

# Water Cherenkov Applications/Challenges

August 7/8, 2023  
US-Japan Kick-off

Ryo Matsumoto, Ka Ming Tsui, Junjie Xia  
For Japan Group

# Current methods of simulation

Ka Ming Tsui

# Overview: Mostly GEANT4 based (e.g. WCSim)

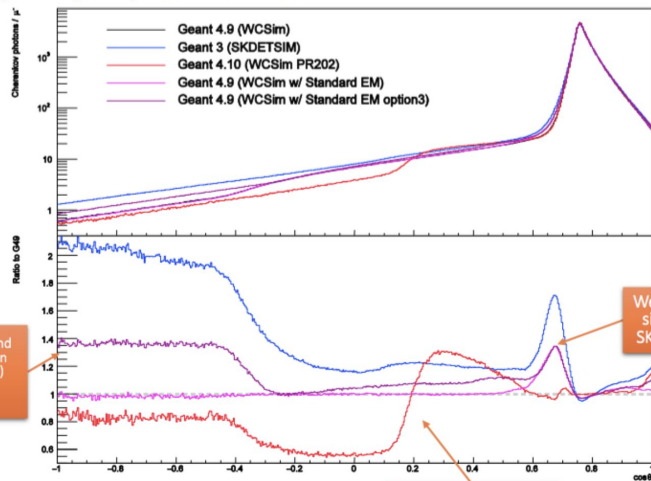
- Definition of physics processes
  - Cherenkov photon profile
  - Hadronic (pion, neutron) interactions
- Accurate description of material and detector geometry for optical processes
  - Photon tracking: water attenuation/scattering, surface absorption/reflection
  - PMTs (photosensors): dimensions, reflectors & inner-structures, photocathode
- Simulation of electronic responses
  - PMT (quantum) efficiency, charge and time smearing
  - Gain/efficiency variations, effects of residual magnetic fields
- Monte Carlo method of particle propagation
  - Stochastic method requires large computing resources

# Physics Processes

- Definition of physics processes
  - Cherenkov photon profile
  - Hadronic (pion, neutron) interactions

## Cherenkov profile for 600 MeV $\mu^-$

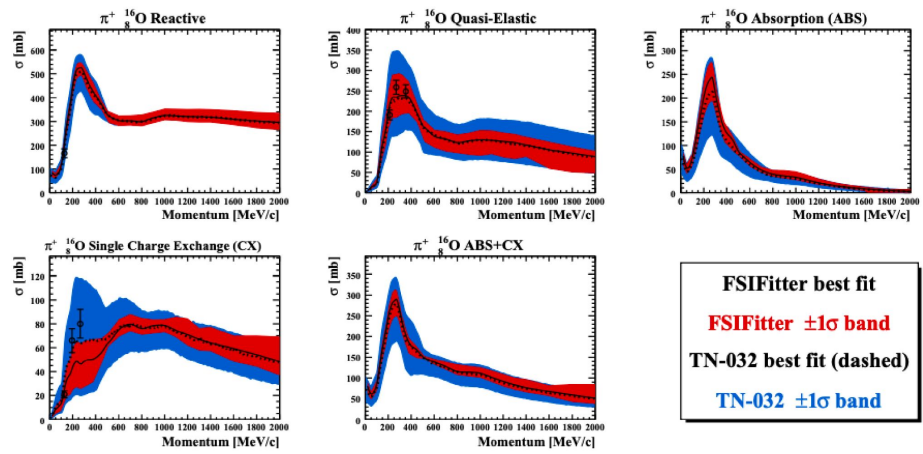
Using true optical photon information.



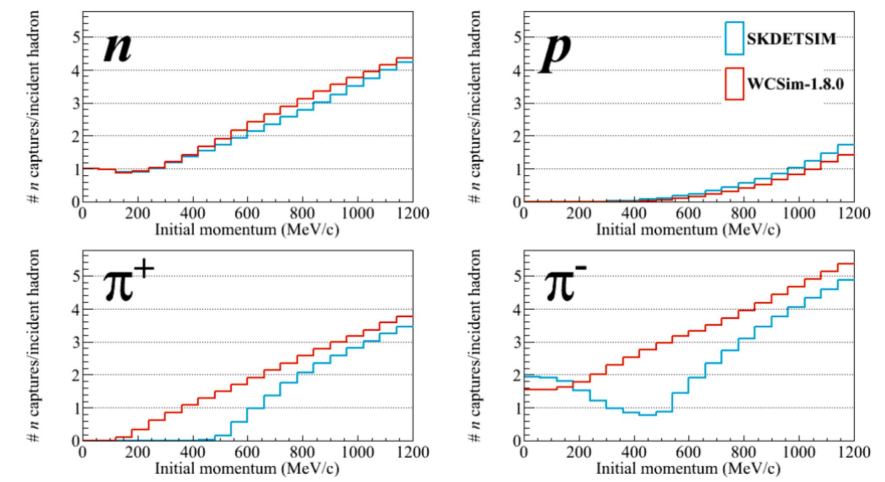
Large angle trend similar between detailed (opt3) model and SKDETSIM

