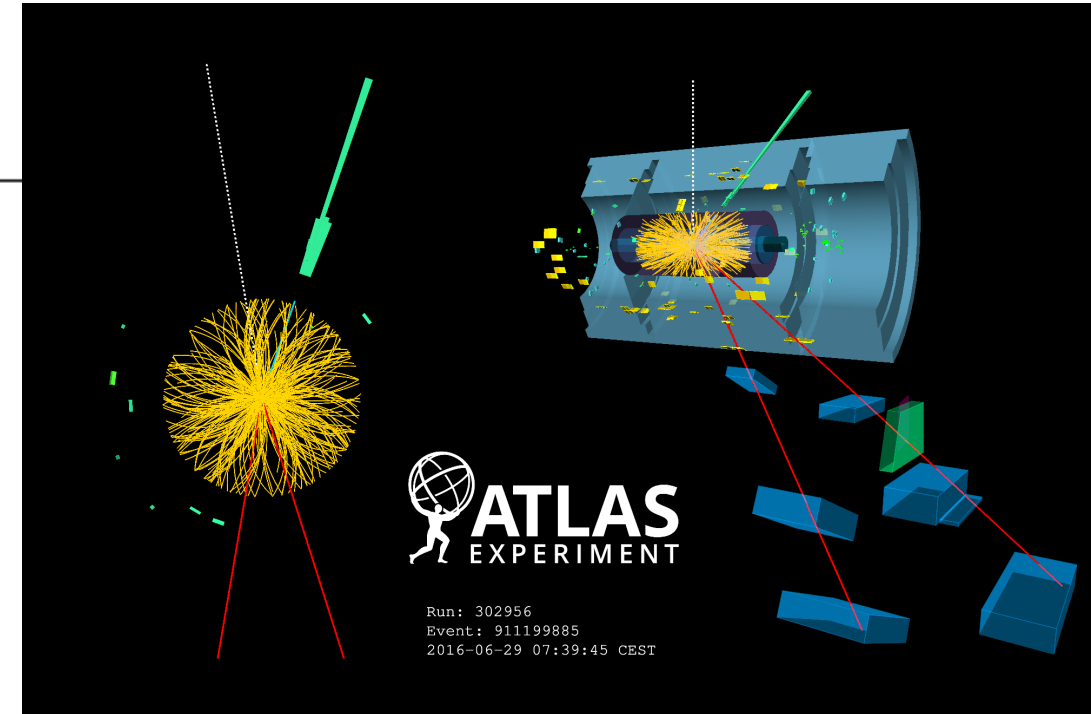
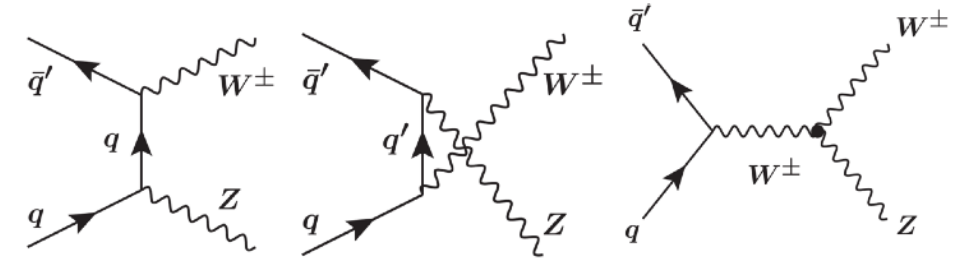


# Event selection

- Three isolated charged leptons with an SFOS lepton pair consistent with the decay of a Z boson

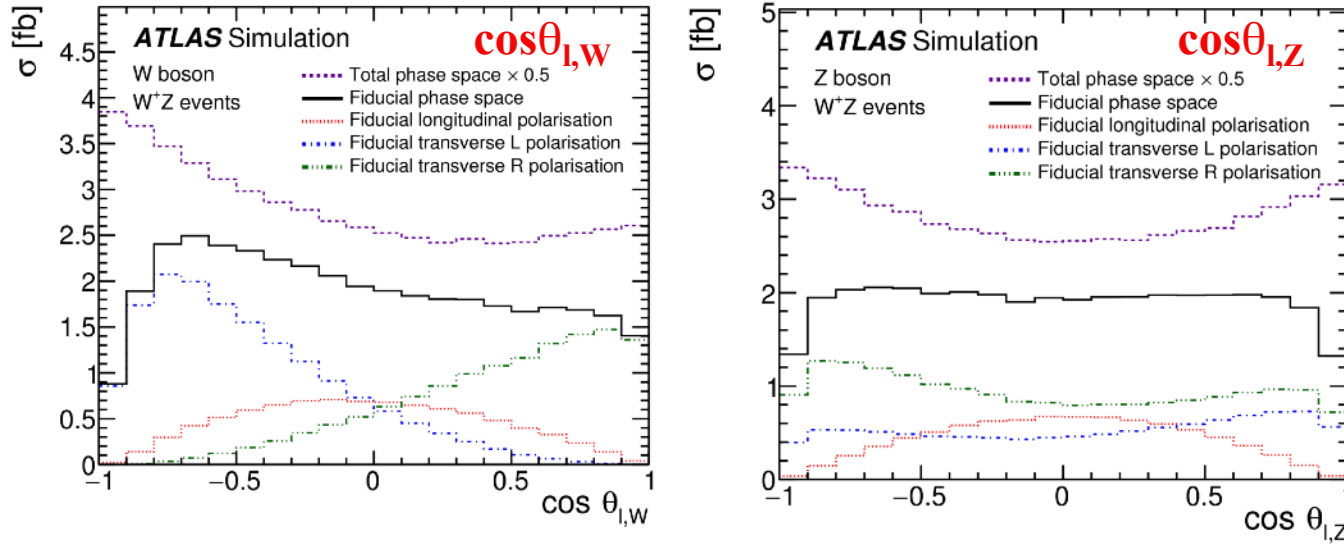
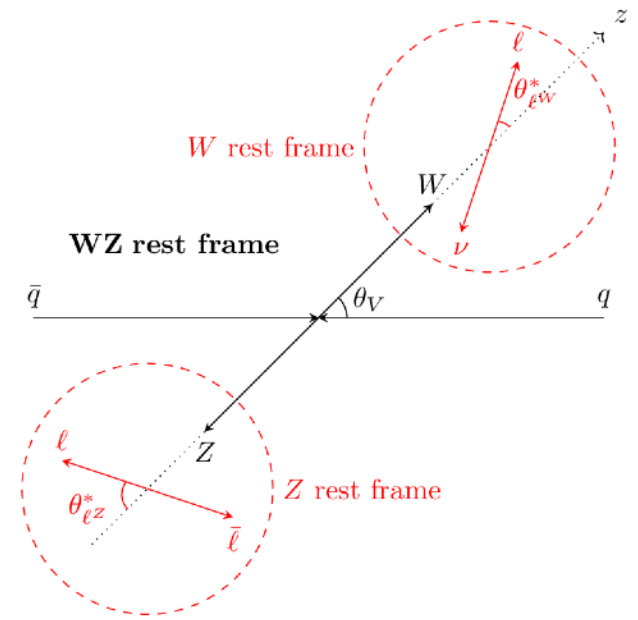
Trigger	At least one of five single lepton triggers fired
Leading lepton $p_T$	$p_T^{\text{lead}} > 27 \text{ GeV}$
Event cleaning	Reject corrupted or incomplete events and events with non-collision background jet
Primary vertex	Hard scattering vertex with at least two tracks
ZZ veto	Strictly less than 4 baseline leptons
$N$ leptons	Exactly 3 leptons passing the Z-lepton selection
Z leptons	2 same flavor oppositely charged leptons passing Z-lepton selection
Mass window	$ m_{\ell\ell} - M_Z  < 10 \text{ GeV}$
W lepton	Remaining lepton passes W-lepton selection
W transverse mass	$m_T^W > 30 \text{ GeV}$

WZ in $\tau$	620 $\pm$ 60	
ZZ	1420 $\pm$ 120	~10%
$t\bar{t} + V$	870 $\pm$ 130	
Misid. leptons	1170 $\pm$ 230	~5%
Others	800 $\pm$ 90	
$W_0Z_0$	920 $\pm$ 40	~6%
$W_0Z_T$	2670 $\pm$ 50	~32%
$W_TZ_0$	2670 $\pm$ 60	
$W_TZ_T$	10200 $\pm$ 230	~62%
Total MC	21400 $\pm$ 500	
Data	21936	

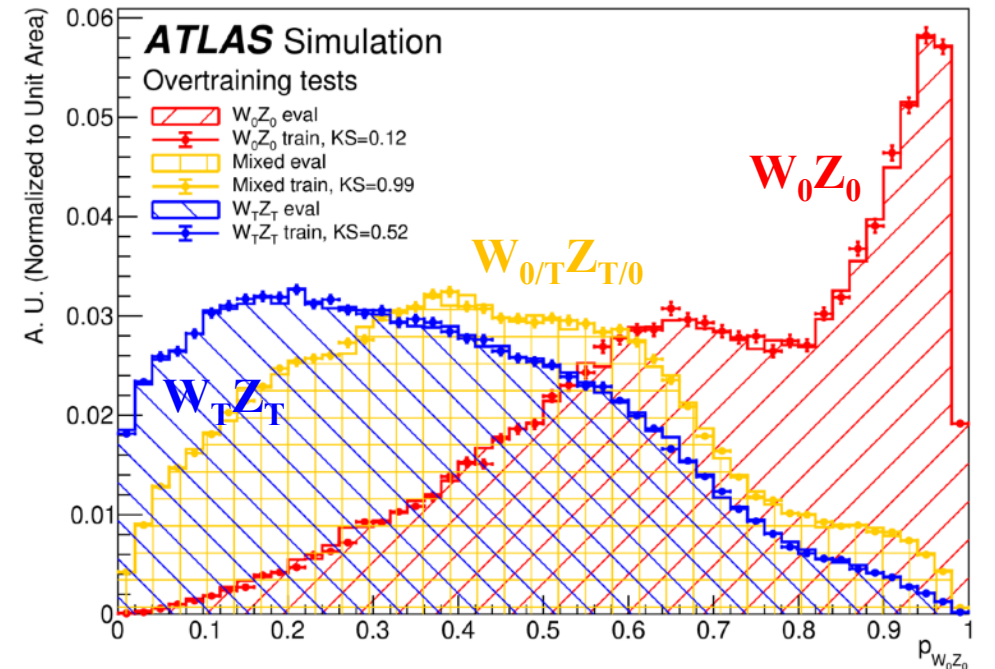
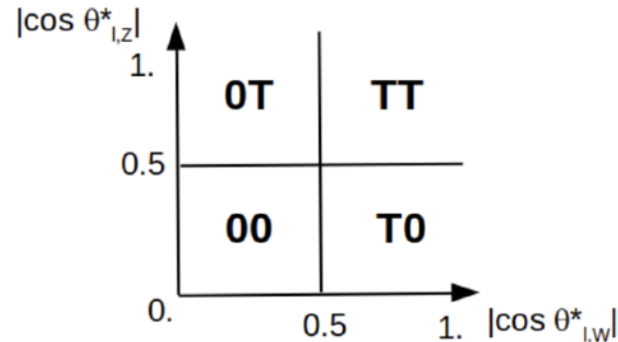


# Discriminating variables used

- The WZ rest frame is used
- A DNN score variable trained with eight kinematic variables ( $\Delta Y_{lZ}$ ,  $\Delta\phi(l_W, l_\nu)$ ,  $\Delta\phi(l^1_Z, l^2_Z)$ ,  $p_T^{WZ}$ , W lepton  $p_T$ , two Z lepton  $p_T$ , and MET)
- The DNN score is trained separately in each of the four categories based on  $|\cos\theta_{l,W}|$  and  $|\cos\theta_{l,Z}|$



**Blue: left-handed**  
**Green: right-handed**  
**Red: longitudinal**



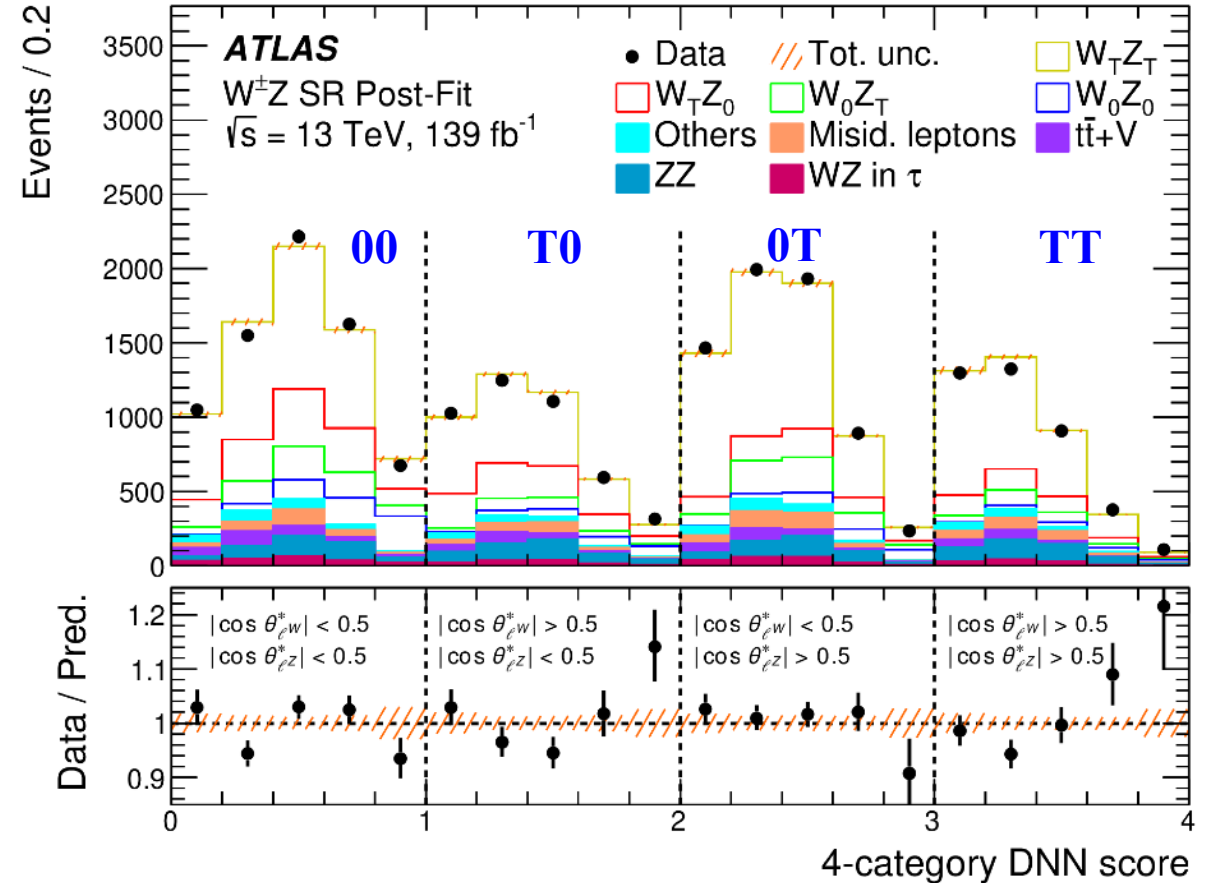
# Templates and fitting

## Template challenges:

- Polarized templates available with MadGraph at LO+real corrections  $\rightarrow$   $\square$  great, but insufficient, bias from 10% to 50% of the fraction values in this phase space
- Polarized templates at NLO QCD are obtained using a multi-dimensional reweighting technique with a classification DNN output [arXiv:1907.08209]:
  - For a given event  $x$  (12 selected kinematic variables describing the event), figure out the probabilities for it to be in 00, 0T, T0, and TT states using LO polarized MadGraph samples
  - These probabilities are then applied as weights to NLO unpolarized POWHEG samples

## Fitting for joint polarization fractions:

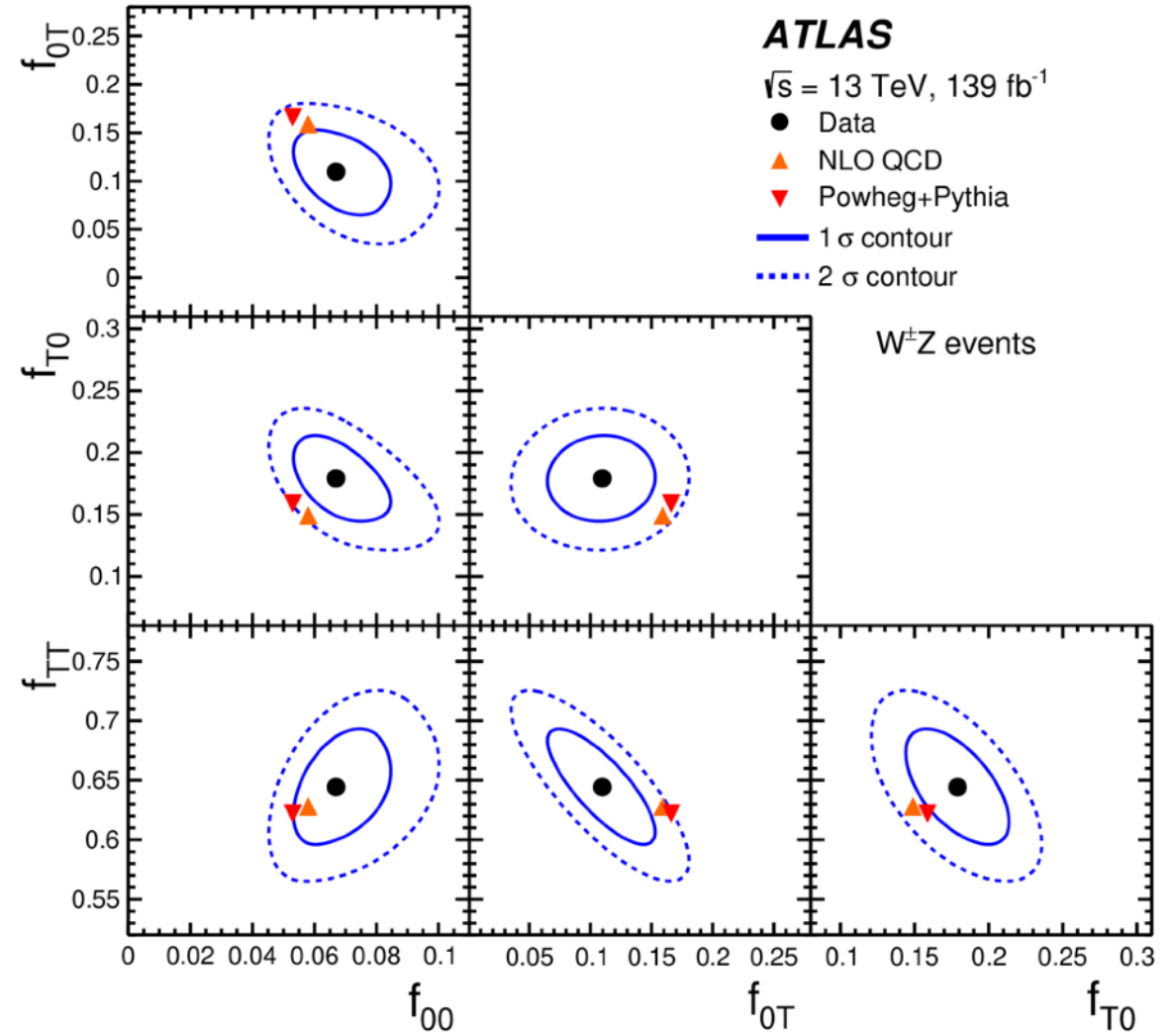
- Four different polarization fractions ( $f_{00}$ ,  $f_{0T}$ ,  $f_{T0}$ , and  $f_{TT}$ ) to extract
- DNN score classifies each joint polarization state
- Simultaneous fit performed in 4 categories based on  $|\cos\theta_{1,W}|$  and  $|\cos\theta_{1,Z}|$



