

k4Clue: Empowering Future Collider Experiments with CLUE

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Felice Pantaleo, Marco Rovere


Introduction

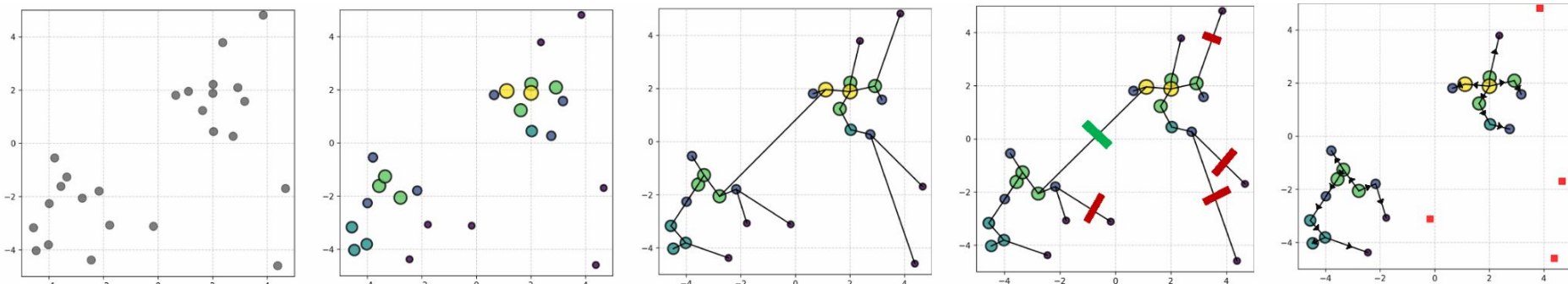


CLUstering of Energy

- CLUE (**CLU**stering of **E**nergy) is a fast density-based clustering algorithm for the next generation of sampling calorimeter with high granularity in HEP

 [doi: 10.3389/fdata.2020.591315](https://doi.org/10.3389/fdata.2020.591315)

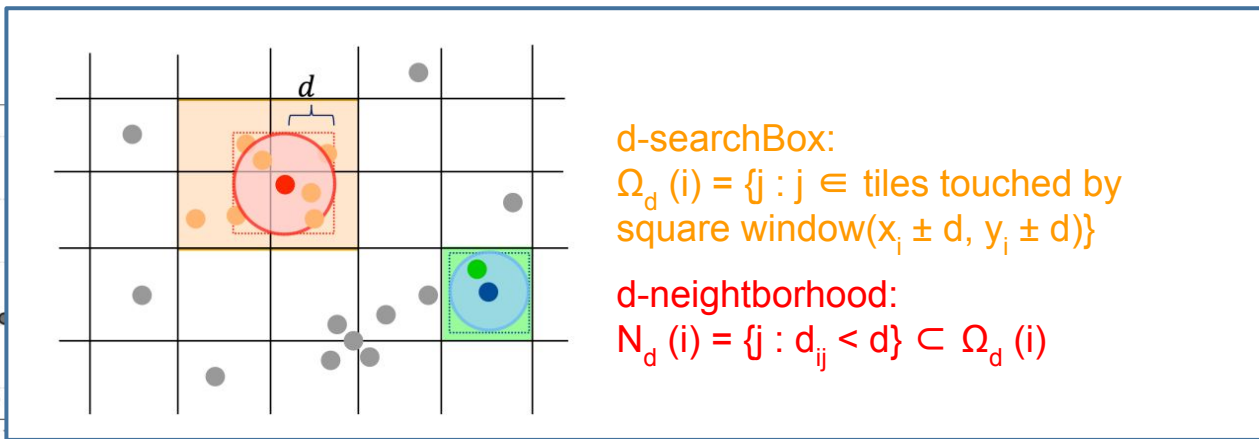
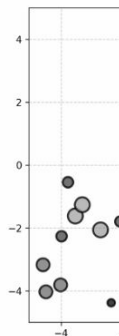
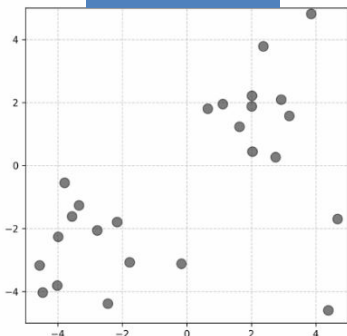
- It uses **energy density** - rather than individual cell energy - to establish **seeds, outliers, and followers** in 2D planes.
- **GPU-friendly**, i.e. suitable for the upcoming era of heterogeneous computing in HEP
- Standalone repo: 