Wentzel IV model has similar structure to SKDETSIM near peak

Geant 4.10 (PR202) very different from other models at angles close to normal

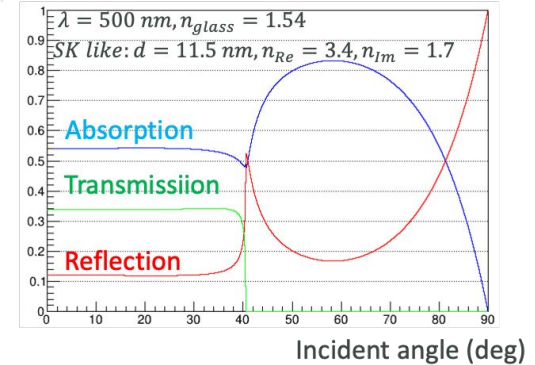
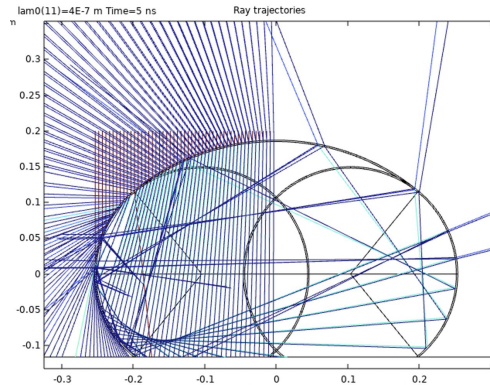
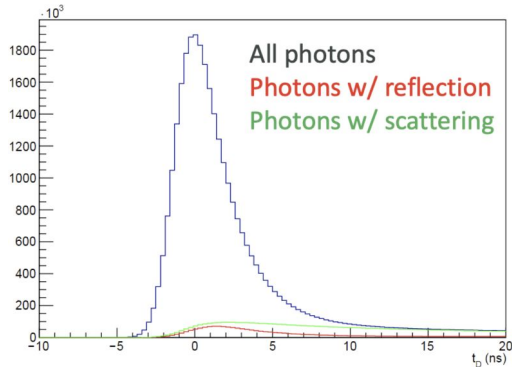
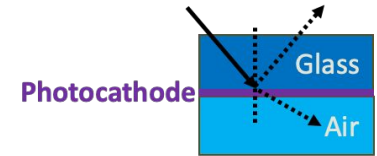
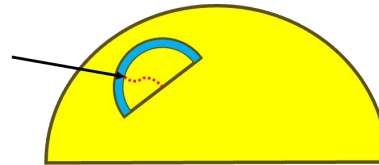
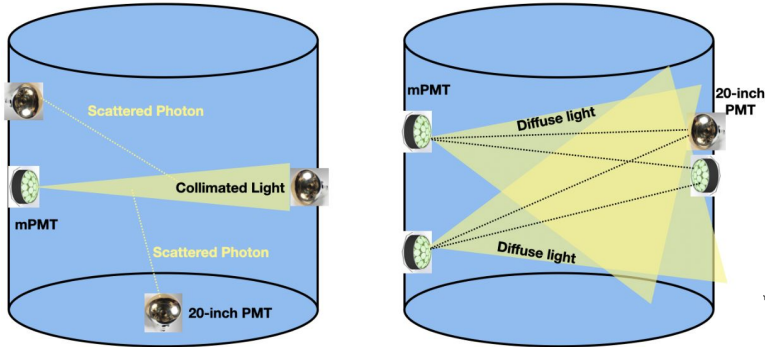


**FSIFitter best fit**  
**FSIFitter  $\pm 1\sigma$  band**  
**TN-032 best fit (dashed)**  
**TN-032  $\pm 1\sigma$  band**



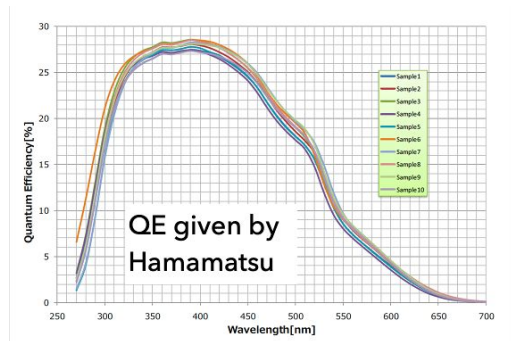
# Optical Processes

- Accurate description of material and detector geometry
  - Photon tracking: water attenuation/scattering, surface absorption/reflection
  - PMTs (photosensors): dimensions, reflectors & inner-structures, photocathode

