

Effective Field Theory description of SM deviations

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Physics across energy scales

All Theories are Effective

an **Effective Theory** is obtained from a more fundamental one taking a kinematic or parametric limit \rightarrow typically ET = the LO in an expansion

- \triangleright ET typically simpler than the full theory in the pertinent regime
- ▶ one **doesn't need to know** the full theory to calculate! the ET is enough

separation of scales/decoupling

Newtonian gravity can be formulated w/o general relativity nuclear physics can be formulate w/o QCD chemistry can be formulated w/o SM. . .

 \rightarrow we expect any theory to be replaced by another one going to higher energies (until the ultimate Theory of Everything)

Effective Field Theories

Effective Field Theories

Fermi Theory of β decay

Bottom-up paradigm

measuring EFT parameters reveals properties of full theory \rightarrow complement direct searches, reach into higher energies

EFT fully specified by **fields+symmetries at E** = μ

- \rightarrow no reference to underlying model
- \rightarrow free couplings that can be measured!
- \rightarrow higher-d terms \Rightarrow limited UV validity, due to E growth

The Standard Model Effective Field Theory – SMEFT

promoting the Standard Model to an EFT

add higher-dimensional terms made of SM fields and respecting the SM symmetries

$$
\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}_5 + \frac{1}{\Lambda^2} \mathcal{L}_6 + \frac{1}{\Lambda^3} \mathcal{L}_7 + \frac{1}{\Lambda^4} \mathcal{L}_8 + \dots \qquad \mathcal{L}_d = \sum_i C_i \mathcal{O}_i^{(d)}
$$

 $C_i =$ Wilson coefficients

 $\mathcal{O}^{(d)}_i =$ gauge-invariant soperators forming a <u>basis</u>: a complete, non-redundant set Buchmüller, Wyler 1986

- **•** describes any beyond-SM theory, provided it lives at $\Lambda \gg v$
- ► a complete catalogue of all allowed beyond-SM effects, organized by expected size
- ▶ not experiment-specific! can be used as a common framework for LHC and other experiments
- ▶ a proper QFT! renormalizable order-by-order, systematically improvable in loops

SMEFT at $d = 5$: Majorana neutrino masses

only one operator! The operator of the opera

$$
\mathcal{L}_5 = C_{5,pr} \left(\overline{\ell_{L,p}^c} \tilde{H}^* \right) \left(\tilde{H}^\dagger \ell_{L,r} \right) + \text{h.c.} = C_{5,pr} \left(\ell_{L,p}^T \tilde{H}^* \right) \mathcal{C} \left(\tilde{H}^\dagger \ell_{L,r} \right) + \text{h.c.}
$$

\n
$$
\downarrow \text{EWSB}
$$

\n
$$
= C_{5,pr} \frac{(v+h)^2}{2} \overline{\nu_{L,p}^c} \nu_{L,r} + \text{h.c.} = C_{5,pr} \frac{(v+h)^2}{2} \nu_{L,p}^T \mathcal{C} \nu_{L,r} + \text{h.c.}
$$

 \rightarrow Majorana mass term for neutrinos + Higgs- ν interactions

violates lepton number conservation! in SM: L accidental. in SMEFT: not conserved in general.

 \diagup impose L conservation. $\Rightarrow \nu$ are Dirac particles, $C_5 \equiv 0$, must introduce ν_R to explain m_ν

 \searrow allow L violation. $\Rightarrow \nu$ are Majorana particles, $C_5 \neq 0$. no ν_R needed in EFT

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SMEFT at $d = 6$: the Warsaw basis

go down to O(100) imposing flavor symmetries, CP Faroughy et al 2005.05366 reljo et al 2203.09561 IB 2012.11343

> they are \sim never all relevant at the same time

Grzadkowski,Iskrzynski,Misiak,Rosiek 1008.4884

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SMEFT at $d = 6$: the Warsaw basis

 ∞ free parameters 2499

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A fast growing series

 $#$ parameters computed with Hilbert series and automated. **flavor** plays a major role.