Step 1: Building Data Structure

- Querying neighborhood is a frequent operation in density-based clustering → **fast!**
- Build **Fixed-Grid Spatial Index** for hits on each layer:
 - Each tile in the grid hosts indices of hits inside it and has a fixed length of memory to store the hosted indices. It is independent by the detector granularity.
- To find the neighborhood hits $N_d(i)$ of i -hit, we only need to loop over hits in $\Omega_d(i)$

build data structure



Step 2: Local energy density

- Calculate local energy density (ρ_i) in a distance (d_c)
 - Each hit j weighted by the deposited energy (E_j)
 - For each hit, calculate ρ_i

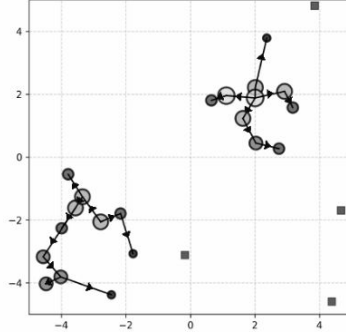
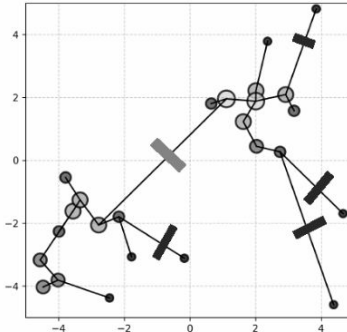
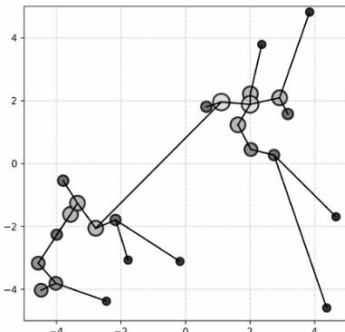
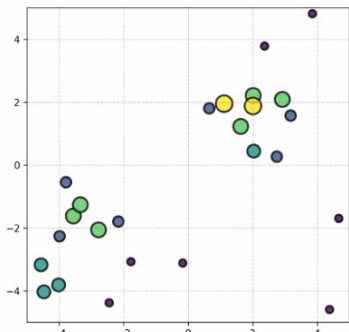
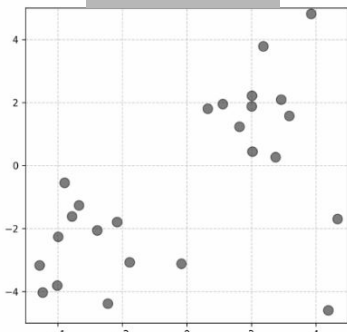
convolution kernel

$k = 0.5$

$$\rho_i = \sum_{j \in N_d(i)} E_j \times f(d_{ij}); f(d_{ij}) = \begin{cases} 1, & \text{if } i = j \\ k, & \text{if } 0 < d_{ij} \leq d_c \\ 0, & \text{if } d_{ij} > d_c \end{cases}$$

build data structure

density



Step 3: Find “closest higher hit”