# Fitted results

	Data	POWHEG+PYTHIA	NLO QCD
$W^\pm Z$			
$f_{00}$	$0.067 \pm 0.010$	$0.0590 \pm 0.0009$	$0.058 \pm 0.002$
$f_{0T}$	$0.110 \pm 0.029$	$0.1515 \pm 0.0017$	$0.159 \pm 0.003$
$f_{T0}$	$0.179 \pm 0.023$	$0.1465 \pm 0.0017$	$0.149 \pm 0.003$
$f_{TT}$	$0.644 \pm 0.032$	$0.6431 \pm 0.0021$	$0.628 \pm 0.004$

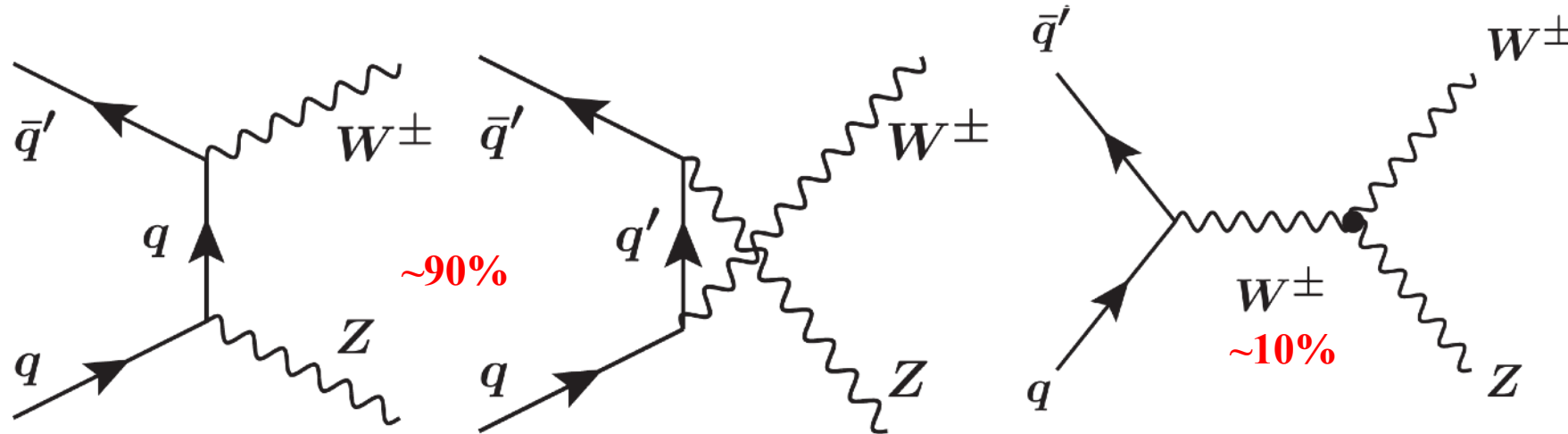
- Stat and syst uncertainties are comparable
- Dominant systematic uncertainty comes from modeling
- Obs. significance on  $f_{00}$  at  $7.1\sigma$  ( $6.2\sigma$  expected)
- Obs. significance on  $f_{0T}$  ( $3.4\sigma$ ),  $f_{T0}$  ( $7.1\sigma$ ) and  $f_{TT}$  ( $11\sigma$ )
- First observation/evidence of WZ in different polarizations
- Joint polarization fractions are also measured for  $W^+Z$  and  $W^-Z$  processes separately
- Individual boson helicity fractions are also measured
- The measured values agree with the SM predictions and the multiplications are consistent with the measured joint helicity fractions when neglecting interference among polarization states ( $f_{00} \approx f_0^W \times f_0^Z$ )



**High- $p_T$  WZ polarization measurement and  
Radiation Amplitude Zero  
arXiv:2402.16365**

# Introduction

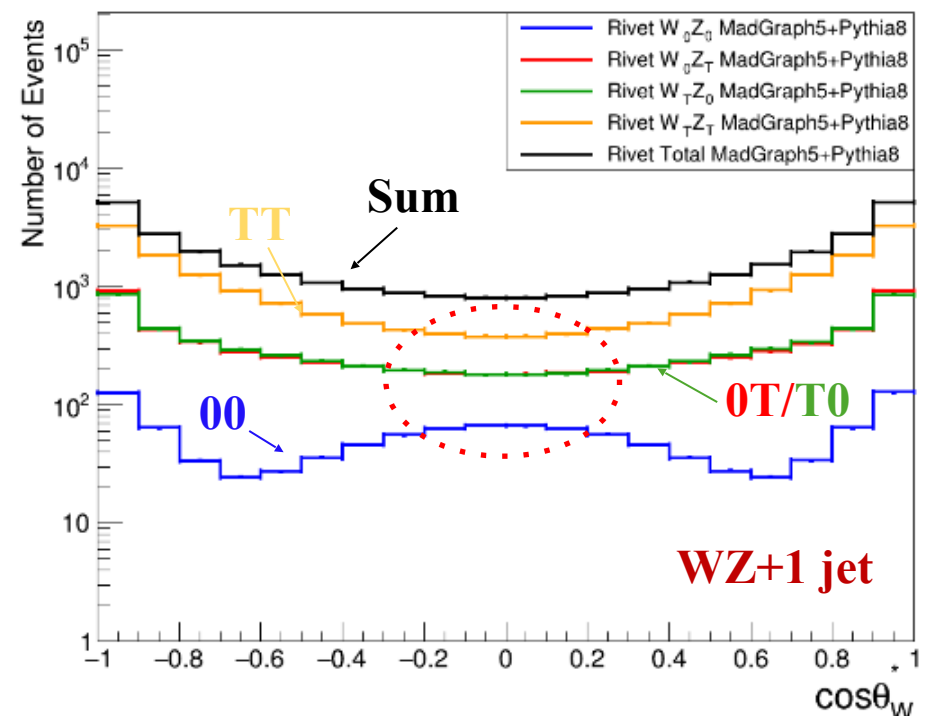
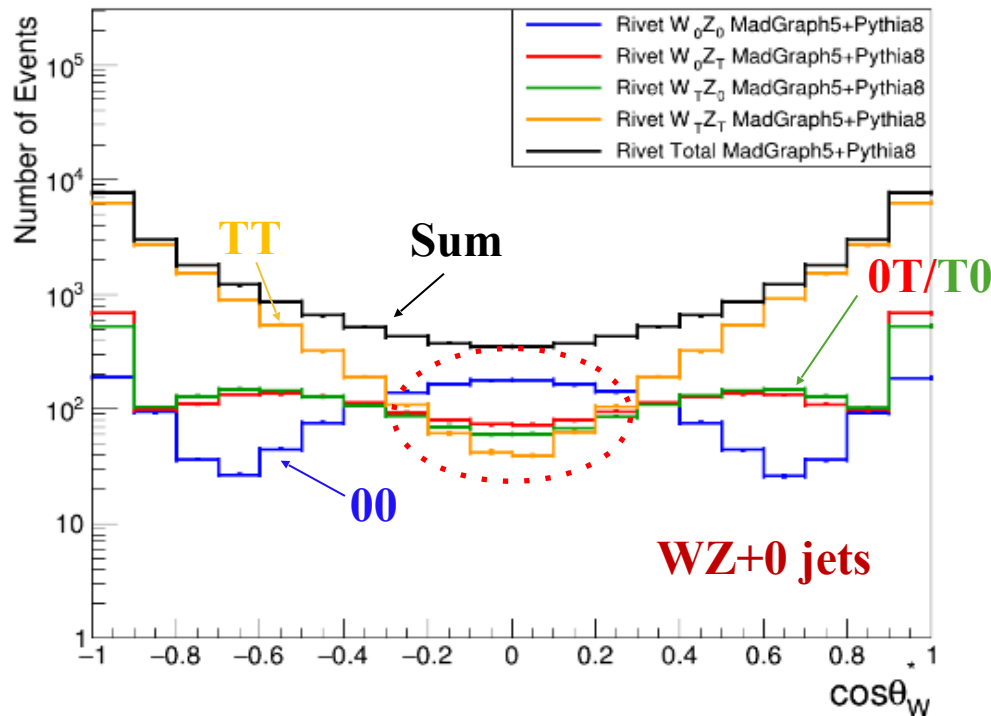
- Inclusive WZ and ZZ polarization measurements are dominated by t- and u-channel production ( $f_{00} \approx f_0^W \times f_0^Z$ )
- Interesting measurements with:
  - Events **produced in the s-channel** where two longitudinally-polarized vector bosons interacting with each other
  - Cross-section/fraction measurements for different polarization states **at high energies**



- Challenges:
  - Only  $\sim 10\%$  of events produced in the s-channel
  - Both bosons are longitudinally polarized is  $\sim 6\% \rightarrow 10\% \times 6\% = 0.6\%$
  - The signal size is  $\sim 0.6\%$  of inclusive diboson production

# Reasons to choose the $WZ \rightarrow \ell \nu \ell \ell$ channel

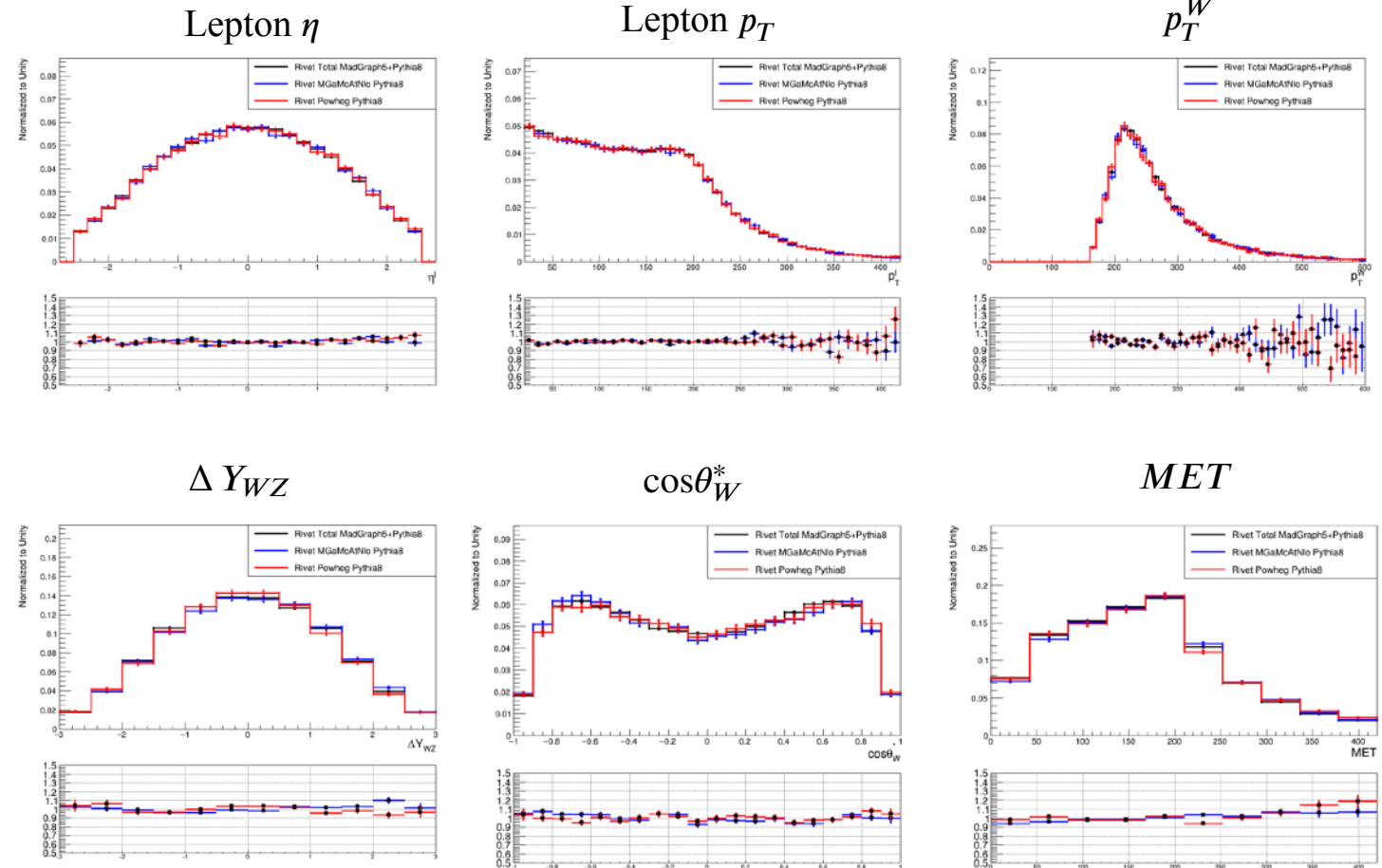
- Experimental side: large cross sections, most kinematical variables can be calculated (neutrino  $p_z$  calculated using the  $W$  mass constraint), small reducible background expected
- Theoretical side: Radiation Amplitude Zero
  - At LO expect to have exact zero for  $\sigma(W_T Z_T)$  in the region with the boson scattering angle  $\cos\theta_W \sim 0$
  - Strong gauge cancellations for the  $0T$  and  $T0$  amplitudes
  - This results in a lower cross section for  $TT+0T+T0$  than  $00$  for  $\cos\theta_W \sim 0$
  - RAZ effect happens only at LO



# Polarized WZ samples

- LO WZ+0 jets and WZ+1 jet events generated with MadGraph
- Pythia is used to perform parton shower and merge these two samples to emulate the NLO effect
- Separate samples generated for events with  $p_T(Z) < 150$  GeV and  $p_T(Z) > 150$  GeV to have more statistics at high  $p_T$
- Samples with  $e/\mu$  and  $\tau$  in the final state are generated separately
- Negligible interference effects
- **Sum of polarized events are compared with inclusive NLO QCD events**
- **Comparison of merged LO MadGraph predictions with NLO EWK+QCD calculations for each polarization state**
- Good agreement observed for all comparison plots

MadGraph Sum of different diboson polarizations LO + Pythia8  
 MadGraph aMC@NLO – NLO + Pythia8  
 Powheg+Pythia8





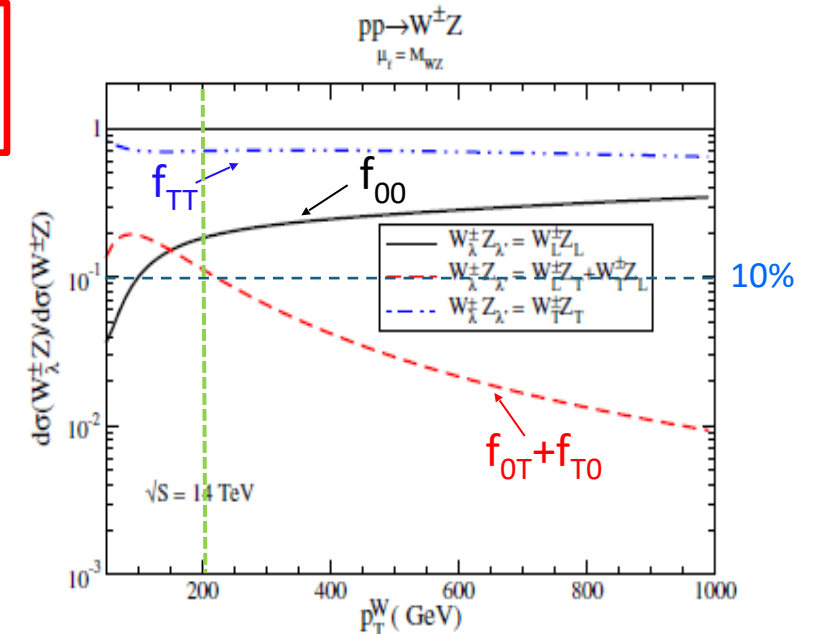
# Event selection

Inclusive WZ event selection	
Event cleaning	Reject LAr, Tile and SCT corrupted events and incomplete events
Primary vertex	Hard scattering vertex with at least two tracks
Triggers in 2015	HLT_e24_lhmedium_L1EM20VH    HLT_e60_lhmedium    HLT_e120_lhloose HLT_mu20_iloose_L1MU15    HLT_mu50
Triggers in 2016–2018	HLT_e26_lhtight_nod0_ivarloose    HLT_e60_lhmedium_nod0    HLT_e140_lhloose_nod0 HLT_mu26_ivarmedium    HLT_mu50
ZZ veto	Less than 4 baseline leptons
$N$ leptons	Exactly three leptons passing the Z lepton selection
Leading lepton $p_T$	$p_T^{\text{lead}} > 25$ GeV (in 2015) or $p_T^{\text{lead}} > 27$ GeV (in 2016-2018)
Z leptons	Two same flavor oppositely charged leptons passing the Z-lepton selection
Z lepton invariant mass	$ m_{\ell\ell} - M_Z  < 10$ GeV
W lepton	Remaining lepton passes the W-lepton selection
W transverse mass	$m_T^W > 30$ GeV
$\Delta R$	$\Delta R(\ell_Z^-, \ell_Z^+) > 0.2, \Delta R(\ell_Z, \ell_W) > 0.3$