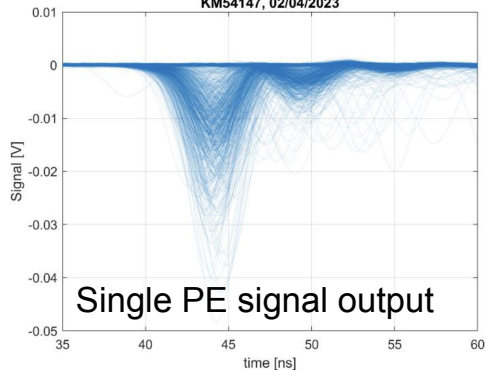


# PMT and Electronics Response

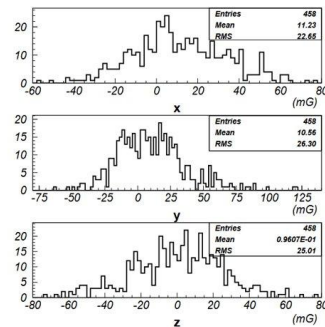
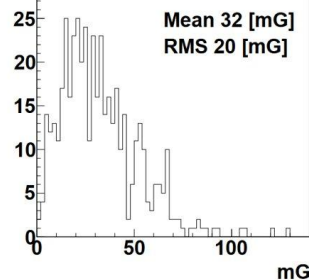
- Simulation of electronic responses
  - PMT (quantum x collection) efficiency, charge and time smearing
  - Gain/efficiency variations, effects of residual magnetic fields



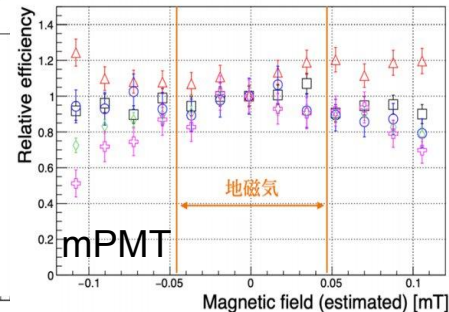
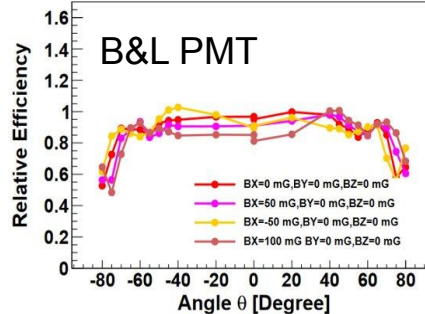
Signal samples HV = 1100V  
KM54147, 02/04/2023



## SK residual magnetic field measurements



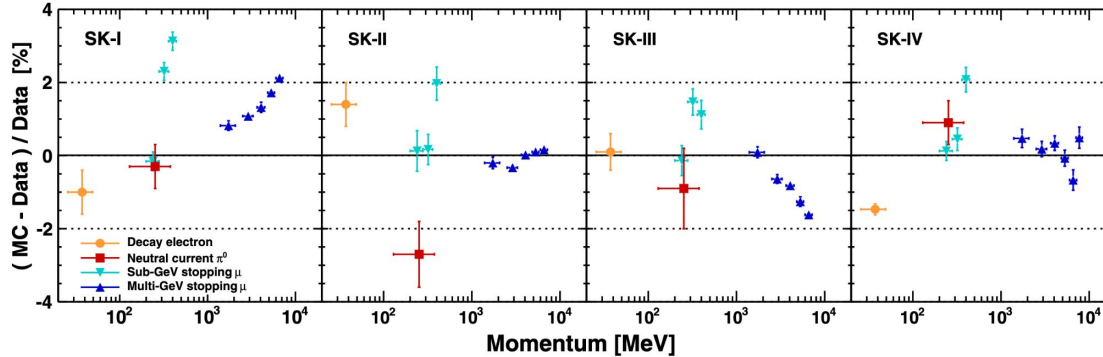
EF6453 Y Direction Scan Efficiency vs. Position (Angle) with BX Change



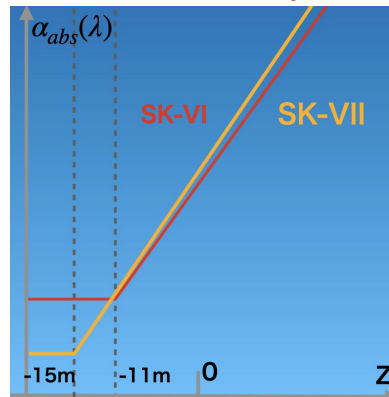
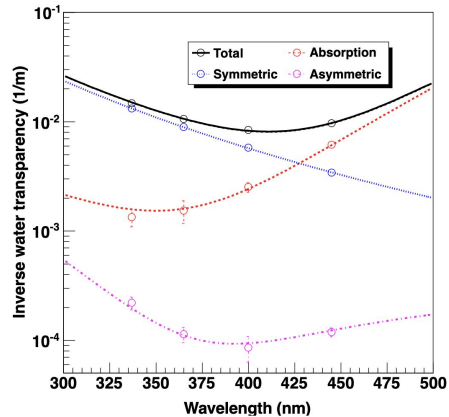
# Current methods of calibration