- Calculate “Nearest-Higher” hit within $N_{dm}(i)$

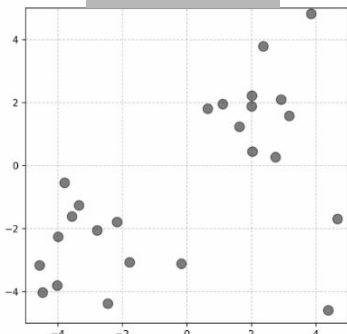
- Define $d_m = o_f * d_c$

- Find the closest hit with higher local energy density, nh_i

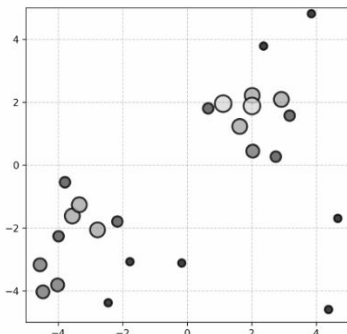
$$nh_i = \begin{cases} \operatorname{argmin}_{j \in \hat{N}_{dm}(i)} d_{ij}, & \text{if } |\hat{N}_{dm}| \neq 0, \hat{N}_{dm}(i) = \{j : j \in N_{dm}(i), \rho_j > \rho_i\} \\ -1, & \text{otherwise} \end{cases}$$

- Calculate the separation distance $\delta_i = \operatorname{dist}(i, nh_i)$

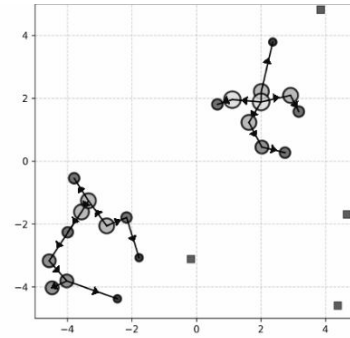
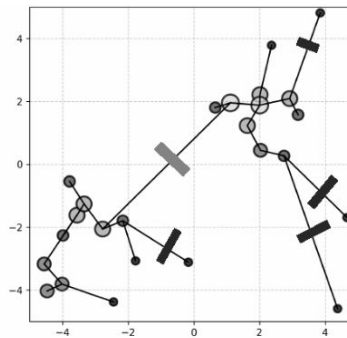
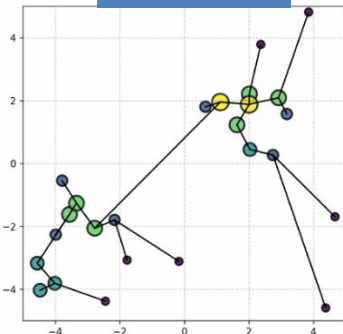
build data structure



density



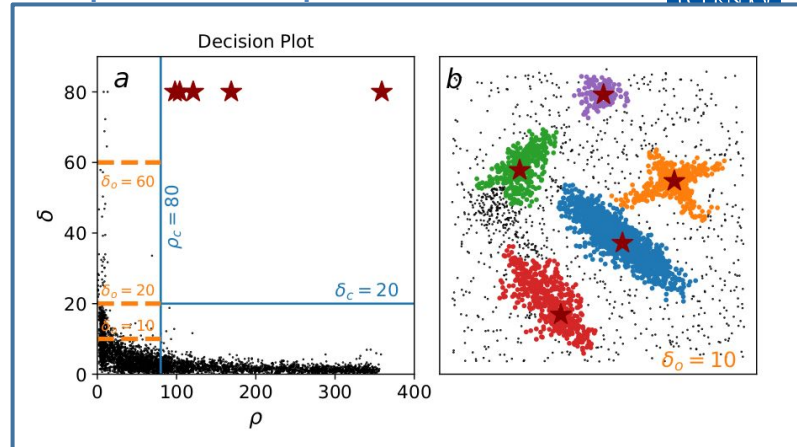
nearest higher



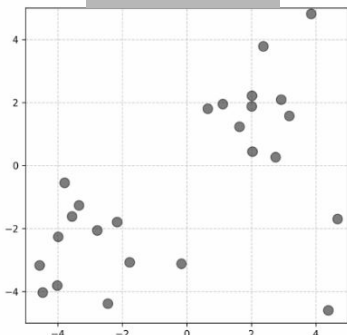
Step 4: Classify hits

- Promote as **seed** if $\rho_i > \rho_c$, $\delta_i > d_c$
- Demote as **outlier** if $\rho_i < \rho_c$, $\delta_i > o_f * d_c$
- Assign unique, progressive cluster ID to each cluster
 - **Followers** are defined and associated to their closest seed