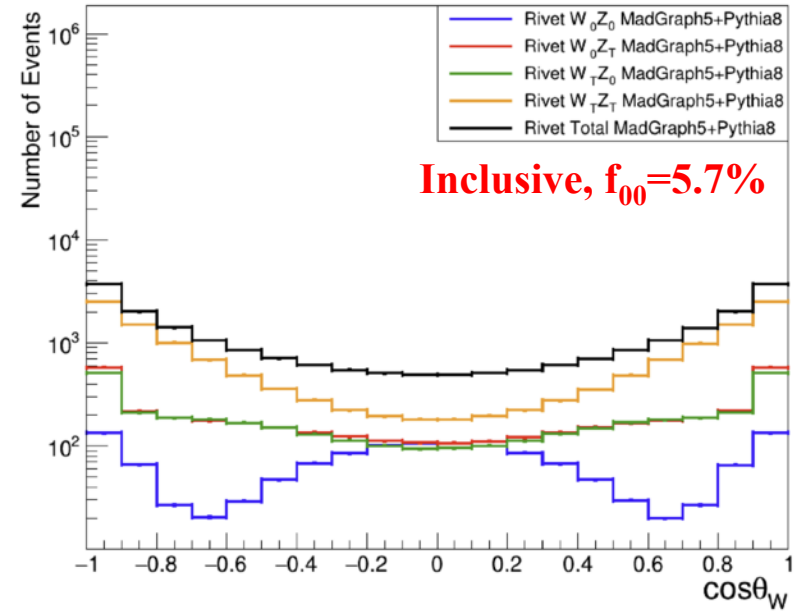
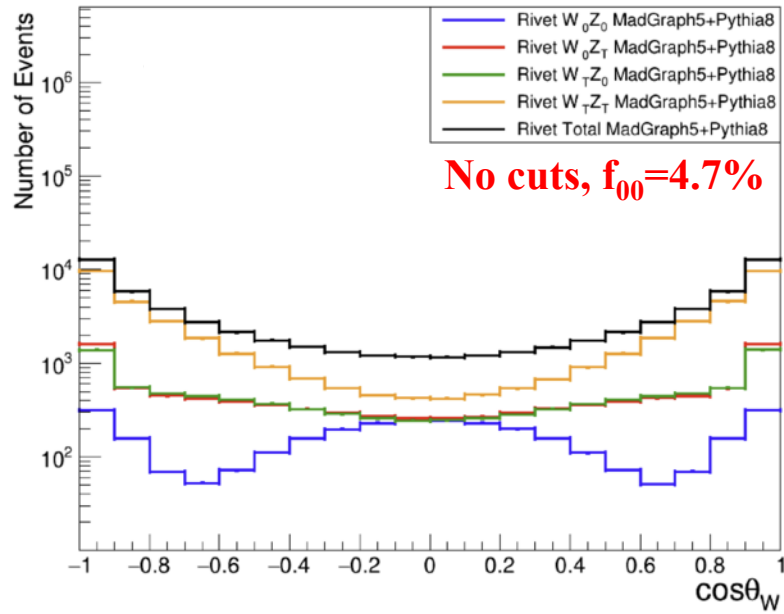
Same requirements as used by the inclusive WZ polarization measurement

	Signal regions		
	Radiation Amplitude Zero	00-enhanced region 1	00-enriched region 2
Pass inclusive WZ event selection	✓	✓	✓
Transverse momentum of the Z boson ( $p_T^Z$ )	-	[100, 200] GeV	> 200 GeV
Transverse momentum of the WZ system ( $p_T^{WZ}$ )	< 20, 40, 70 GeV		< 70 GeV

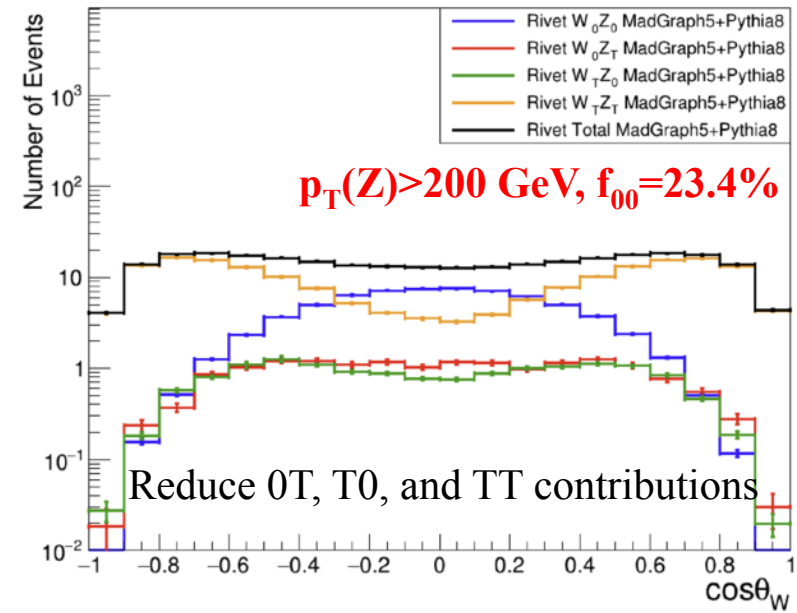
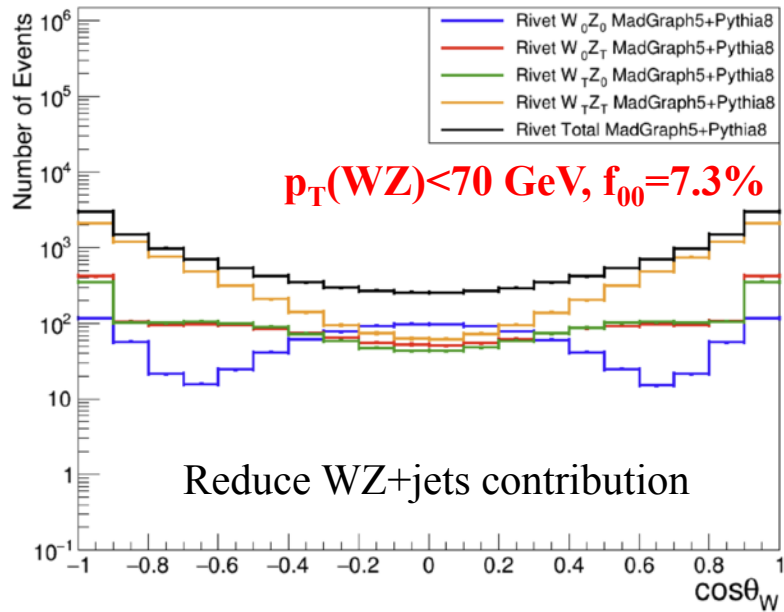
- **Inclusive:** events with three isolated leptons
- **Low- $p_T(WZ)$ :**  $p_T(WZ) < 70$  GeV to reduce WZ+jets events → increase the RAZ effect
- **High  $p_T(Z)$ :**  $100 < p_T(Z) < 200$  GeV (or  $p_T(Z) > 200$  GeV) to select s-channel events

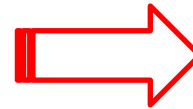
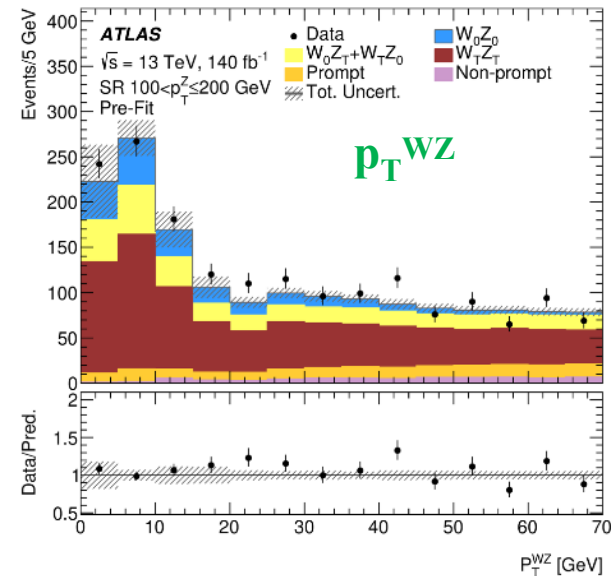
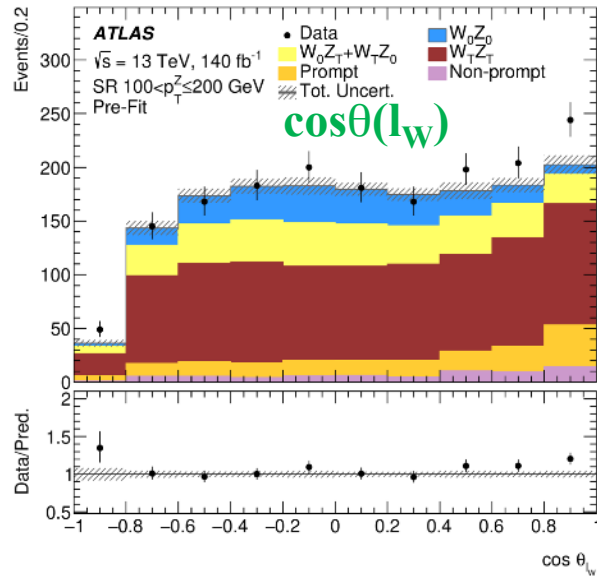
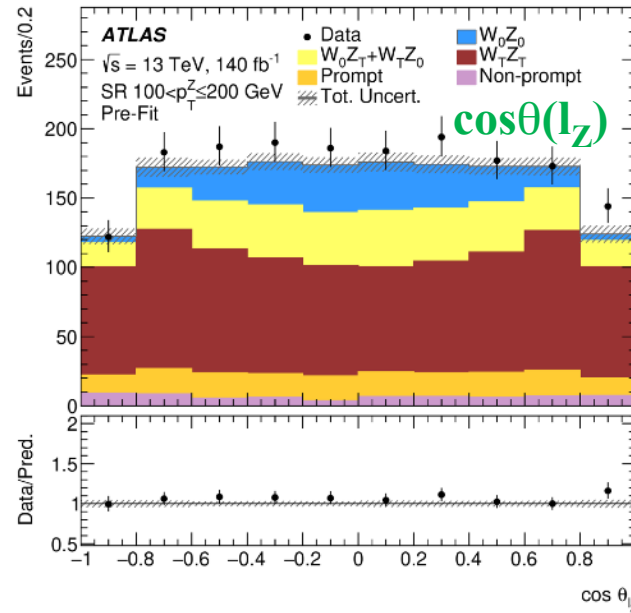
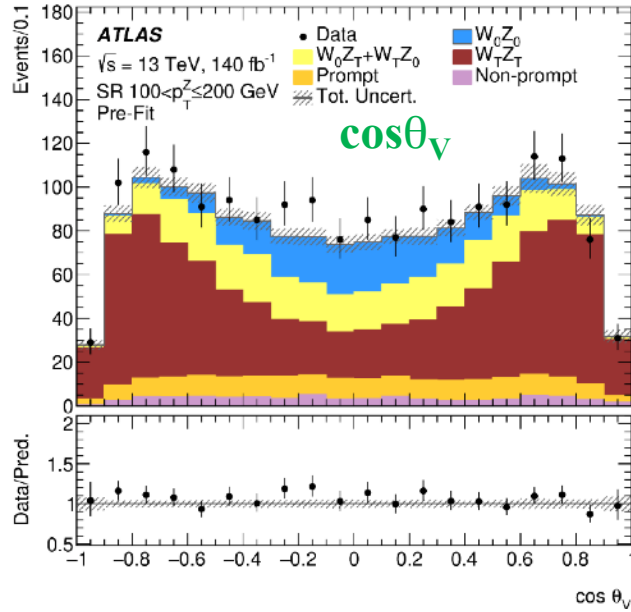