# Top-down approach

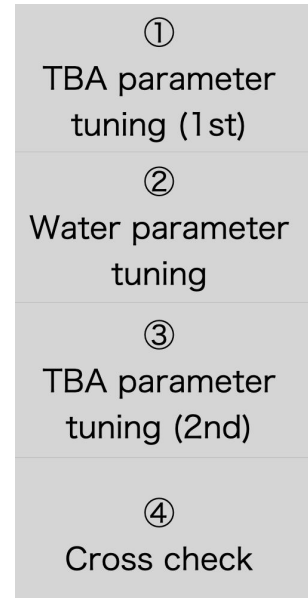
- Effective parameters of energy uncertainty



- Tuning of e.g. water parameters are not properly correlated



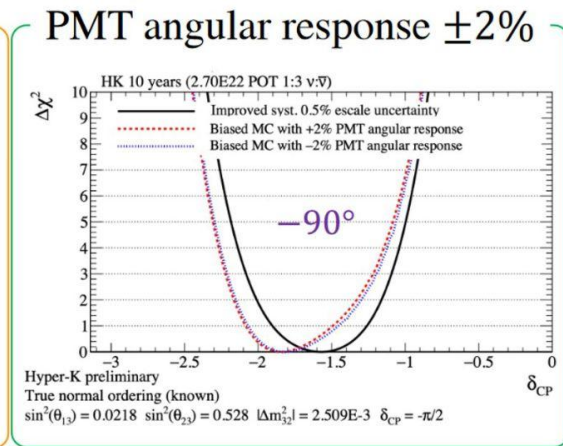
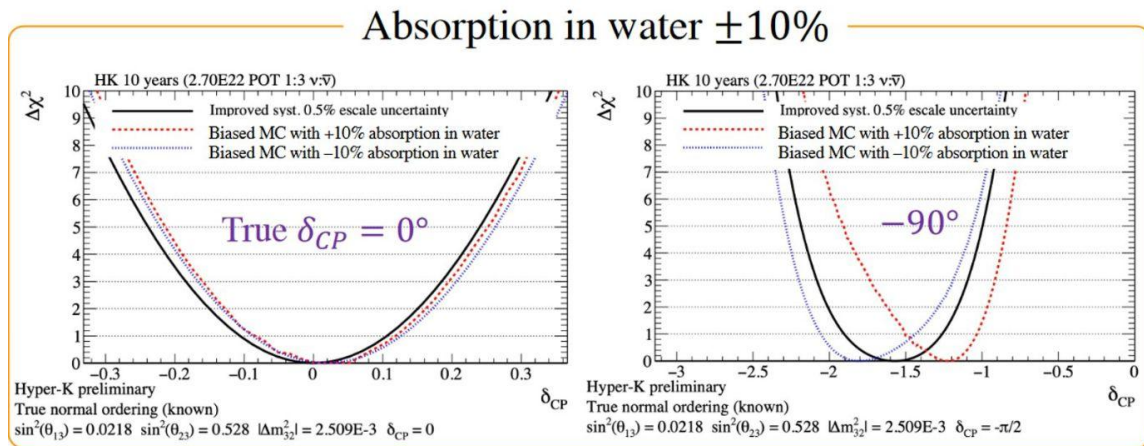
## Sequential steps





# Bottom-up approach

- Formulate set of important detector parameters
  - Water quality, photocathode model, pe conversion factor/collection efficiency, reflectivity, etc.
- Derive prediction for diffusers, LED, radioactive source, etc.
  - Analytic + MC simulation (empirical parametrization + spline)
- Maximum likelihood fit w.r.t. Data
  - Challenges of computing time and convergence over large number of parameters and calibration samples
- Propagate uncertainties to reconstruction and oscillation analysis



# Application of DDSims to e.g. WCTE

- Goal:

Photons starting at position  $\mathbf{r}$ , direction  $\mathbf{u}$

$$p(\mu, t)_i = N_{\text{ph}}(\mathbf{r}, \mathbf{u}) \left( \phi^{\text{dir}}(\mathbf{r}, \mathbf{u}, i) + \phi^{\text{ind}}(\mathbf{r}, \mathbf{u}, i) \right)$$

PMT hits

Direct & indirect hit prediction

- Known photon calibration sources (LEDs, diffuser ball, NiCf) to train  $\phi$ 
  - Easiest and earliest proof-of-concept from calibration runs
- Tagged particle beams to train Cherenkov yields from particles of known ID and kinematics
  - Secondary interactions and decays, etc. are included, will need more careful event selections