Henning,Lu,Melia,Murayama 1512.03433

bases available up to dimension 12

- $d = 5$ Weinberg PRL43(1979)1566
- $d = 6$ Grzadkowski et al 1008.4884
- $d = 7$ Lehman 1410.4193, Henning et al 1512.0343
- $d = 8$ Li et al 2005.00008. Murphy 2005.00059
- $d = 9$ Li et al 2007.07899, Liao, Ma 2007.08125
- $d = 10.11.12$ Harlander, Kempksens, Schaaf 2305.06832

In SMEFT, operators of odd dimension violate the conservation of B and/or L Kobach 1604.05726

Renormalization Group evolution

when going to 1-loop divergences appear, reabsorbed by counterterms of the same dimension

SMEFT operators run and mix with each other, order by order in Λ

fully computed at 1 loop for dim-6, automated in DsixTools, wilson

Alonso,Jenkins,Manohar,Trott 1308.2627,1310.4838,1312.2014 Celis,Fuentes-Martin,Ruiz-Femenia,Vicente,Virto 1704.04504,2010.16341, Aebischer,Kumar,Straub 1804.05033

partial results for dim6-2loops and dim8-1loop

Elias-Miro' et al 2005.06983,2112.12131, Bern,Parra-Martinez 2005.12917, Jin,Ren,Yang 2011.02494, Fuentes-Martin,Palavric,Thomsen 2311.13630, Bresciani,Levati,Mastrolia,Paradisi 2312.05026, Chala et al 2106.05291,2205.03301,2309.16611. . .

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Below m_W : the Low Energy EFT (LEFT) or Weak EFT (WET)

at energies $\leq m_W$, the heaviest SM particles effectively decouple, and another EFT is more appropriate

fields: SM w/o H, W, Z, t symmetries: $U(1)_{em} \times SU(3)_{c}$

$$
\mathscr{L}_{\text{LEFT}} = \mathscr{L}_{\text{QED+QCD}} + \nu \mathscr{L}_3 + \frac{1}{\nu} \mathscr{L}_5 + \frac{1}{\nu^2} \mathscr{L}_6 + \dots
$$

$$
\mathcal{L}_{\text{QED+QCD}} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{4} G_{\mu\nu}^A G^{A\mu\nu} + \sum_{\psi} \bar{\psi} i \not{D} \psi - \sum_{\psi} \left[\bar{\psi}_R M_{\psi} \psi_L + \text{h.c.} \right]
$$

$$
+ \theta_{\text{QED}} \frac{e^2}{32\pi^2} F_{\mu\nu} \tilde{F}^{\mu\nu} + \theta_{\text{QCD}} \frac{g_s^2}{32\pi^2} G_{\mu\nu} \tilde{G}^{A\mu\nu}
$$

 \mathbb{C} employed extensively in **flavor physics**. at even lower energies $\leq \Lambda_{QCD}$: chiral perturbation theory

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LEFT operators

bases available up to $d = 9$ Jenkins,Manohar,Stoffer 1709.04486, Aebischer,Fael,Greub,Virto 1704.06639 Liao,Ma,Wang 2005.08013, Murphy 2012.13291, Li,Ren,Xiao,Yu,Zheng 2012.09188

matching to SMEFT and RG running Aebischer,Crivellin,Fael,Greub 1512.02830, Jenkins,Manohar,Stoffer 1709.04486,1711.05270

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The bigger picture $-$ a blooming research field!

no BSM particles discovered so far, no conclusive clue about where to find NP (HL-)LHC projected to reach %-ish precision on many observables

Higgs, EW, top, flavor sectors intertwined: each operator enters many places, each process corrected by many operators