# 00-enhanced signal regions

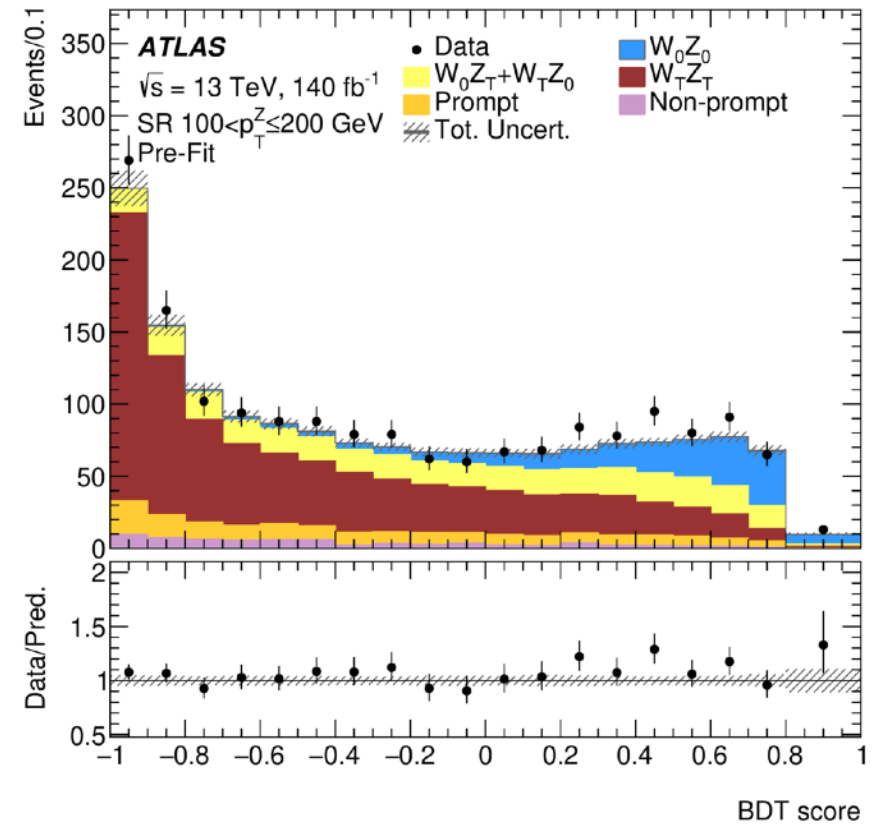


Blue: 00  
 Red: 0T  
 Green: T0  
 Orange: TT

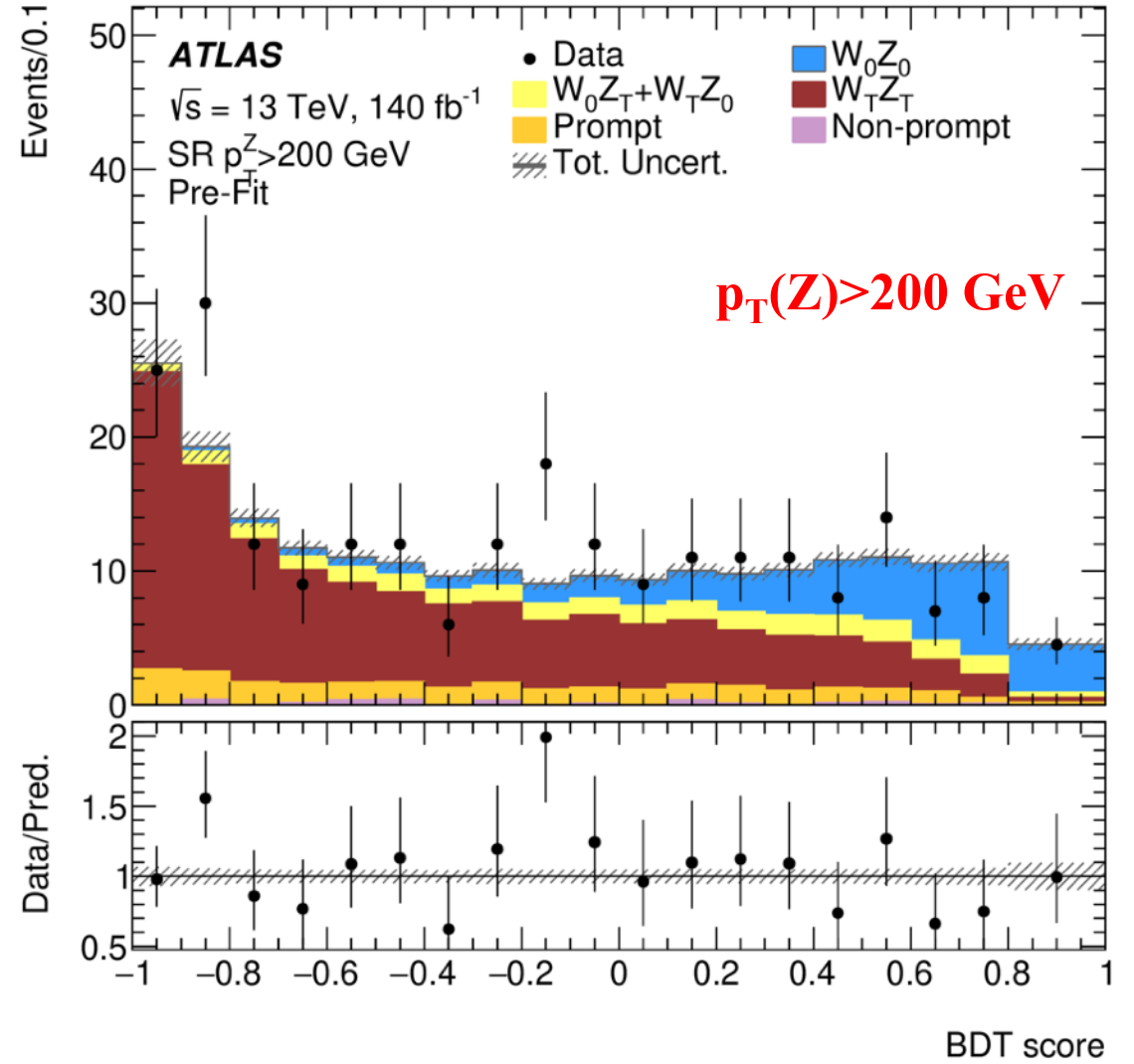
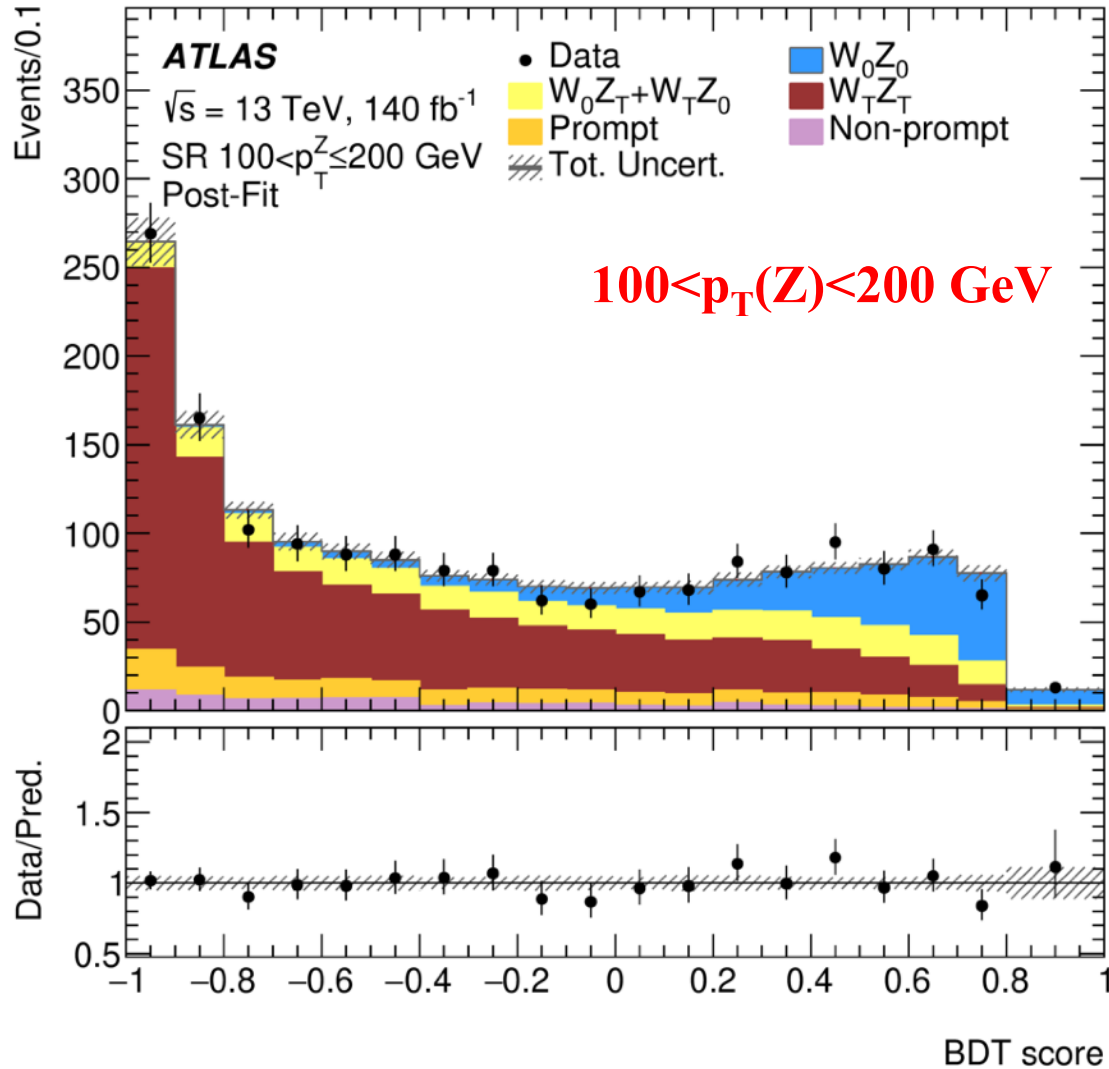




- A BDT discriminant is trained using seven kinematical variables to separate  $00$  from other polarization states
- Separate BDT variable trained for each  $00$ -enhanced signal region
- Pre-fit plots are shown



# Fitting results



# Results

Process	$100 < p_T^Z \leq 200 \text{ GeV}$		$p_T^Z > 200 \text{ GeV}$	
	Pre-fit	Post-fit	Pre-fit	Post-fit
$W_0Z_0$	$222 \pm 5$	$290 \pm 60$	$47.6 \pm 1.5$	$28 \pm 19$
$W_0Z_T + W_TZ_0$	$323 \pm 12$	$280 \pm 140$	$23.7 \pm 0.8$	$50 \pm 40$
$W_TZ_T$	$856 \pm 31$	$920 \pm 100$	$124 \pm 4$	$132 \pm 29$
Prompt background	$169 \pm 18$	$166 \pm 18$	$24.1 \pm 2.7$	$24.2 \pm 2.7$
Non-prompt background	$68 \pm 29$	$80 \pm 40$	$2.8 \pm 1.1$	$2.8 \pm 1.1$
Total Expected	$1640 \pm 60$	$1740 \pm 40$	$222 \pm 8$	$236 \pm 15$
Data	1740		236	

- First observation/evidence of joint longitudinally-polarized bosons at high energies  $\rightarrow$  approaching the regime where longitudinal bosons behave as Goldstone bosons
- These signal regions are dominated by s-channel events where two bosons directly interact with each other

## Two-parameter fit: $f_{00}$ and $N_{\text{tot}}$

	Measurement	
	$100 < p_T^Z \leq 200 \text{ GeV}$	$p_T^Z > 200 \text{ GeV}$
$f_{00}$	$0.17 \pm_{0.02}^{0.02} \text{ (stat)} \pm_{0.02}^{0.01} \text{ (syst)}$	$0.16 \pm_{0.05}^{0.05} \text{ (stat)} \pm_{0.03}^{0.02} \text{ (syst)}$
$f_{XX}$	$0.83 \pm_{0.02}^{0.02} \text{ (stat)} \pm_{0.01}^{0.02} \text{ (syst)}$	$0.84 \pm_{0.05}^{0.05} \text{ (stat)} \pm_{0.02}^{0.03} \text{ (syst)}$
$f_{00}$ obs (exp) sig.	7.7 (6.9) $\sigma$	3.2 (4.2) $\sigma$

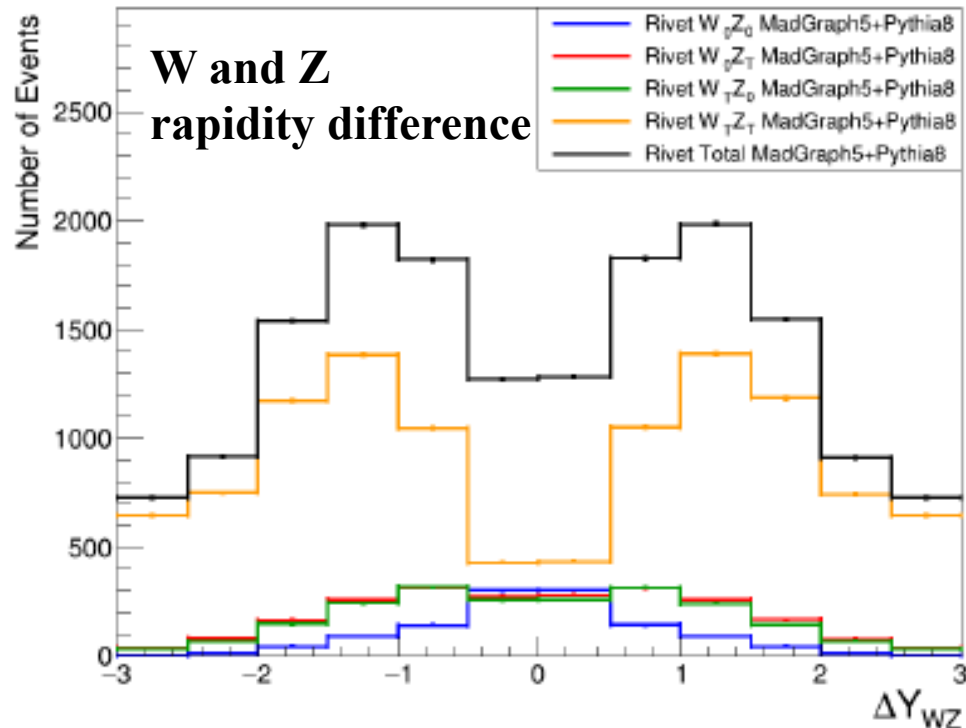
## Three-parameter fit: $f_{00}$ , $f_{0T+T0}$ , and $N_{\text{tot}}$

	Measurement	
	$100 < p_T^Z \leq 200 \text{ GeV}$	$p_T^Z > 200 \text{ GeV}$
$f_{00}$	$0.19 \pm_{0.03}^{0.03} \text{ (stat)} \pm_{0.02}^{0.02} \text{ (syst)}$	$0.13 \pm_{0.08}^{0.09} \text{ (stat)} \pm_{0.02}^{0.02} \text{ (syst)}$
$f_{0T+T0}$	$0.18 \pm_{0.08}^{0.07} \text{ (stat)} \pm_{0.06}^{0.05} \text{ (syst)}$	$0.23 \pm_{0.18}^{0.17} \text{ (stat)} \pm_{0.10}^{0.06} \text{ (syst)}$
$f_{TT}$	$0.63 \pm_{0.05}^{0.05} \text{ (stat)} \pm_{0.04}^{0.04} \text{ (syst)}$	$0.64 \pm_{0.12}^{0.12} \text{ (stat)} \pm_{0.06}^{0.06} \text{ (syst)}$
$f_{00}$ obs (exp) sig.	5.2 (4.3) $\sigma$	1.6 (2.5) $\sigma$

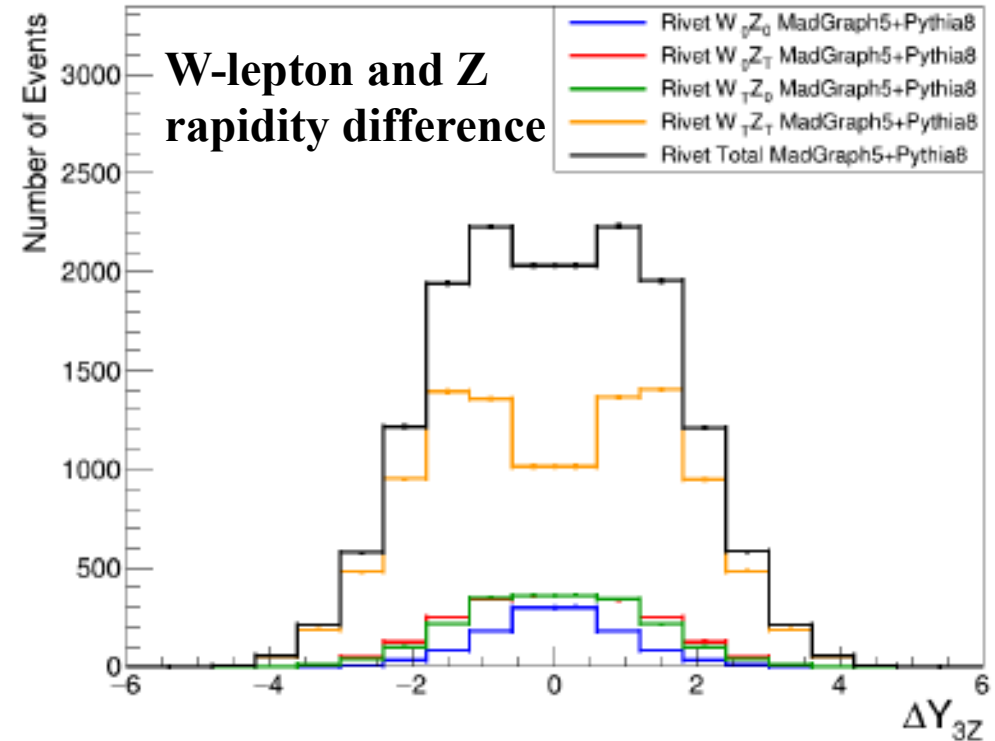
	Prediction	
	$100 < p_T^Z \leq 200 \text{ GeV}$	$p_T^Z > 200 \text{ GeV}$
$f_{00}$	$0.152 \pm 0.006$	$0.234 \pm 0.007$
$f_{0T}$	$0.120 \pm 0.002$	$0.062 \pm 0.002$
$f_{T0}$	$0.109 \pm 0.001$	$0.058 \pm 0.001$
$f_{TT}$	$0.619 \pm 0.007$	$0.646 \pm 0.008$

# Radiation amplitude zero

- Result of destructive interferences between different Feynman diagrams
- Theorists were pessimistic about the observation of RAZ in WZ production due to the polarization of the W boson (arXiv: hep-ph/9506286)
- New MadGraph versions allow us to generate WZ events in different polarization states
- A dip observed in  $\Delta\eta(l, \gamma)$  for  $W\gamma$  production, similarly we expect to see a dip in  $\Delta Y_{WZ}$  and  $\Delta Y_{lZ}$  distributions
- Larger dip expected in the  $\Delta Y_{WZ}$  distribution



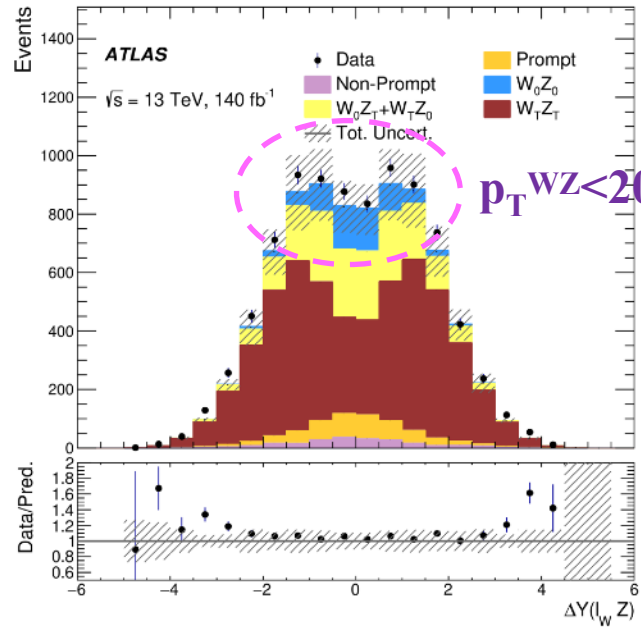
**TT, T0, 0T and 00 contributions are not stacked together**



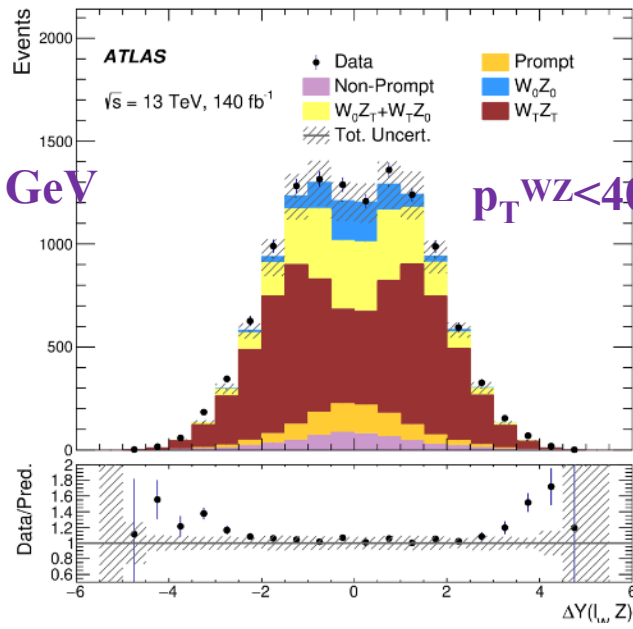
**Peak structure: 00, T0, and 0T**  
**Dip structure: TT**

Blue: 00  
 Red: 0T  
 Green: T0  
 Orange: TT

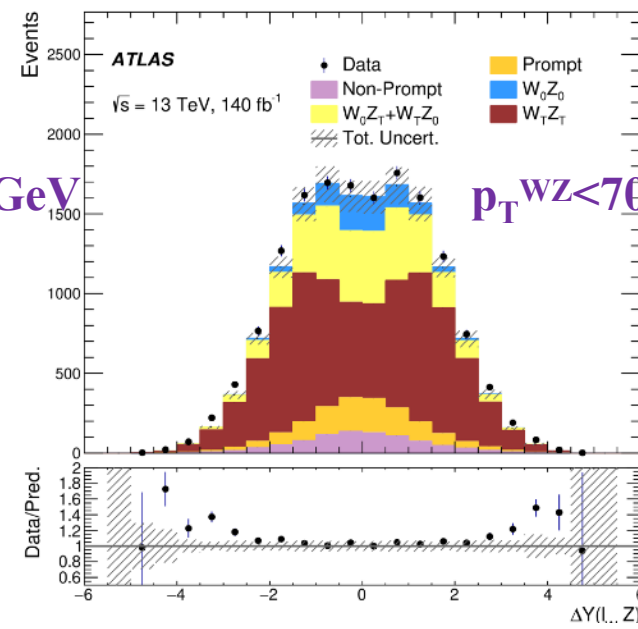
# RAZ effect for different $p_T(WZ)$ [ $\Delta Y(l_W Z)$ ]