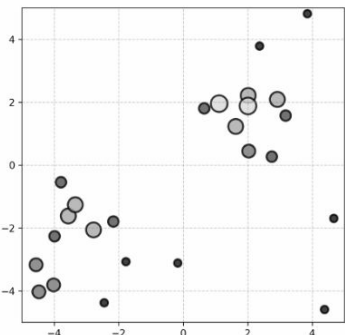
Example of decision plot



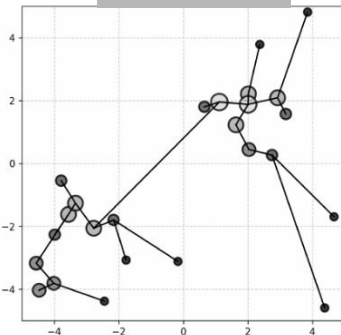
build data structure



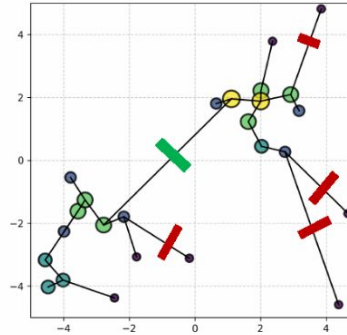
density



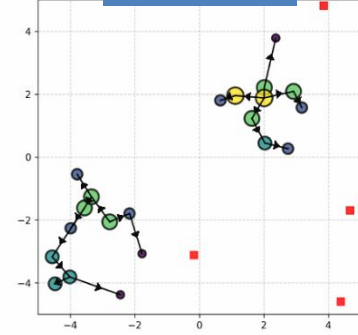
nearest higher



find seed



assign clusters



Clustering procedure recap

Input parameters:

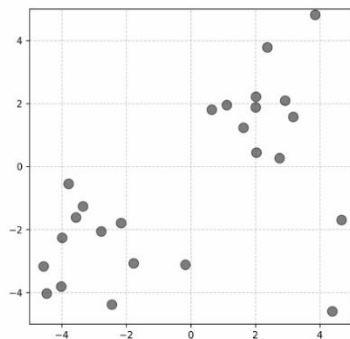
d_c : Critical Distance

o_f : Outlier Delta Factor

ρ_c : Minimum Local Density

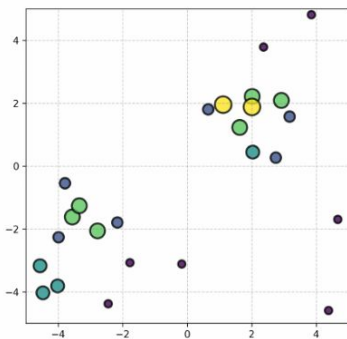
build data structure

Query the neighborhood of a point by looping over the points in N_c in the bins touched by the tiles intersected by d_c



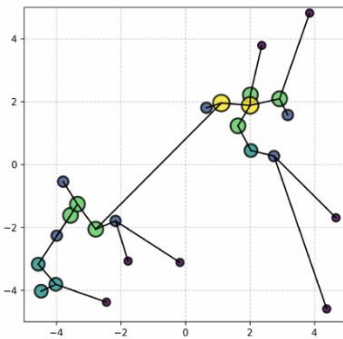
density

Hit position and energy used to calculate the hit's local energy density ρ_i and its distance δ_i to the nearest hit with higher local density



nearest higher

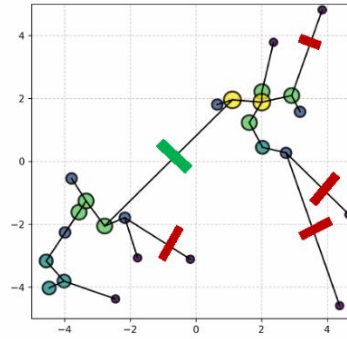
Define the nearest-higher of each hit as the hit with the local energy density higher than the hits itself and within a distance of $d_m = o_f \times d_c$



find seed

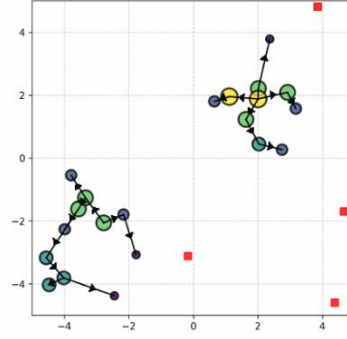
Use following criteria:

- seed: $\rho_i \geq \rho_c$ and $\delta_i \geq d_c$;
- outlier: $\rho_i < \rho_c$ and $\delta_i \geq (o_f \times d_c)$

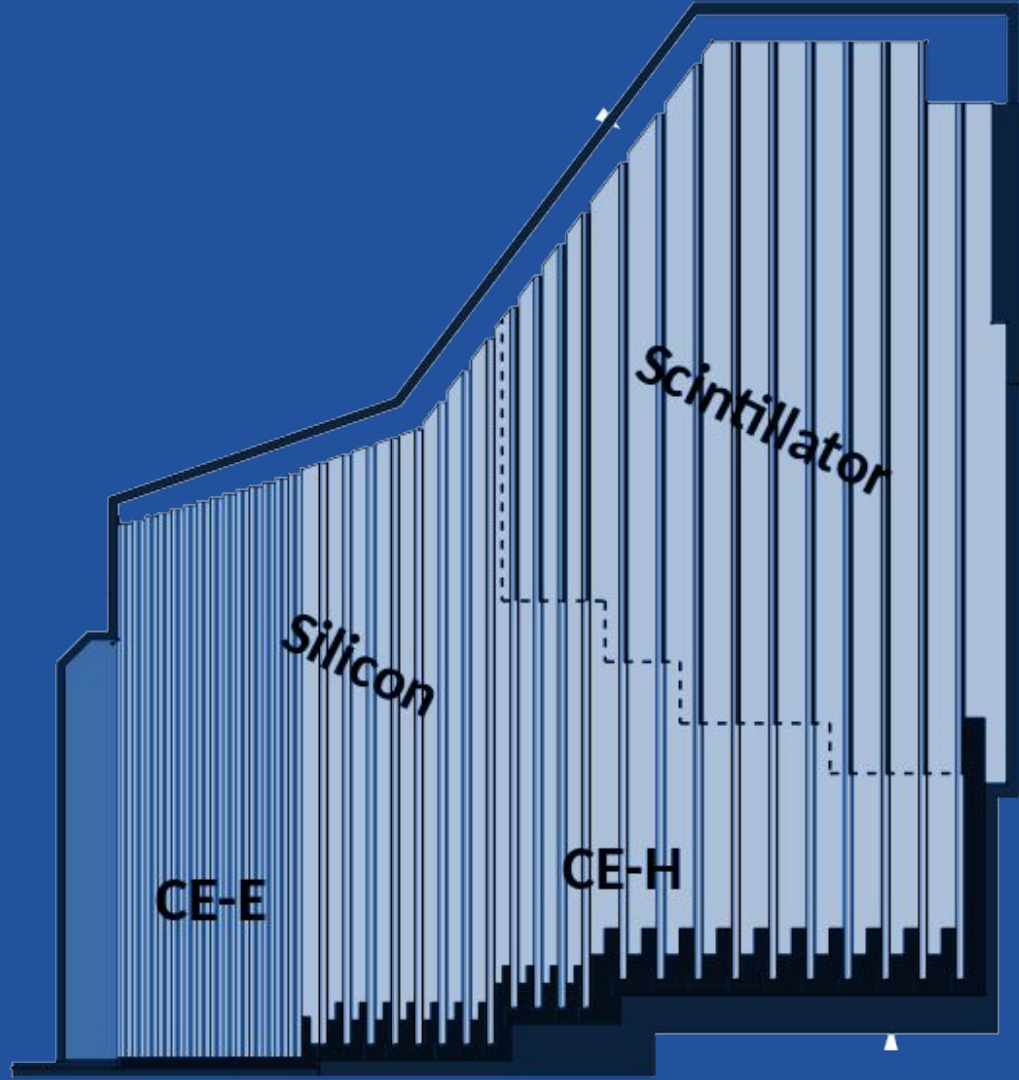


assign clusters

Register each remaining point as a follower to its nearest-higher



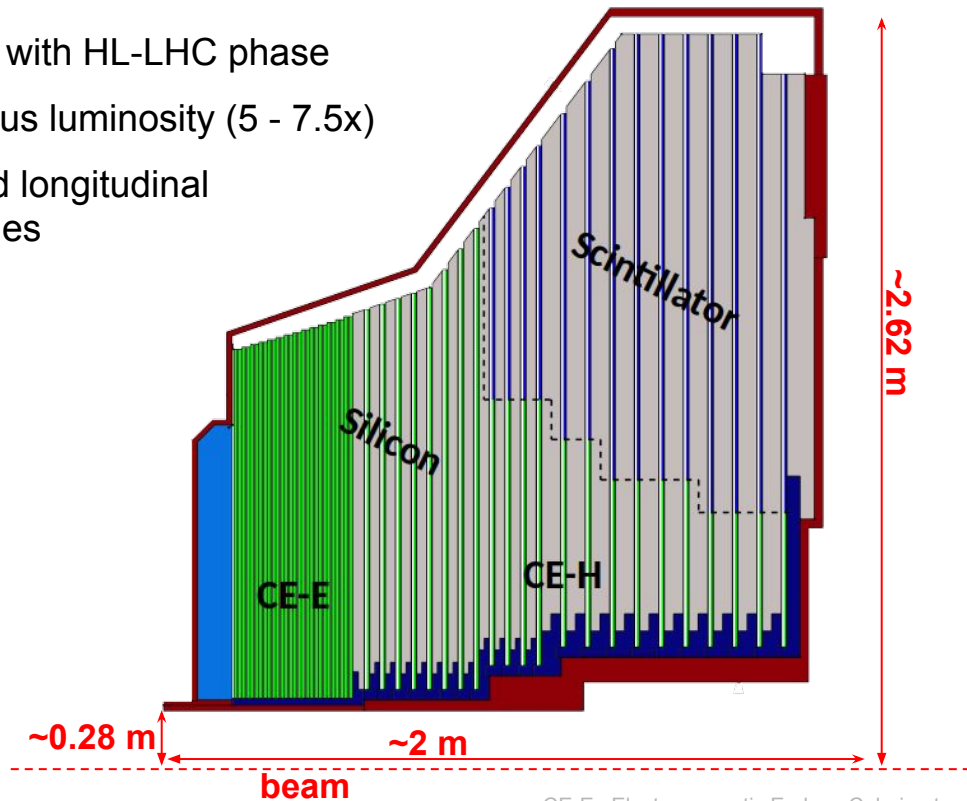
CLUE in the HGCAL reconstruction



- Phase-2 upgrade of CMS is needed to cope with HL-LHC phase
 - A significant increase in the instantaneous luminosity (5 - 7.5x)
- Imaging calorimeter with very fine lateral and longitudinal segmentation, and precision timing capabilities
 - Covering $1.5 < \eta < 3.0$

Both endcaps	Silicon	Scintillators
Area	~620 m ²	~400 m ²
Channel size	0.5 - 1 cm ²	4 - 30 cm ²
#Modules	~30'000	~4'000
#Channels	~6 M	240 k
Op. temp.	-30 °C	-30 °C