# fiTQun - Event Reconstruction

Ryo Matsumoto

# Concept of fiTQun

- A maximum likelihood fitter based on the look-up table of Cherenkov photons (maximized using MINUIT by ROOT).
- Likelihood function  $L(x)$  uses charge and time information of the PMTs and determine the particle kinematics  $x$ :

$$L(x) = \underbrace{\prod_j^{\text{unhit PMTs}} P(\text{unhit}_j|x)}_{\text{unhit probability}} \underbrace{\prod_i^{\text{hit PMTs}} P(\text{hit}_i|x) f_q(q_i|x) f_t(t_i|x)}_{\text{hit probability, charge and time likelihood}}$$

- Both of the hit and unhit probabilities are taken into account.
- All parameters  $x$  (vertex, direction, momentum etc.) are fit simultaneously.
- *Need to prepare look-up tables*

# Predicted charge by direct photon

- $P$ ,  $f_q$ ,  $f_t$  are functions of predicted PMT charge  $\mu$
- The charge is estimated from the sum of expectations from the direct and indirect light
- For direct light, predicted charge is given as an integral along the particle track length  $s$ :

$$\mu^{dir} = \Phi \int ds g(p, s, \cos \theta) \Omega(R) T(R) \epsilon(\eta)$$

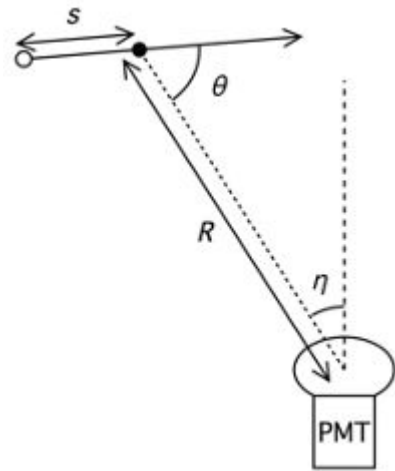
$\Phi$ : normalization factor

$g$ : Cherenkov emission profile  $\rightarrow$  using look-up table

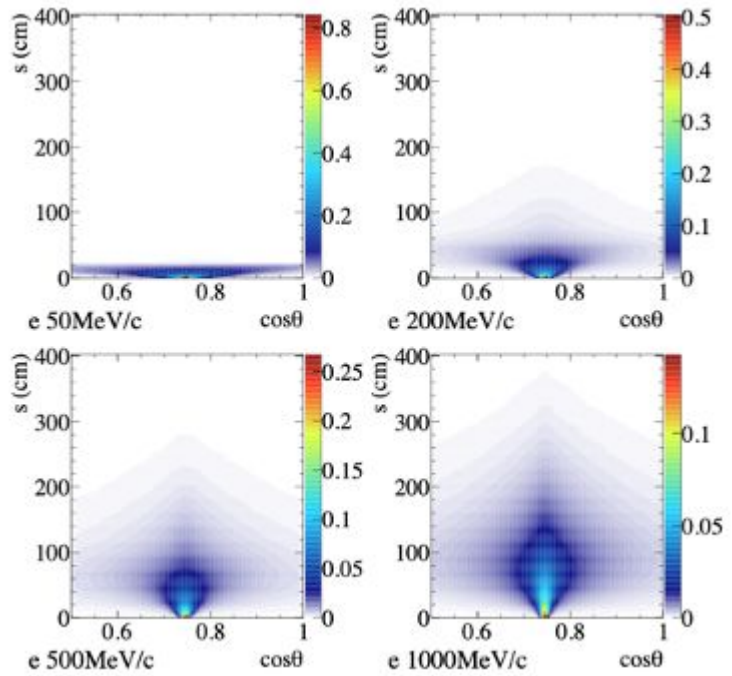
$\Omega$ : Solid angle of PMT

$T$ : attenuation of light

$\epsilon$ : PMT angular response  $\rightarrow$  using look-up table

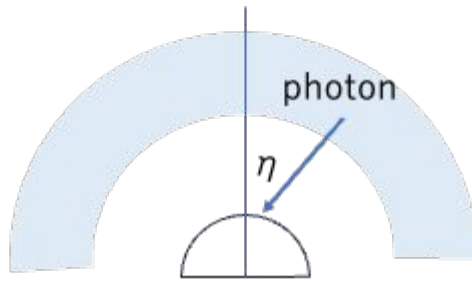


# Cherenkov emission profile

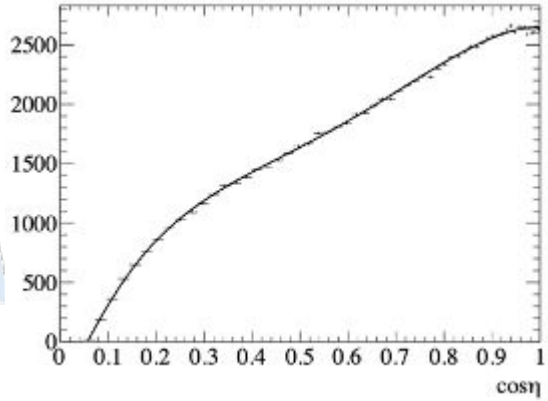


Simulate Cherenkov emission with several momentum  
→ apply polynomial fit and get table for  $s$ ,  $\cos$  and momentum