$p_T^{WZ} < 20 \text{ GeV}$

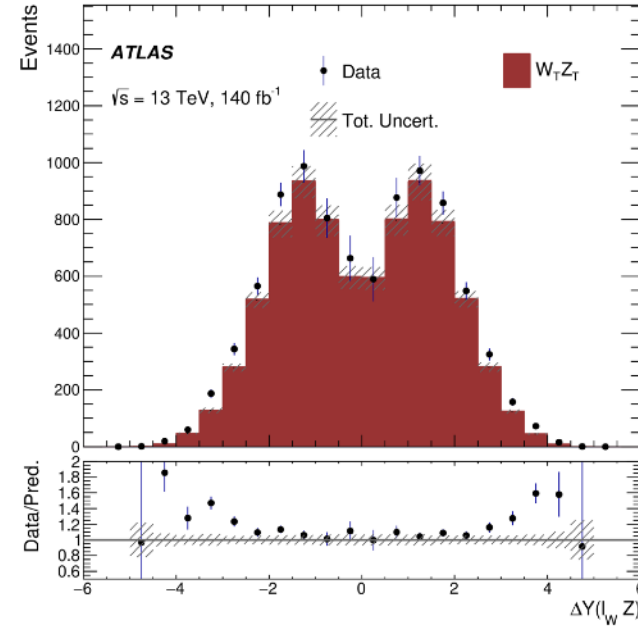
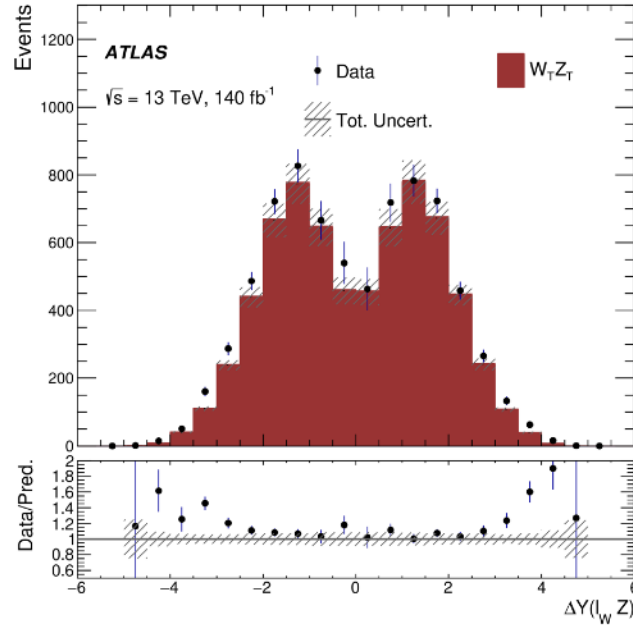
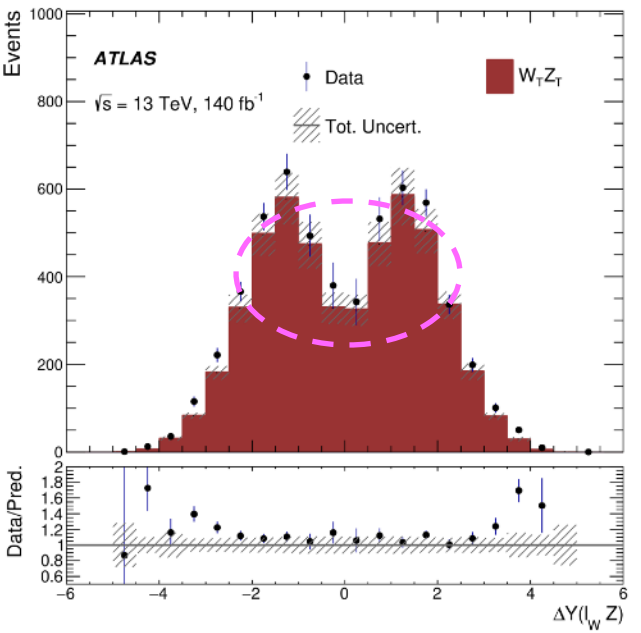


$p_T^{WZ} < 40 \text{ GeV}$



$p_T^{WZ} < 70 \text{ GeV}$

Inclusive events with contributions from all polarization states



TT-only events and contributions from 00, 0T, and T0 are removed

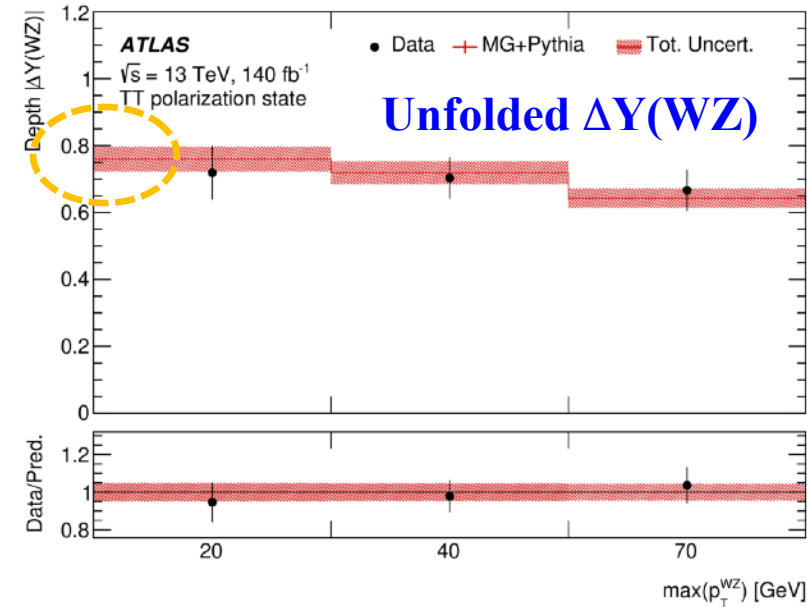
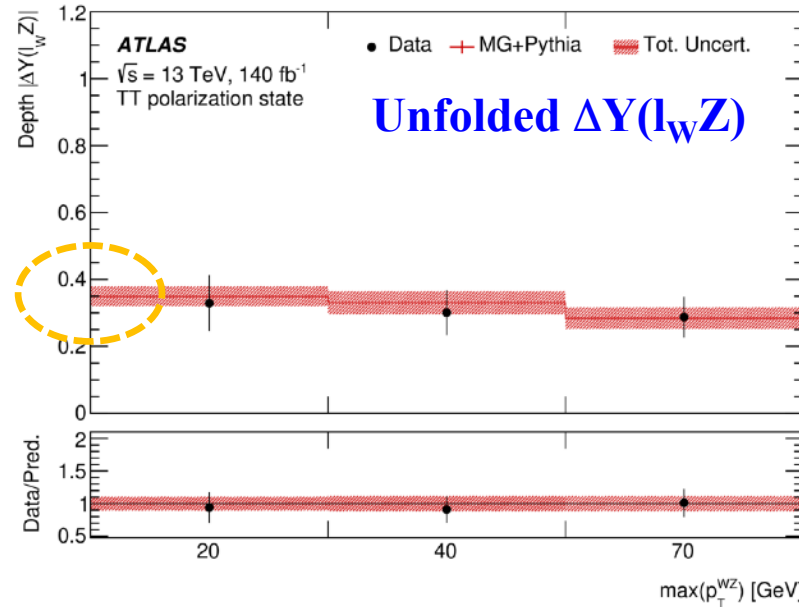
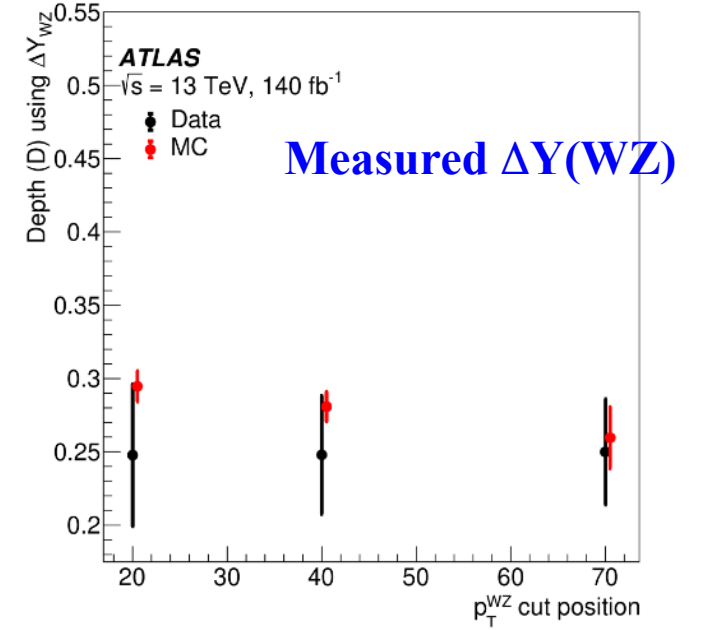
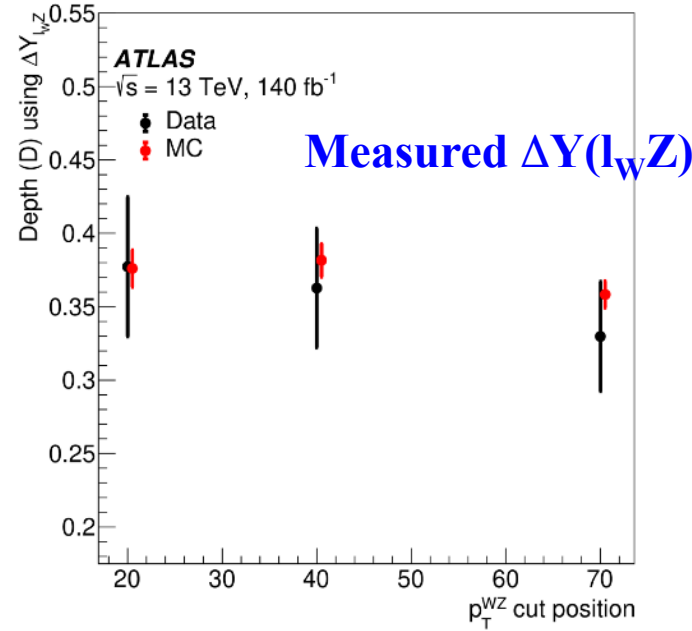
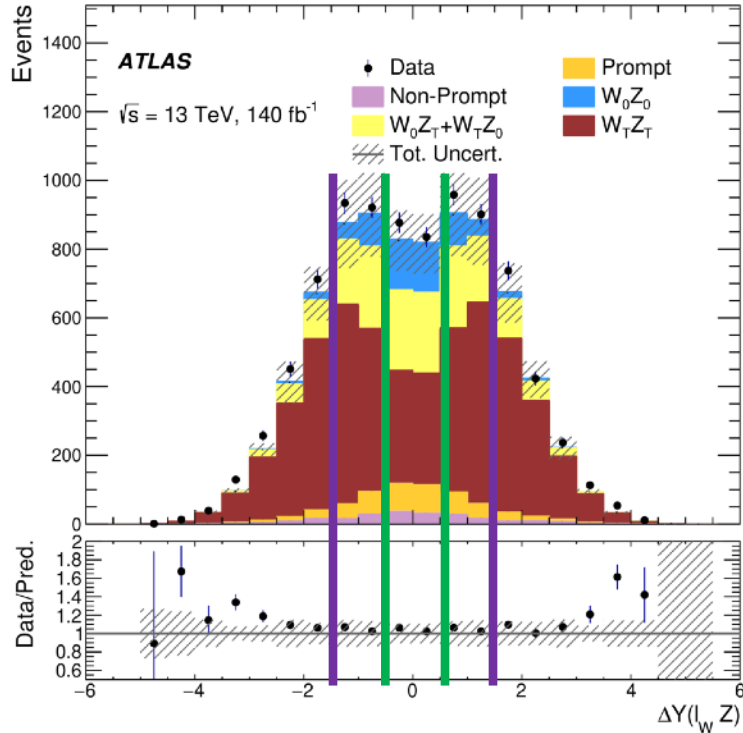
# Quantify the depth of the dip

$$D = 1 - 2 \times \frac{N_{\text{unf}}^{\text{central}}}{N_{\text{unf}}^{\text{sides}}}$$

$D=0$ , flat

$D>0$ , dip structure

$D<0$ , peak structure





# Conclusions

- Diboson polarization measurements are interesting:
  - Probe the ingredients of the Higgs mechanism (interactions of longitudinal components of W and Z bosons, Goldstone bosons, restoration of electroweak symmetry breaking, ...)
  - Perform precise measurements to test the SM gauge structure and higher-order corrections, constraints on the scale of new physics
  - Direct search for physics beyond the SM (new physics often sensitive to longitudinal components)
  - Increasing interests in both experimental and theoretical communities since ~2018
  
- With our current data we are already able to probe the polarization fractions in VV production:
  - First evidence/observation of double longitudinally-polarized vector bosons in VV production (inclusive WZ, inclusive ZZ, high- $p_T$  WZ s-channel events)
  - First observation of RAZ in WZ production with two transversely-polarized bosons
  - Large systematic uncertainty on measurements due to the modelling of polarized templates! → the theory community is actively working on these topics
  - VBS production still severely limited by data statistics, but already showing promise in same-sign WW production
  - VH polarization fractions are also interesting to measure
  - More results on polarization measurements of diboson (VV, VH), ratios of  $V_L V_L / V_L H$ , VBS polarization,  $H \rightarrow ZZ^*$  polarization and entanglement measurements are expected

# Some recent theoretical publications on polarized bosons

- Polarised VBS (so far LO):

[Poncelet's talk at the MBI2022 workshop](#)

W boson polarization in vector boson scattering at the LHC,

Ballestrero, Maina, Pelliccioli 1710.09339

Polarized vector boson scattering in the fully leptonic WZ and ZZ channels at the LHC,

Ballestrero, Maina, Pelliccioli 1907.04722

Automated predictions from polarized matrix elements

Buarque Franzosi, Mattelaer, Ruiz, Shil 1912.01725

Different polarization definitions in same-sign WW scattering at the LHC,

Ballestrero, Maina, Pelliccioli 2007.07133

- Polarized Diboson NLO QCD / NLO EW : WW / WZ / ZZ

Fiducial polarization observables in hadronic WZ production: A next-to-leading order QCD+EW study,

Baglio, Le Duc 1810.11034

Anomalous triple gauge boson couplings in ZZ production at the LHC and the role of Z boson polarizations,

Rahama, Singh 1810.11657

Polarization observables in WZ production at the 13 TeV LHC: Inclusive case,

Baglio, Le Duc 1910.13746

Unravelling the anomalous gauge boson couplings in ZW<sup>+</sup>- production at the LHC and the role of spin-1 polarizations,

Rahama, Singh 1911.03111

Polarized electroweak bosons in W+W<sup>-</sup> production at the LHC including NLO QCD effects,

Denner, Pelliccioli 2006.14867

NLO EW and QCD corrections to polarized ZZ production in the four-charged-lepton channel at the LHC,

Denner, Pelliccioli 2107.06579

Breaking down the entire spectrum of spin correlations of a pair of particles involving fermions and gauge bosons,

Rahama, Singh 2109.09345

NLO QCD predictions for doubly-polarized WZ production at the LHC,

Denner, Pelliccioli 2010.07149

Doubly-polarized WZ hadronic cross sections at NLO QCD+EW accuracy,

Duc Ninh Le, Baglio 2203.01470

Doubly-polarized WZ hadronic production at NLO QCD+EW: Calculation method and further results

Duc Ninh Le, Baglio, Dao 2208.09232

- Polarized Diboson NNLO QCD

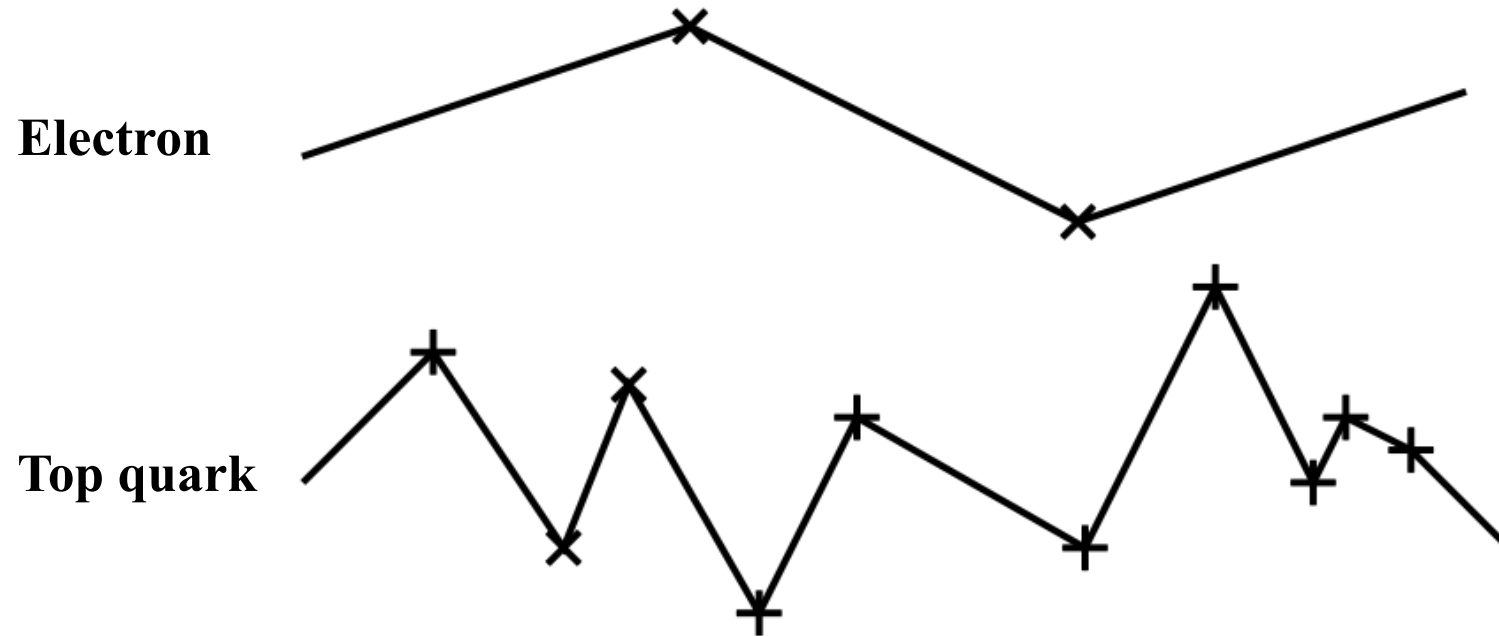
NNLO QCD study of polarised W+W<sup>-</sup> production at the LHC,