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Higgs, EW, top, flavor sectors intertwined: each operator enters many places, each process corrected by many operators

adopt SMEFT as a universal tool for **agnostic**, **bottom-up searches**

perform a broad campaign of measurements, combined in large global analyses

Two main challenges

1. being sensitive to indirect BSM effects \rightarrow needs uncertainty reduction

in bulk
$$
\sim \frac{v^2}{\Lambda^2} = \frac{v^2 g_{UV}}{M^2}
$$
.
\n $g_{UV} \approx 1, \quad M \approx 2 \,\text{TeV}$ \rightarrow 1.5%
\non tails $\sim \frac{E^2}{\Lambda^2} \approx \frac{E^2 g_{UV}}{M^2}$ $E \approx 1 \,\text{TeV}, M \approx 3 \,\text{TeV}$ \rightarrow 10%

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2. making sure that, if we observe a deviation, we interpret it correctly

▶ retaining all relevant contributions: all operators, NLO corrections. . .

 \downarrow handling many parameters in predictions and fits, understanding the theory structure

- ▶ correct understanding of uncertainties and correlations
- § systematic mapping to BSM models

case study: latest ATLAS Higgs combination ATLAS 2402.05742

observables: Simplified-Template Cross Sections (STXS) D¨uhrssen-Debling et al 2003.01700 (IV.1) predictions:

$$
A_{SMEFT} = A_{SM} + \sum_{i} \frac{C_i}{\Lambda^2} A_i, \qquad A_i = \text{ amplitude with 1 insertion of operator } O_i
$$
\n
$$
\sigma_{SMEFT} = \sigma_{SM, best} \left[1 + \frac{1}{\Lambda^2} \sum_{i} \frac{2 \Re (C_i A_i A_{SM}^\dagger)}{|A_{SM}|^2} + \frac{1}{\Lambda^4} \sum_{i} \frac{|C_i A_i|^2}{|A_{SM}|^2} + \frac{1}{\Lambda^4} \sum_{i > j} \frac{2 \Re (C_i C_j^* A_i A_j^\dagger)}{|A_{SM}|^2} \right]
$$
\nlinear

 A_{SM} , A_i computed at the same order.

Automated in general-purpose Monte Carlo up to 1 loop in QCD (5 flavor scheme). IB 2012.11343 $_{\tt Degrande~et~al~2008.11743}$ 1-loop-EW and 2-loop-QCD results available (semi)analytic only for select processes

 $\sigma_{SM, best}$ can be computed at higher order in the SM (eg. NNLO, N³LO QCD)

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n case study: latest ATLAS Higgs combination ATLAS 2402.05742

effects in acceptances: operators that alter the kinematics can change the fraction of selected events

important to check these contributions when fitting unfolded observables

Marginalized fit results

all Warsaw basis considered, only 19 combinations meaningfully constrained

selected with Principal Component Analysis: diagonalize Fisher information matrix

$$
\mathcal{I}_{ij} = -\frac{\partial^2 \log \mathcal{L}}{\partial C_i \partial C_j}
$$

eigenvalues \simeq (bound)⁻¹ theep only eigenvectors with eigenvalues above a chosen sensitivity threshold

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Correlations

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Linear valley valley to the participation

ATLAS

 \sqrt{s} = 13 TeV. 139 fb⁻¹. m_{ν} = 125.09 GeV

 Δ

quadratics usually improve constraints comparison to linear helps checking EFT validity.

secondary minima can also appear in the likelihood

0.32 $10¹$ Linear+quad (obs.) Linear quau, (vus.) Ā $10¹$ 3.2 $10¹$ 10^{-1} $10¹⁰$ $10¹$ $p_{\rm SM} = 98.2\%$ **Best Fit** $-$ 68 % CL $\frac{Q_{1/2}Q_{2}}{Q_{2/2}Q_{2}}$ an din tingg 200000 $\frac{\mathsf{a}_{\mathcal{D}}}{\mathsf{a}_{\mathcal{D}}^{\prime\prime}}$ v **ATLAS** $\sqrt{8}$ = 13 TeV 139 ft $---$ Linear (exp.) $2 log(L/L)$ 10 $m_{\rm H}$ = 125.09 GeV Linear (obs.) SMEFT $\Lambda = 1$ TeV $---$ Linear + quad. (exp.) - Linear + quad. (obs.) -0.1 -0.05 0.05 0.1