# PMT angular response



ex. PMT angular response in SK



Zenith angle distribution of hits by photons around a PMT

# Predicted charge by indirect photon

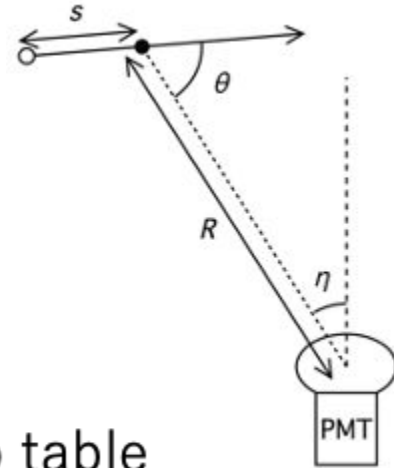
- The indirect photon includes the light scattered in water and detector component such as surface of PMTs.
- The predicted charge of indirect light is similar to the one of direct light:

$$\mu^{sct} = \Phi \int ds \frac{\rho(p, s)}{4\pi} A(s) \Omega(R) T(R) \epsilon(\eta)$$

$\rho/4\pi$ : integral of the Cherenkov emission profile  $g$

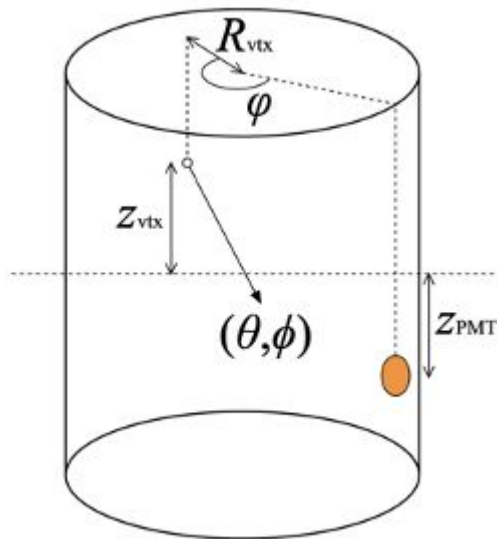
$$\rho(p, s) = \int d\Omega g(p, s, \cos \theta)$$

$A$ : scattering light distribution table  $\rightarrow$  using look-up table

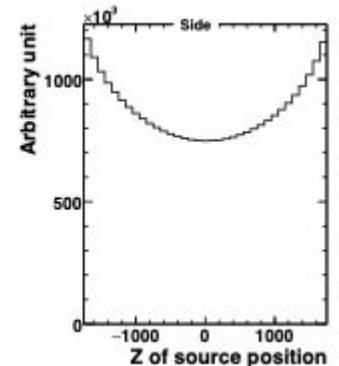
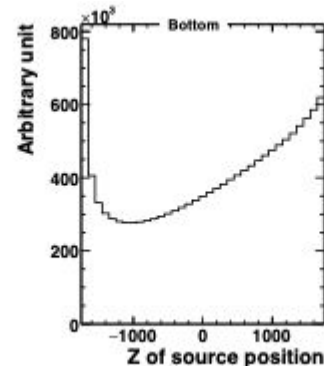
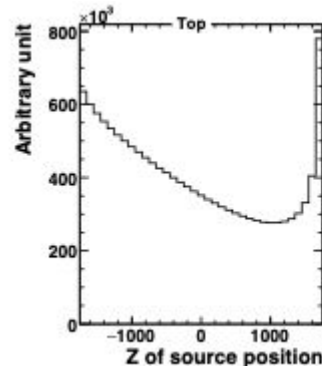


# Scattering light distribution table

- Scattering light distribution is created from  $10^9$  events (electron, 3MeV, uniform vertex and direction)
  - Fill 6-dimensional tables for top, bottom and barrel PMTs
- Among the tables, this requires the most events due to high dimension
  - The replacement by SIREN may contribute to computing resource and precision



ex. projected distribution to Z of source position in SK





# Functions depending on charge in likelihood

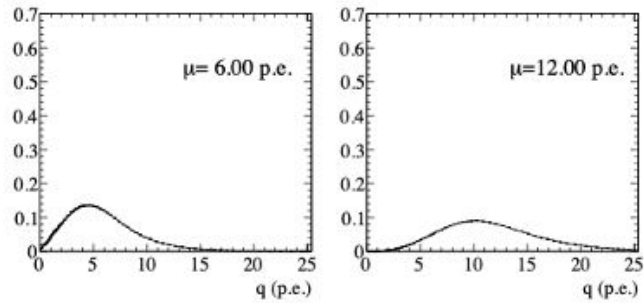
$$L(x) = \prod_j^{unhit\ PMTs} P(unhit_j|x) \prod_i^{hit\ PMTs} P(hit_i|x) f_q(q_i|x) f_t(t_i|x)$$