Poncelet, Popescu 2102.13583

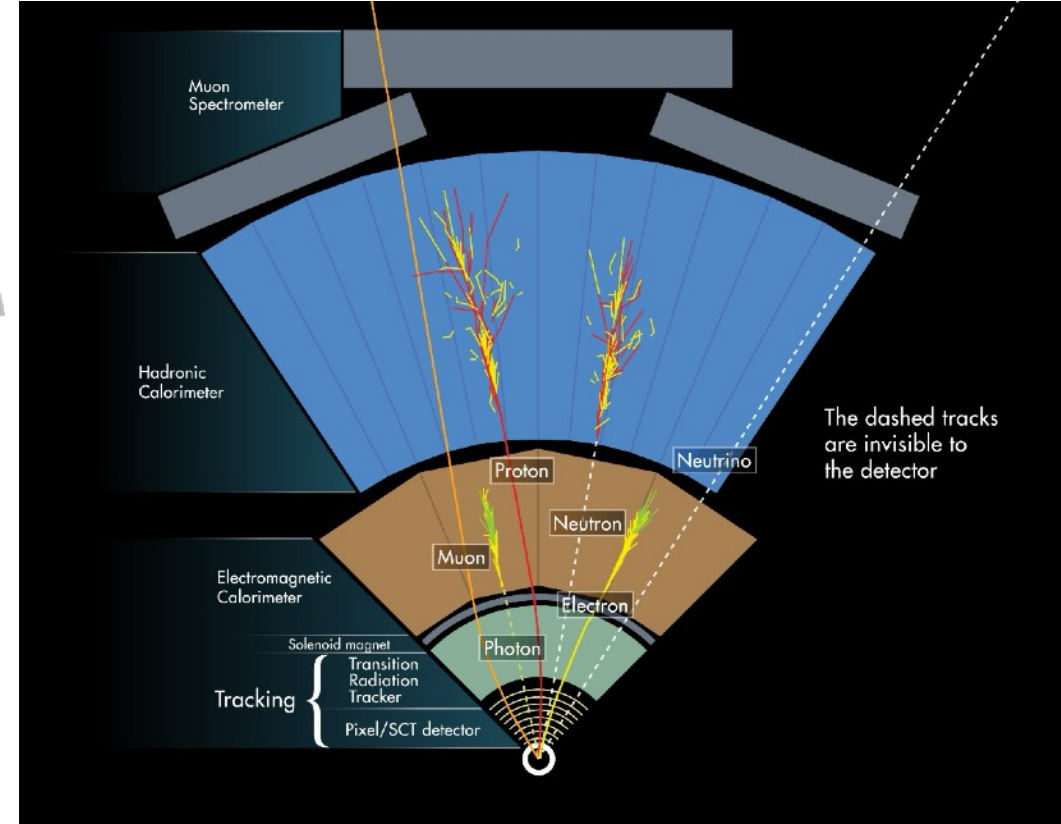
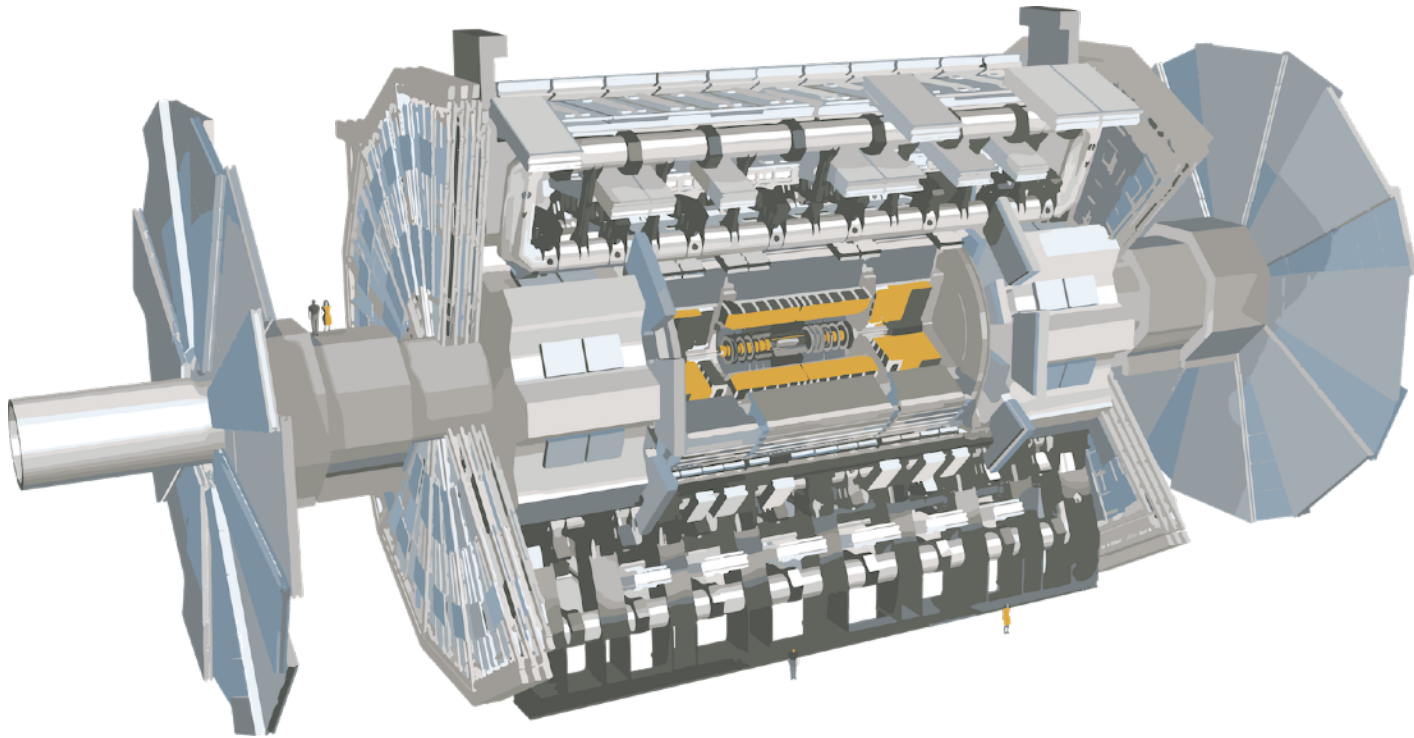
# BACKUP

# Fermion masses

- Masses of matter particles (Fermions) come from the Yukawa coupling between the particle and the Higgs field
  - Space is filled with the Higgs field
  - Matter particles interact with the Higgs field, “slow down” and appear to be massive
- The coupling depends on the mass of the particle, Higgs likes to couple to heavy particles



# ATLAS detector



# DNN Reweighting method hypotheses

- HP.1: A DNN can be trained to classify events belonging to two samples,  $S_A$  and  $S_B$ , in a way that its output can be interpreted as the likelihood of an event to belong to  $S_A$  and the complementary to unity of its output as the event likelihood to belong to  $S_B$ . Under such assumption, it is possible to define a weight function  $w(x) = DNN(x) / [1 - DNN(x)]$  that can reweight events from  $S_B$  to match  $S_A$ , where  $x$  is a vector of observables used as DNN inputs.
- HP.2: The underlying probability density function (pdf) to generate diboson polarized samples at NLO can be factorized as:

$$pdf_{NLO}(x, i, j) \propto pdf_{LO}(x) \times pdf(x, i, j) \times pdf_{LO \rightarrow NLO}(x)$$

where  $x$  is a vector of observables fully describing a generated event

$i, j = L, T$  are the W and Z polarization states

- the underlying  $pdf$  generating the polarized MadGraph sample is proportional to  $pdf_{LO}(x) \times pdf(x, i, j)$
- the  $pdf$  generating the unpolarized NLO WZ inclusive POWHEG sample is proportional to  $pdf_{LO}(x) \times pdf_{LO \rightarrow NLO}(x)$
- Such factorization implies that the  $pdf(x, i, j)$ , which generates the polarization states, does not depend on the generation order

# DNN Reweighting method

- Step 1: train a set of four DNNs,  $DNN(i, j)$ , to discriminate each  $(i, j)$  polarization MadGraph sample at LO from the sum of LO polarized MadGraph samples (unpolarized sample). The set of four weight functions defined as in HP.1 can then be interpreted as HP.2  $pdf(x, i, j)$ :
 
$$w(x, i, j) = DNN_{(i,j)}(x)/[1-DNN_{(i,j)}(x)] \propto pdf_{LO}(x) \times pdf(x, i, j)/pdf_{LO}(x) \propto pdf(x, i, j)$$
- Step 2: Applying  $w(x, i, j)$  to the NLO unpolarized POWHEG sample to produce NLO polarized samples

# DNN Reweighting validation

- $w(x, i, j)$  can be applied to the sum of LO polarized MadGraph samples to reproduce the LO polarized MadGraph samples, this is to validate HP.1
- An independent weight function can be derived by training one DNN to discriminate the NLO unpolarized POWHEG sample from the sum of LO polarized MadGraph samples (unpolarized). The corresponding weight function defined as in HP.1 can then be interpreted as HP.2  $pdf_{LO \rightarrow NLO}(x)$ :

$$w(x) = DNN(x)/[1-DNN_{(i,j)}(x)] \propto pdf_{LO}(x) \times pdf_{LO \rightarrow NLO}(x)/pdf_{LO}(x) \propto pdf_{LO \rightarrow NLO}(x)$$

If such  $w(x)$  is applied to the sum of LO polarized MadGraph samples, HP.1 can again be tested by comparing the reweighted unpolarized MadGraph NLO sample against the NLO unpolarized POWHEG sample

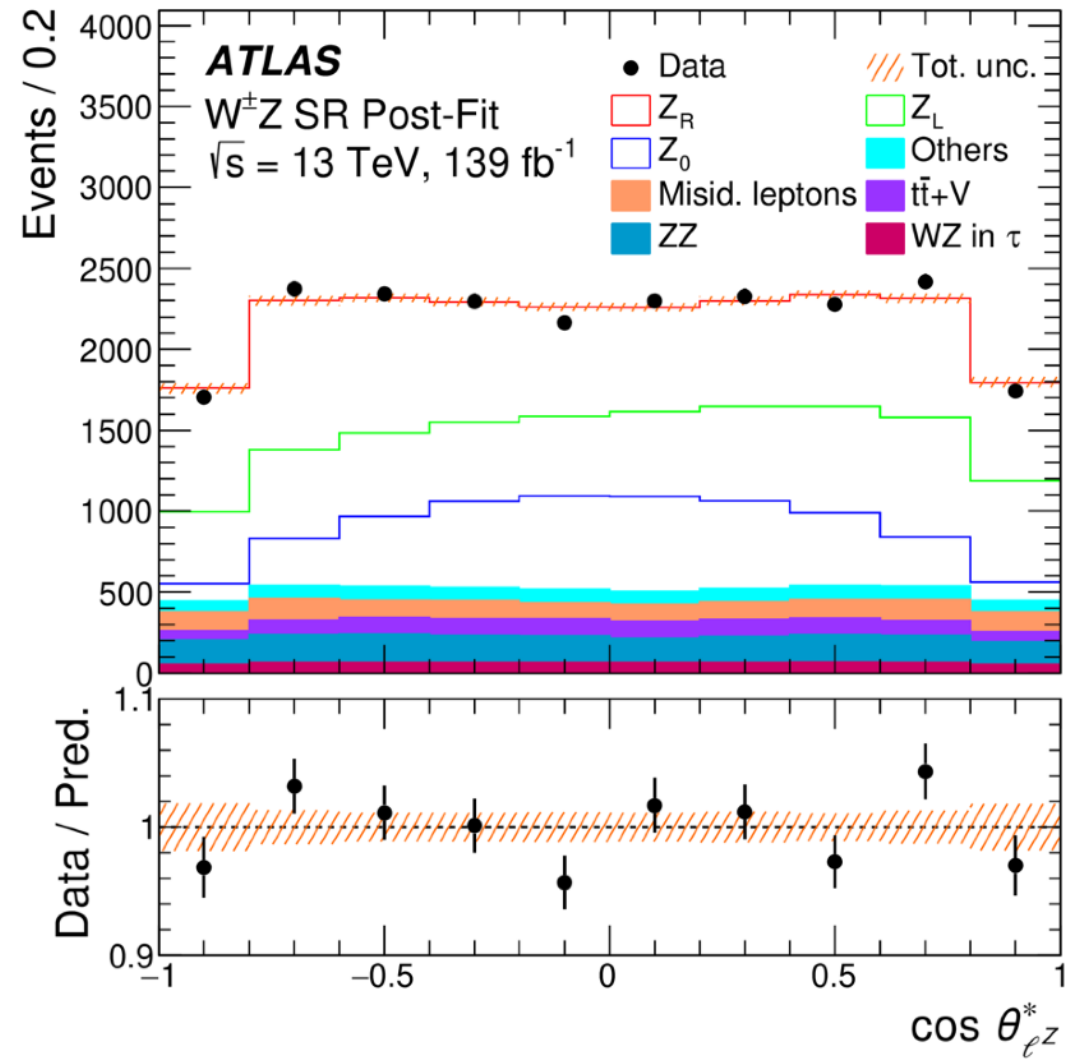
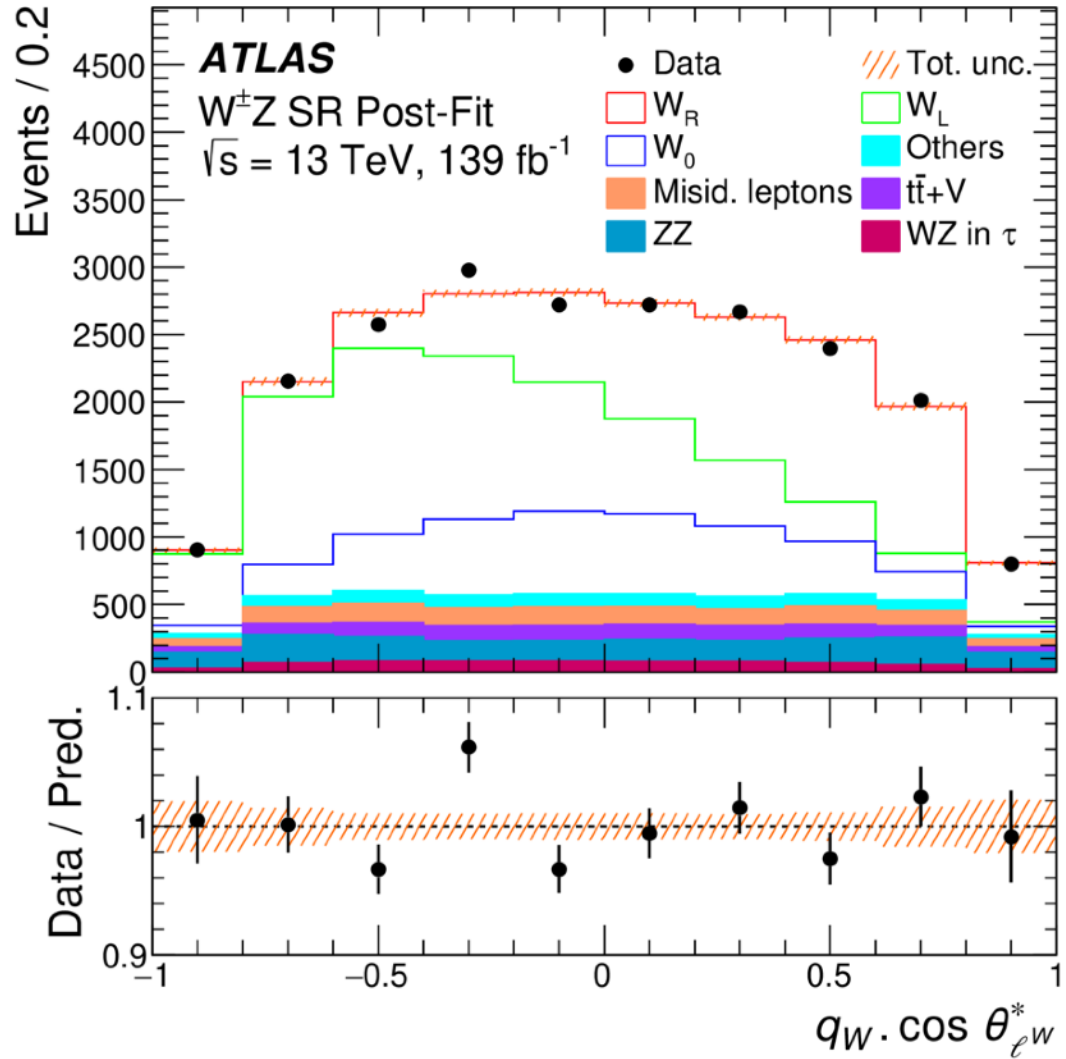
- If  $w(x)$  shown above is applied to the LO polarized MadGraph samples, an alternative set of NLO polarized samples can be obtained and HP.2 can be validated by comparing the two sets of reweighted polarized samples, the former being the NLO reweighting of LO polarized MadGraph samples and the latter being the polarization reweighting of NLO inclusive POWHEG sample