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SMFFT $A = 1$ TeV

Top and Higgs interplay

SMEFT in LEP EWPOs

other pre-LHC EW measurements:

m^W CDF,D0 1204.0042

 $e^+e^- \rightarrow W^+W^-$ diff. ALEPH EPJC(2004)147 $e^+e^- \to e^+e^-$ diff. LEP2 1302.3415

SMEFT in LEP EWPOs

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Z-pole data leave 2 directions unconstrained in the Warsaw basis, that are (weakly) closed by WW

IB,Trott 1701.06424

 \downarrow results in strong residual correlations and large differences between individual and profiled bounds

Higgs, top and EW combinations

so far performed only by theorists: Fitmaker: Ellis, Madigan, Mimasu, Sanz, You 2012.02779

SMEFiT: Ethier,Maltoni,Mantani,Nocera,Rojo 2105.00006 SMEFiT: Celada,Giani,ter Hoeve,Mantani,Rojo,Rossia,Thomas,Vryonidou 2404.12809 SFitter: Elmeri,Madigan,Plehn,Schmal 2312.12502

From SMEFT to concrete BSM models

Automated matching tools

Fuentes-Martin, König, Pagès, Thomsen, Wilsch 2012.08506, 2212.04510

matchmakereft Carmona,Lazopoulos,Olgoso, Santiago 2112.10787

dictionaries

tree-level: complete deBlas,Criado,Perez-Victoria,Santiago

1-loop: partial Guedes, Olgoso, Santiago 2303.16965

f fit model parameters through SMEFT fitting infrastructure

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Open challenges for the future

- ▶ refine theory predictions, properly accounting for RG running in fits
- ▶ extend matching and running to **higher orders**
- § properly account for experimental uncertainties and correlations
- ▶ understand SMEFT effects beyond matrix element
- ▶ understand and treat SMEFT-born uncertainties [scale dependence, missing higher orders in loops and EFT. . .]
- ▶ relax Gaussianity assumptions in fit, incorporate full likelihoods from experiments
- \blacktriangleright relax flavor indices and CP assumptions
- ▶ explore interplay with resonance searches

§ . . .

EFT

An alternative to SMEFT? the Higgs EFT

changing the symmetry properties of the Higgs field changes the classification of BSM effects

Feruglio 9301281, Grinstein, Trott 0704.1505, Buchalla, Catà 1203.6510, Alonso et al 1212.3305, IB et al 1311.1823,1604.06801, Buchalla et al 1307.5017,1511.00988. . .

$$
H \mapsto \frac{v + |h|}{\sqrt{2}} \mathbf{U}, \qquad \mathbf{U} = \exp\left(\frac{i\vec{\sigma} \cdot \vec{\pi}}{v}\right)
$$

 $HEFT \supset SMEFT \supset SM$

- EXP HEFT expands around vacuum, SMEFT around $H = 0$
- ▶ recent geometric interpretation proves that Alonso, Jenkins, Manohar 1511.00724,1605.03602 there are BSM theories that admit HEFT but not SMEFT
	- with BSM sources of EWSB Cohen et al 2008.0597,Banta et al 2110.02967
	- with BSM particles that take $> 1/2$ of their mass from EWSB
- ▶ HEFT more convergent than SMEFT
- unclear whether unique HEFT phenomenological signatures exist

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Wrapping up

- ▶ Effective Field Theories are a powerful theoretical concept, long used to investigate nature
- ▶ in particular, SMEFT has become a very popular tool for BSM searches
	- \rightarrow enable **model-independent** "agnostic" searches
	- \rightarrow allow exploitation of high projected precision of HL-LHC measurements
	- \rightarrow allow joining information from LHC searches and measurements at other experiments
- ▶ the SMEFT program for LHC is blooming.
	- \rightarrow massive developments in several directions, theoretical and technical
	- \rightarrow sensitivity already in the interesting region for many operator classes!