## Unhit probability with mean number of p.e.s :

$$P(unhit|x) = (1 + a_1 \mu + a_2 \mu^2 + a_3 \mu^3) e^{-\mu}$$

collection for events cannot cross PMT hit threshold  $\times$  Poisson with zero expectation

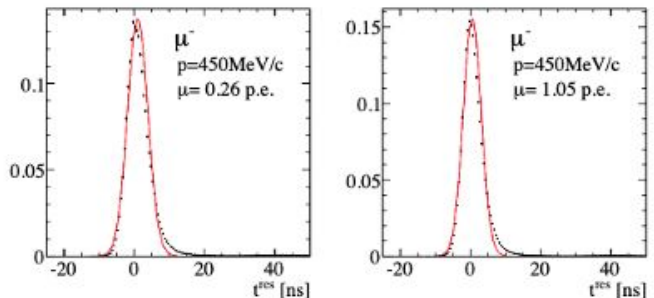
### Charge likelihood $f_q$



ex. 20-inch PMT in SK

- Charge distribution with predicted charge  $\mu$
- Look-up table obtained from simulation

### Time likelihood $f_t$

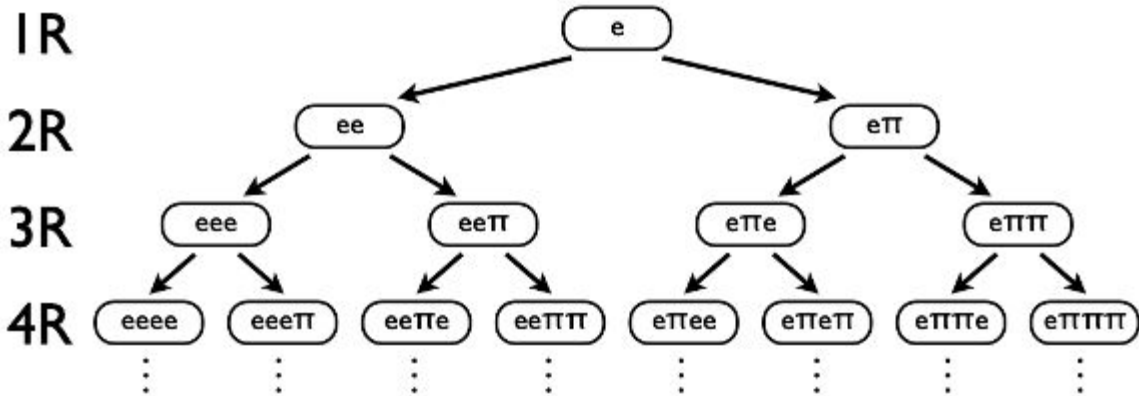


ex. residual time of direct light in SK

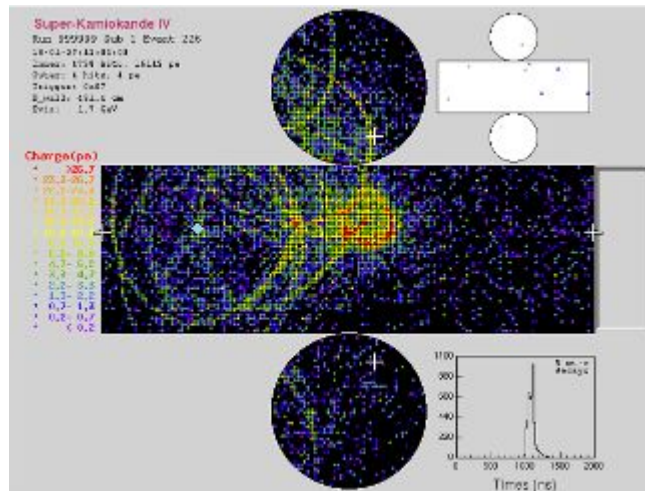
- Time distribution with predicted charge  $\mu$  and momentum

# Multi-ring fitter

- The algorithm searches the rings by sequentially increasing the number of rings (e or  $\pi$ )
- Check if likelihood is better than before the ring was added
- Since the computing time is  $2^N$ , this process is the most time consuming among the process