# Inclusive WZ diboson polarization uncertainties

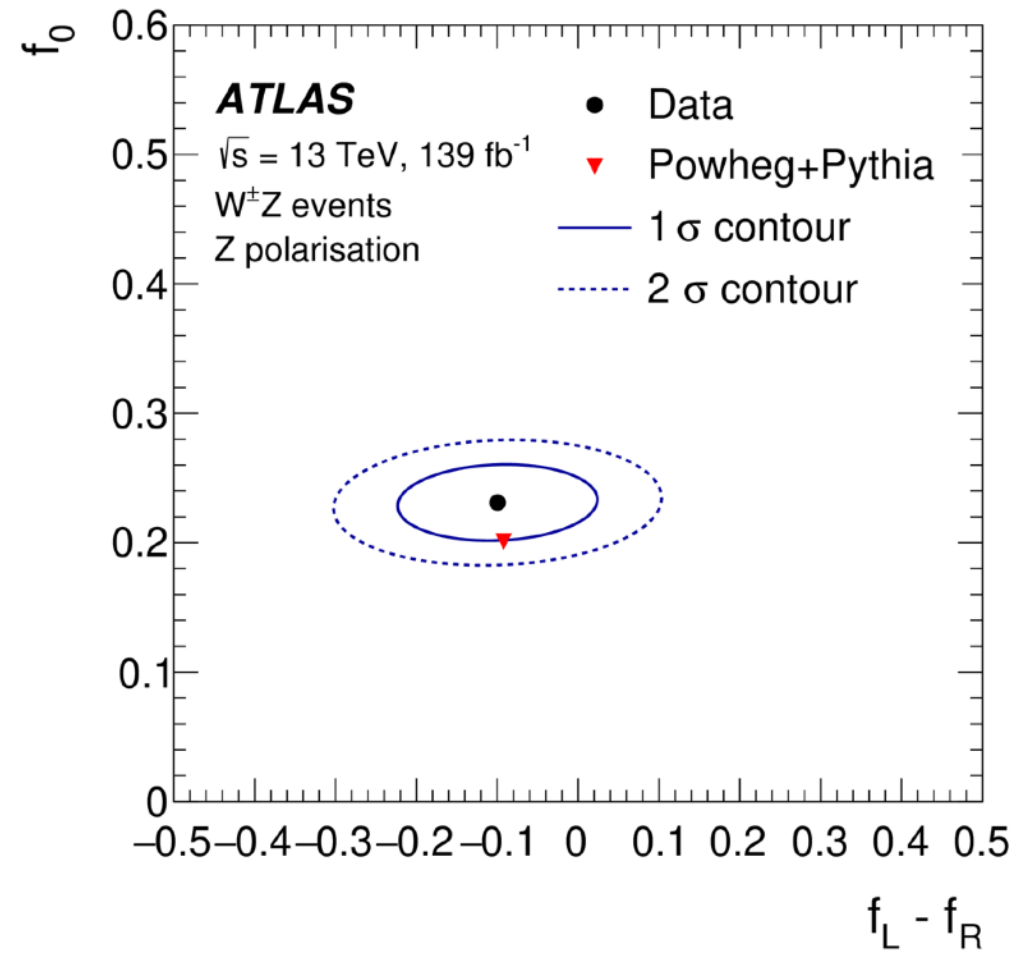
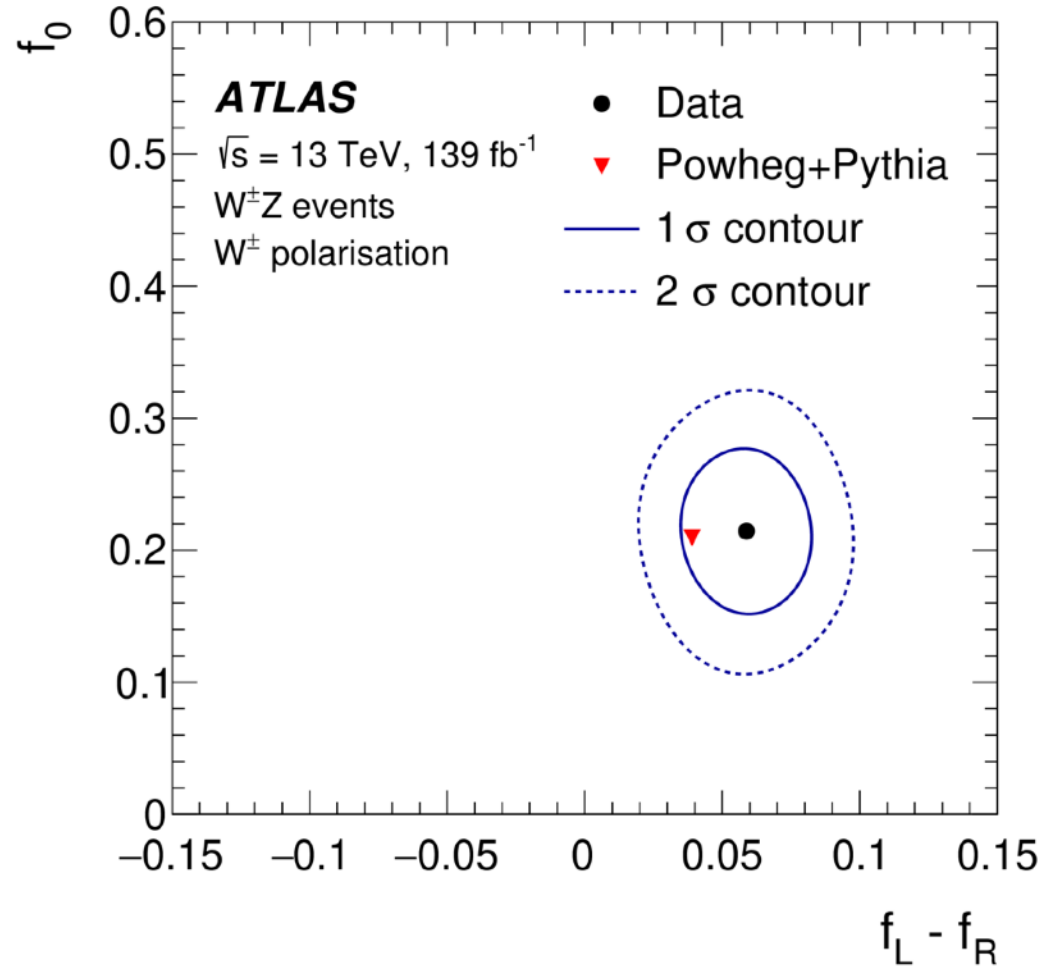
	$f_{00}$	$f_{0T}$	$f_{T0}$	$f_{TT}$
Relative uncertainty [%]				
$e$ energy scale and id. efficiency	0.34	0.6	0.8	0.31
$\mu$ energy scale and id. efficiency	0.8	0.23	0.23	0.13
$E_T^{\text{miss}}$ and jets	3.3	1.3	1.2	0.4
Pile-up	0.6	0.17	0.4	0.15
Misidentified lepton background	2.3	1.6	0.8	0.26
ZZ background	0.9	0.17	0.32	0.07
Other backgrounds	3.0	1.6	1.3	0.4
Parton Distribution Function	0.5	1.8	0.09	0.5
QCD scale	0.19	8	0.9	2.0
Modelling	9	4	2.9	1.2
Total systematic uncertainty	14	15	8	4
Luminosity	0.35	0.24	0.15	0.05
Statistical uncertainty	13	10	12	3.0
Total	19	18	14	5

# Post-fit data/MC comparison



All four categories of  $\cos\theta_{1,W}$  and  $\cos\theta_{1,Z}$  are summed together

# Single boson polarization results (Inclusive WZ)



# High-energy behavior of amplitudes with different polarizations

		SM	BSM	
LL	$q_{L,R}\bar{q}_{L,R} \rightarrow V_L V_L(h)$	$\sim 1$	$\sim E^2/M^2$	
TL	$q_{L,R}\bar{q}_{L,R} \rightarrow V_{\pm} V_L(h)$	$\sim m_W/E$	$\sim m_W E/M^2$	
TT	$q_{L,R}\bar{q}_{L,R} \rightarrow V_{\pm} V_{\pm}$	$\sim m_W^2/E^2$	$\sim E^2/M^2$	negligible contribution, $1/E^2$ dependence in SM
	$q_{L,R}\bar{q}_{L,R} \rightarrow V_{\pm} V_{\mp}$	$\sim 1$	$\sim 1$	

The results of the table can be understood as follows. Maximal helicity violating (MHV) amplitudes  $q\bar{q} \rightarrow V_{\pm} V_{\pm}$  are suppressed in the SM massless limit [20,21], and scale like  $m_W^2/E^2$  for finite mass; MHV selection rules don't apply in BSM, where they grow therefore unsuppressed. On the other hand,  $q\bar{q} \rightarrow V_{\pm} V_{\mp}$  are not suppressed in the SM at high-energy, but don't receive contributions from  $d = 6$  operators [19,22]. The suppression of SM amplitudes with one longitudinal only can be understood as a consequence of the symmetry under which all the SM doublets (Higgs and fermions) change sign, namely  $H \rightarrow -H$ ,  $Q_L \rightarrow -Q_L$  and  $L_L \rightarrow -L_L$ . This operation corresponds to the “ $g_L = -\mathbb{1}$ ” element of  $SU(2)_L$ , which is part of the SM gauge group and hence it is respected both by the SM and the BSM Lagrangian. Since the symmetry is only broken by the Higgs VEV  $v$ , it produces a selection rule that controls whether even or odd powers of  $v$  (actually, of  $m_W$ ) are present in the amplitudes [23]. Transversely polarized vector bosons are even under the symmetry, while longitudinal polarizations are odd because they are related to the Goldstone components of the Higgs doublet through the Equivalence Theorem.<sup>4</sup> The amplitudes for producing one transverse and one longitudinal state (or a Higgs) are odd, hence they scale like  $m_W/E$  and  $m_W E/M^2$ , respectively, in the SM and in the  $d = 6$  EFT, as the table shows.

# Radiation amplitude zero for $W\gamma$

arXiv:hep-ph/9506286

In fact, it is not difficult to see what is happening for some simple cases. Take  $d\bar{u} \rightarrow W^- \gamma$  as an example. There are three Feynman diagrams to contribute at the Born level: a  $t$ -channel diagram with an amplitude proportional to  $Q_u/t$ , a  $u$ -channel diagram proportional to  $Q_d/u$ , and an  $s$ -channel diagram proportional to  $Q_{W^-}/(s - M_W^2)$ , where  $t = (p_d - p_W)^2 = -\frac{1}{2}(s - M_W^2)(1 - \cos \theta)$ . Notice the charge relation in the Standard Model  $Q_d - Q_u = Q_{W^-}$ , and the kinematical relation  $s - M_W^2 = -t - u$ , one can easily cast the amplitude into the form

$$\mathcal{M} \sim \left( \frac{Q_u}{t} + \frac{Q_d}{u} \right) F(\sigma_i, \lambda_i, p_i), \quad (2)$$

# Radiation amplitude zero for WZ

arXiv:hep-ph/9506286

symmetry, such as the Standard Model (SM). It is conceivable that the radiation of a  $Z$ -boson may have some similarity to that of a photon. For the case of  $d\bar{u} \rightarrow W^- Z$ , the amplitude can be written as [13]

$$\mathcal{M} \sim X F_X(\sigma_i, \lambda_i, p_i) + Y F_Y(\sigma_i, \lambda_i, p_i), \quad (3)$$

where  $X$  and  $Y$  are combinations of coupling factors

$$X = \frac{s}{2} \left( \frac{g_-^{f_1}}{u} + \frac{g_-^{f_2}}{t} \right), \quad Y = g_-^{f_1} \frac{M_Z^2 s}{2u(s - M_W^2)}, \quad (4)$$

with the left-handed neutral current couplings  $g_-^{f_1} - g_-^{f_2} = Q_W \cot \theta_w$ , and  $F_{X,Y}(\sigma_i, \lambda_i, p_i)$  contain the spin dependent part and is roughly proportional to the product of the vector-boson wave functions  $\epsilon_w^* \cdot \epsilon_z^*$ . It is obvious that without the  $Y$ -term, the helicity amplitudes would factorize. In this case, all amplitudes would simultaneously vanish for  $g_-^{f_1}/u + g_-^{f_2}/t = 0$ , analogous to the  $W\gamma$  case in Eq. 2. Since  $Y$  is directly proportional to  $M_Z^2$ , one may naively expect full factorization when  $M_Z^2 \ll s$ . In fact, in the high energy limit, only three helicity amplitudes remain non-zero:

$$\begin{aligned} \mathcal{M}(\lambda_w = \pm, \lambda_z = \mp) &\longrightarrow \frac{1}{\sin \theta} (\lambda_w - \cos \theta) \left[ (g_-^{f_1} - g_-^{f_2}) \cos \theta - (g_-^{f_1} + g_-^{f_2}) \right], \\ \mathcal{M}(\lambda_w = 0, \lambda_z = 0) &\longrightarrow \frac{1}{2} \sin \theta \frac{M_Z}{M_W} (g_-^{f_2} - g_-^{f_1}). \end{aligned} \quad (5)$$

While the dominant amplitudes  $\mathcal{M}(\pm, \mp)$  fully factorize in the high energy limit,  $\mathcal{M}(0, 0)$  behaves differently. This can be traced to the special energy-dependence of the polarization

# Event yields at the truth level

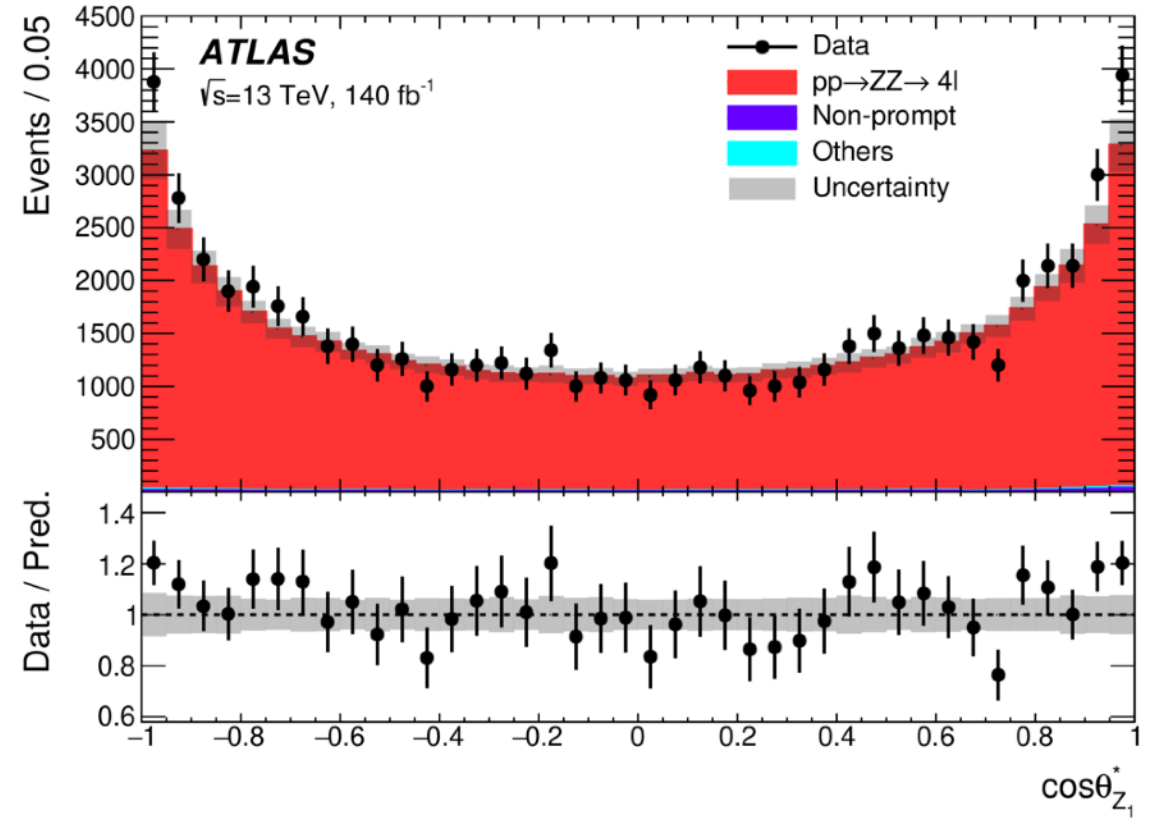
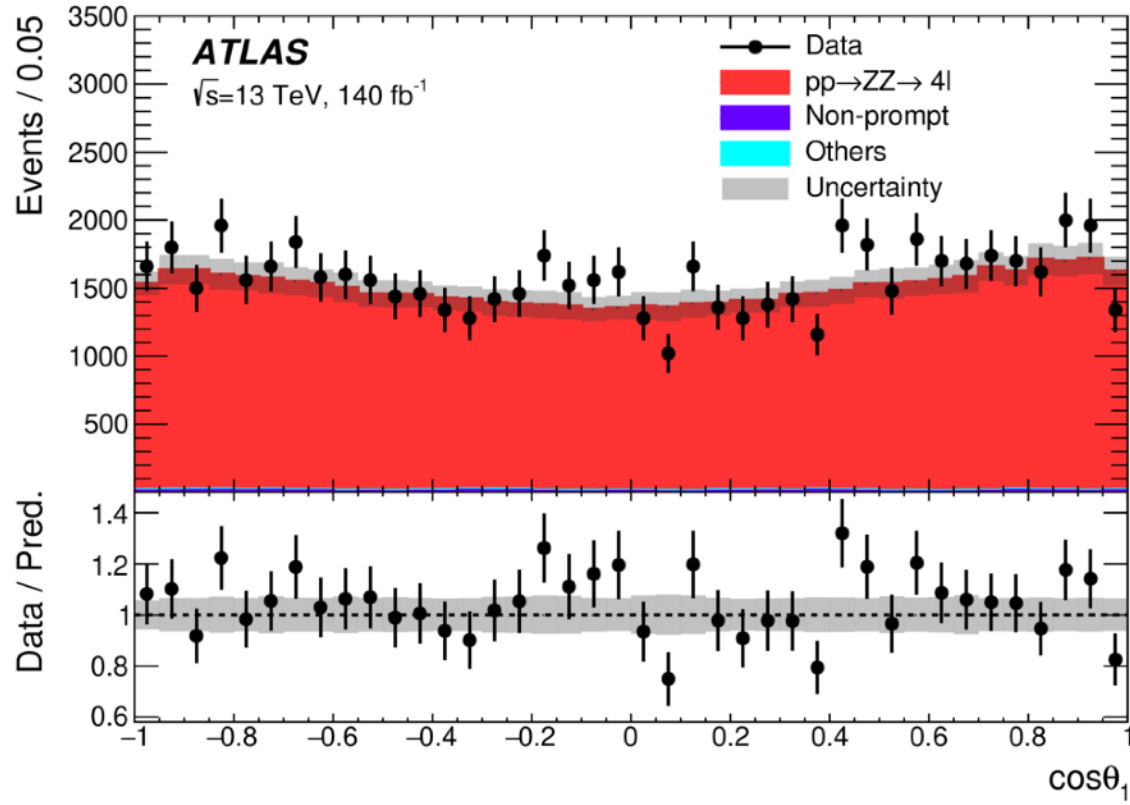
Selection cut	Polarization	Cross-section (pb)	No. of expected events			Fraction
			Total	0-jet	1-jet	
Without any cuts	$W_0Z_0$	0.0229	3214	2127	1103	4.7%
	$W_0Z_T$	0.0701	9825	3333	6511	14.3%
	$W_TZ_0$	0.0678	9496	3029	6482	13.8%
	$W_TZ_T$	0.330	46259	25472	20834	67.2%
Inclusive phase-space	$W_0Z_0$	0.00978	1370	888.9	490.5	5.7%
	$W_0Z_T$	0.0280	3924	1229	2698	16.4%
	$W_TZ_0$	0.0264	3699	1130	2566	15.5%
	$W_TZ_T$	0.106	14873	7415	7487	62.3%
$p_T^{WZ} < 70$ GeV	$W_0Z_0$	0.00875	1226	887	347	7.3%
	$W_0Z_T$	0.0165	2306	1228	1082	13.8%
	$W_TZ_0$	0.0155	2175	1129	1041	13.0%
	$W_TZ_T$	0.0785	10992	7403	3598	65.8%
$p_T^Z > 200$ GeV	$W_0Z_0$	0.000485	68	43	25	23.7%
	$W_0Z_T$	0.000119	17	8	9	5.8%
	$W_TZ_0$	0.000107	15	7	8	5.2%
	$W_TZ_T$	0.00133	187	88	99	65.2%
$p_T^Z > 100$ GeV	$W_0Z_0$	0.00258	361	252	109	16.1%
	$W_0Z_T$	0.00176	246	118	127	11.0%
	$W_TZ_0$	0.00160	224	116	110	10.0%
	$W_TZ_T$	0.0100	1407	703	701	62.9%
$100 < p_T^Z \leq 200$ GeV	$W_0Z_0$	0.00210	293	209	85	15.1%
	$W_0Z_T$	0.00164	229	111	118	11.8%
	$W_TZ_0$	0.00149	209	109	102	10.7%
	$W_TZ_T$	0.00867	1220	615	602	62.4%

# Variables used in the BDT training

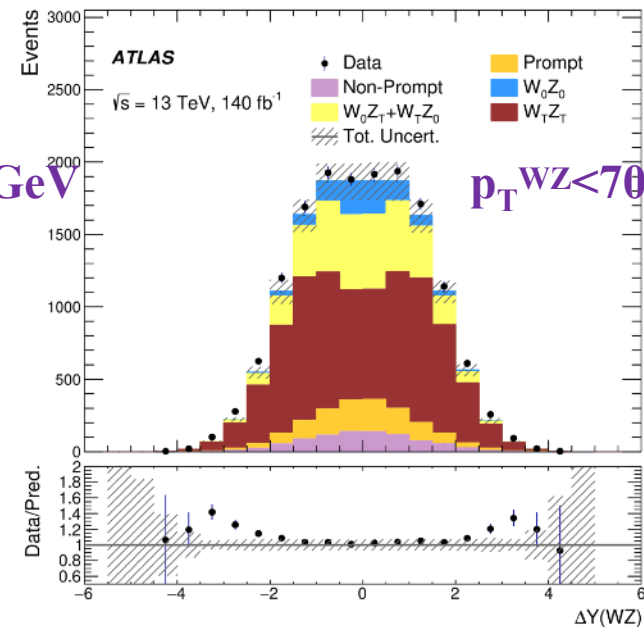
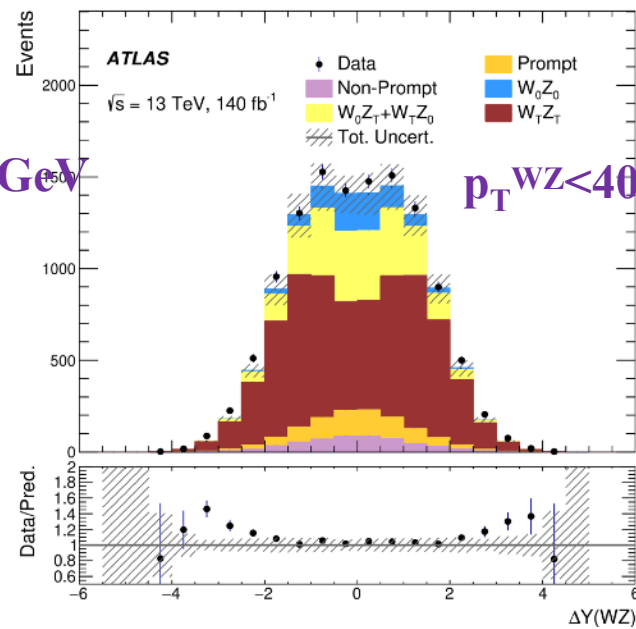
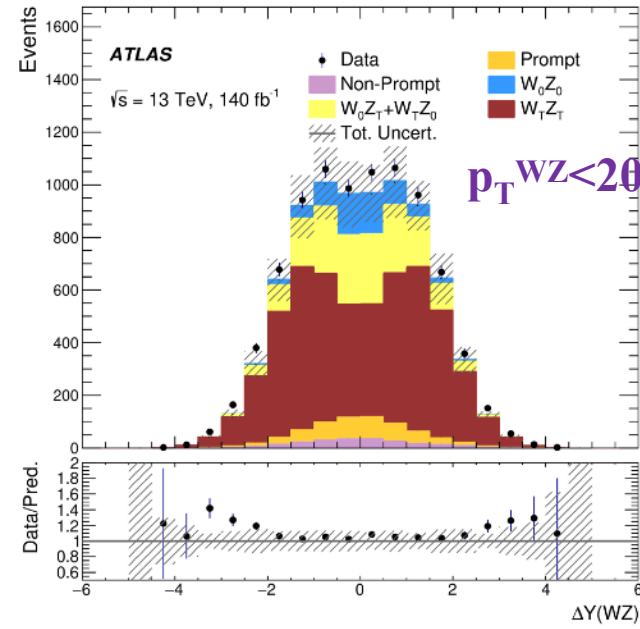
Training variable	Definition
$\Delta Y(\ell_W Z)$	Rapidity difference between the $W$ lepton and $Z$ boson
$p_T^{WZ}$	Transverse momentum of the $WZ$ system
$p_T(\ell_W)$	Transverse momentum of the $W$ lepton
$p_T(\ell_2^Z)$	Transverse momentum of the subleading $Z$ lepton
$E_T^{\text{miss}}$	Missing transverse momentum
$\cos \theta_{\ell_Z}$	Cosine of the angle of the $Z$ lepton in the $WZ$ rest frame w.r.t the $z$ -axis
$\cos \theta_{\ell_W}$	Cosine of the angle of the $W$ lepton in the $WZ$ rest frame w.r.t. the $z$ -axis



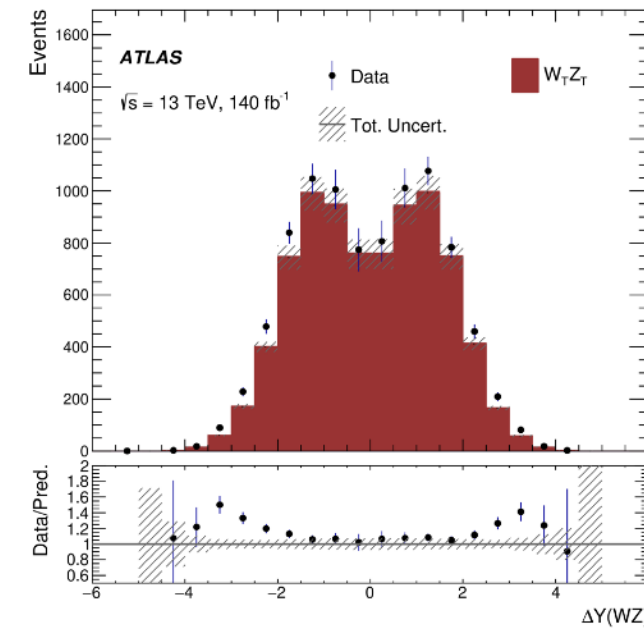
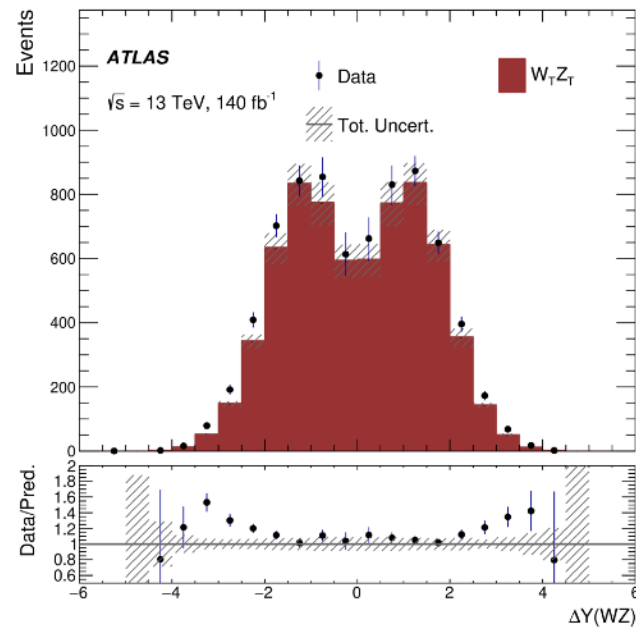
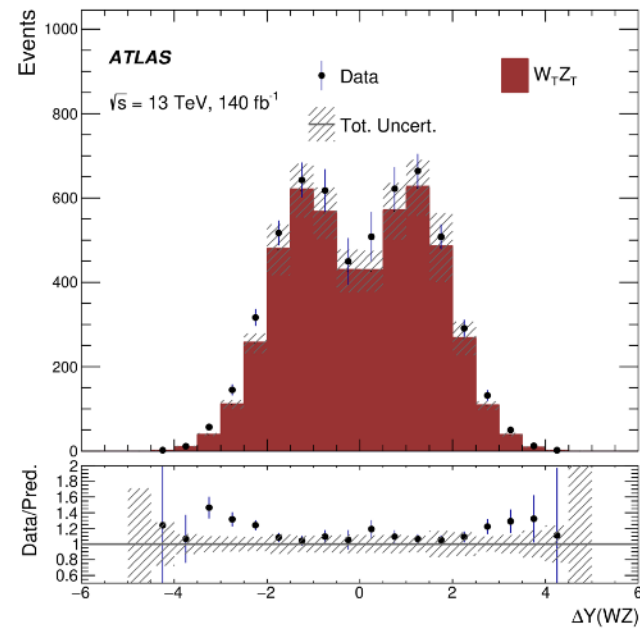
# ZZ Post-fit data/MC comparison



# RAZ effect for different $p_T(WZ)$ [ $\Delta Y(WZ)$ ]



Inclusive events with contributions from all polarization states



TT-only events and contributions from 00, 0T, and T0 are removed

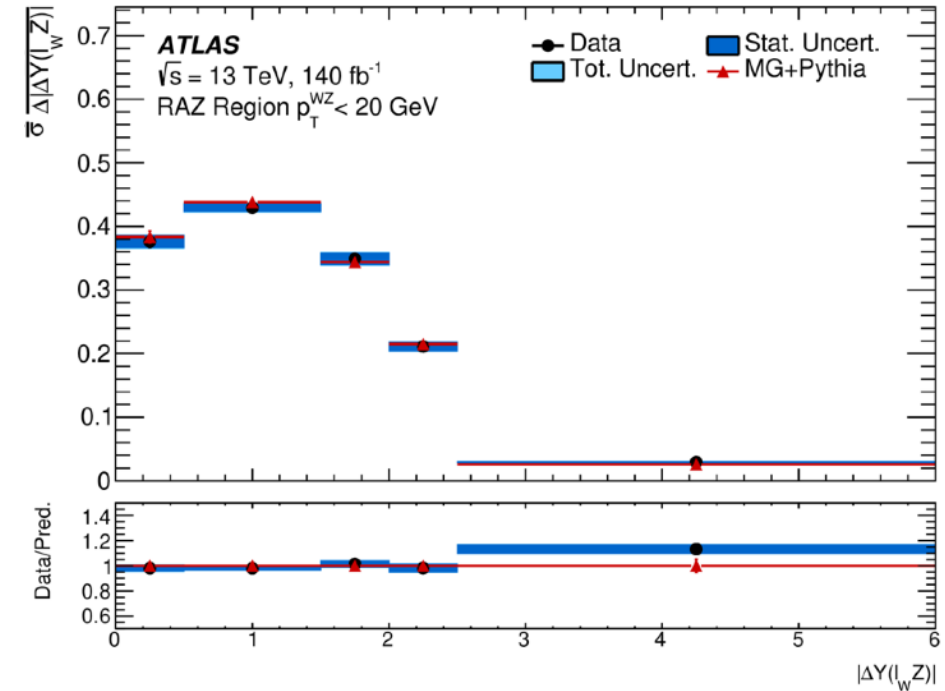
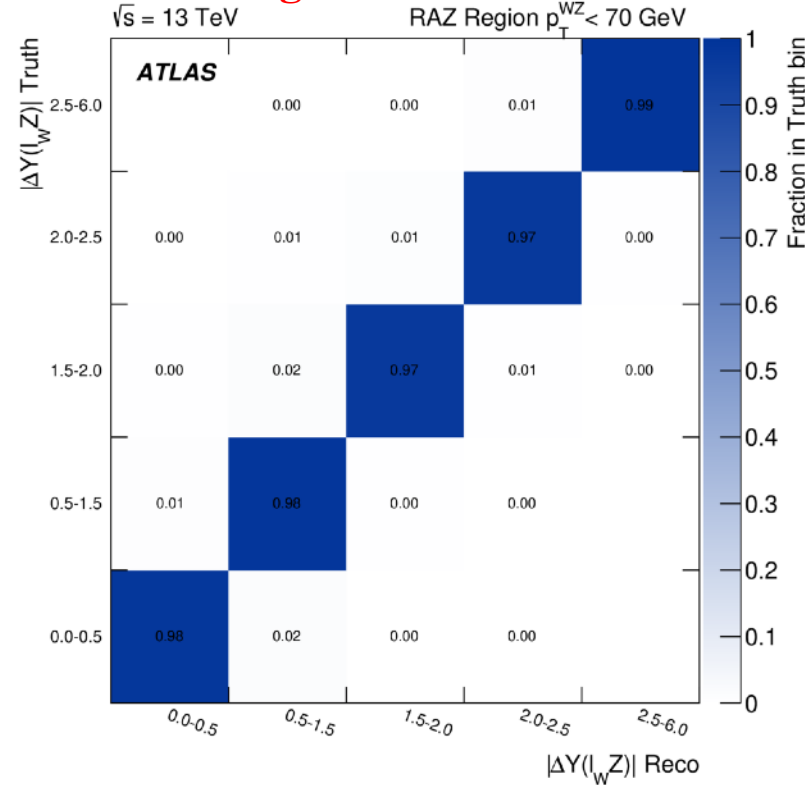
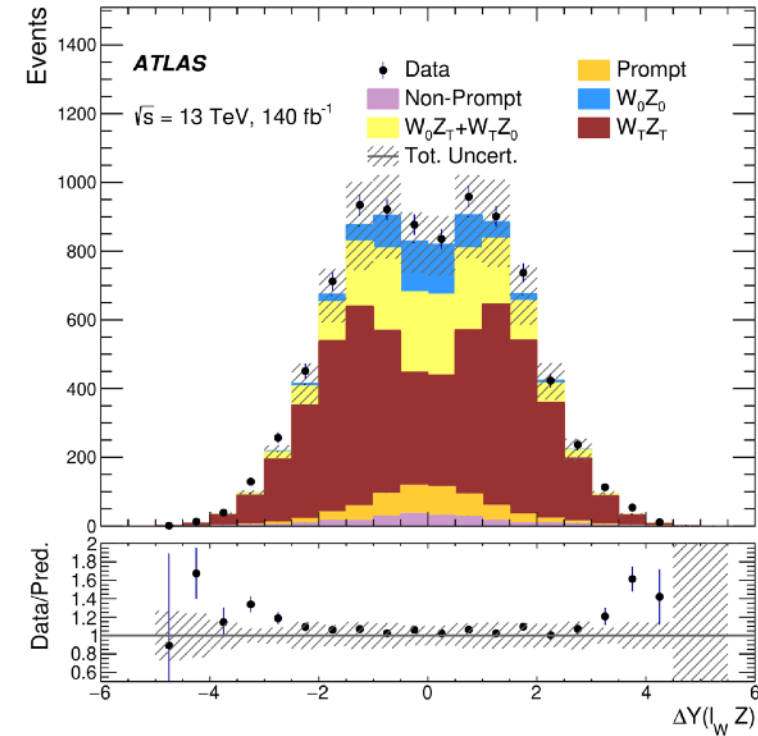
# Unfolded $\Delta Y(l_W Z)$ distributions

$p_T(WZ) < 20$  GeV

Raw distribution

Migration matrix

Unfolded distribution



- Unfolded both  $|\Delta Y(WZ)|$  and  $|\Delta Y(l_W Z)|$  distributions for 12 different cases:
  - For inclusive events with three  $p_T(WZ)$  cuts
  - For TT-only events with three  $p_T(WZ)$  cuts
- In general good agreement found between unfolded distributions and theoretical predictions