Example of multi-ring event display



# Outlook

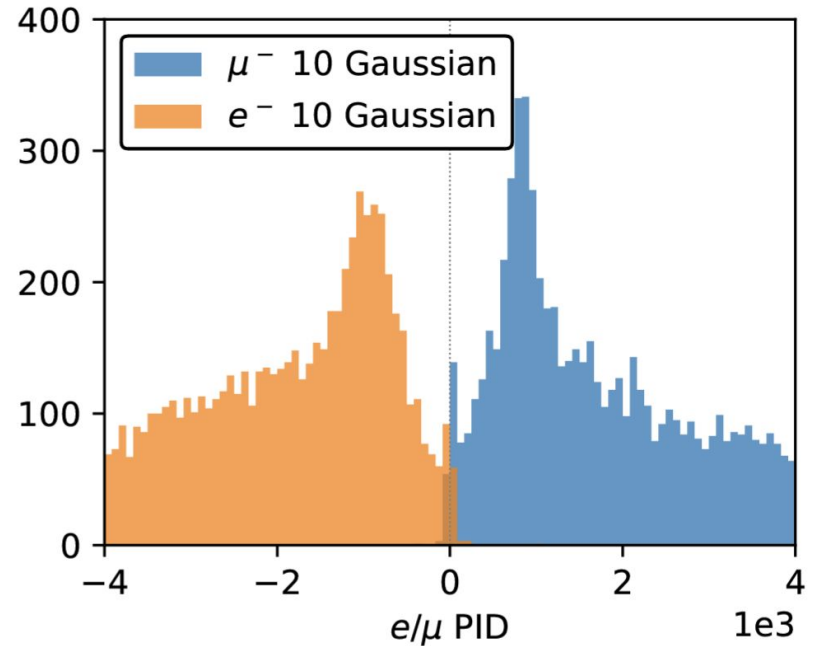
- Application to fiTQun:
  - Replace generation method of current tuning files
  - Directly produce predicted charge from particle track
- Since there are many times of predicted charge calculation in fiTQun, it may contribute to reducing total computing time
- Application to detector simulation:
  - E.g. Can the same SIREN for fiTQun indirect light table be used instead of G4 photon propagation?
    - Systematics (e.g. water parameters) directly tuned/optimized from calibration data
  - Include other parts of simulation, like QExCE of each PMT?

# Appendix

# NN-based Reconstruction

# A working example

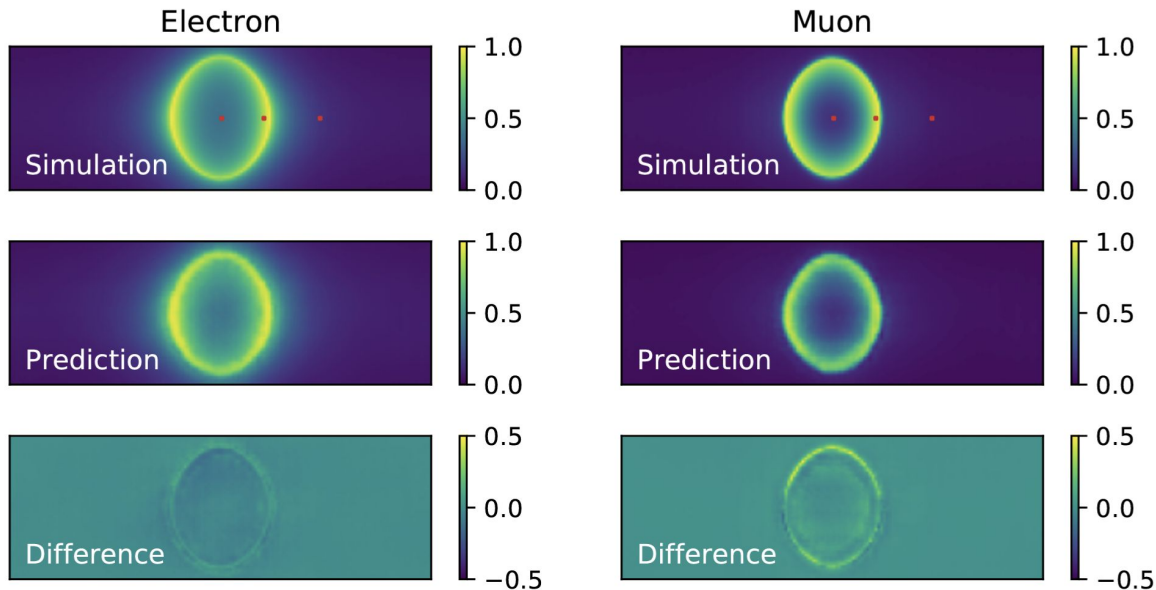
- A deep convolutional NN to generate WC detector responses to a particle of given particle type, energy, position, and direction.
- Loss designed based on the fitQun likelihood function on p.17, optimized by ADAM and can be trained on the “physics MC”.
- Enabled finer details in each individual photodetector responses by multi-gaussian distributions, and the correlation between charge and timing.



Demonstration of the PID likelihoods given by a trained CNN for single ring events uniformly generated inside the WC detector. Pile-up of events around the boundary comes from the events near detector walls.

# A working example

- In this example, the CNN-generated WC events show some extents of “smearing effect”, which might have be originated from the use of ReLU.



- To solve this “smearing effect”, the use of periodic activation functions, e.g. ideas from [SIREN](#) and [NeRF](#), is under study.