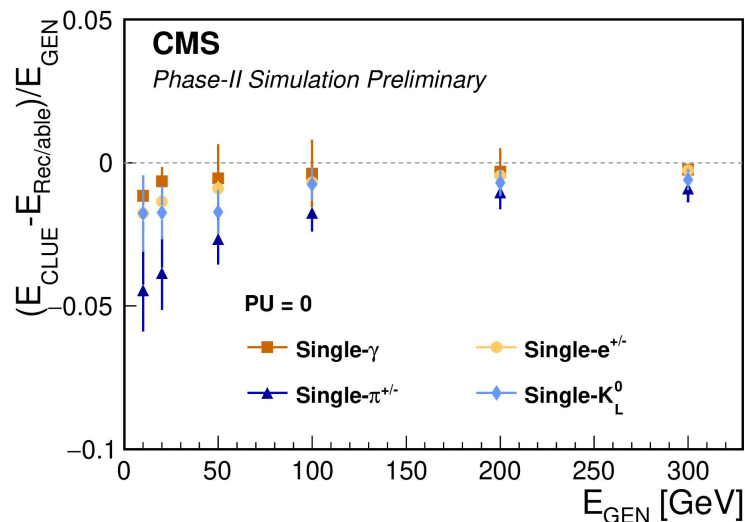
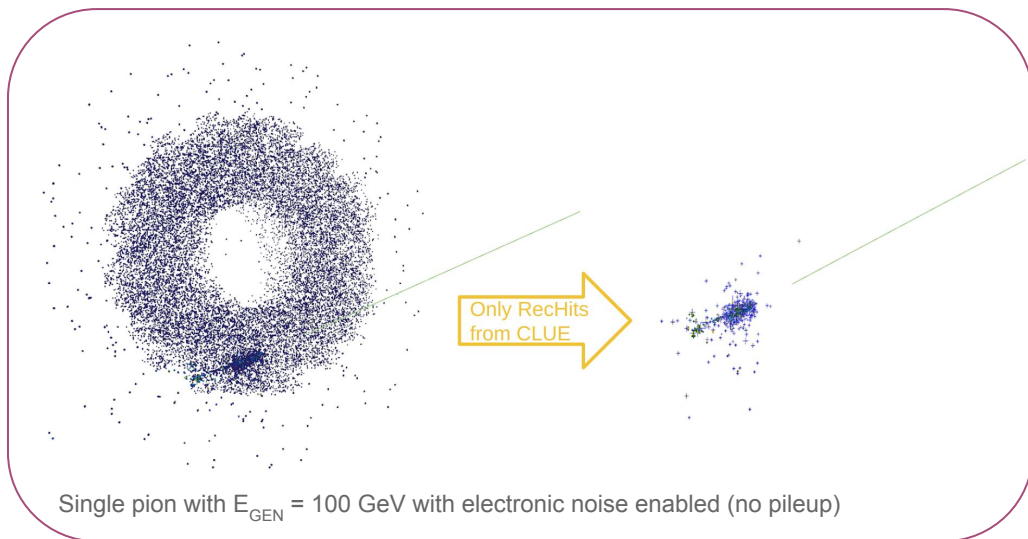
[Ref.](#)



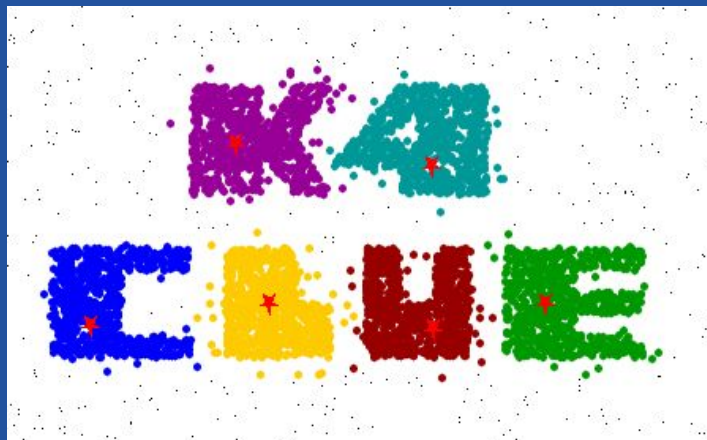
CE-E : Electromagnetic Endcap Calorimeter
 CE-H : Hadronic Endcap Calorimeter

HGCAL Software Reconstruction

- The HGCAL reconstruction framework is **TICL (The Iterative Clustering)**
- It starts by calibrating deposited energy in individual cells, also called RecHits → an order of **10^5 RecHits** in the HGCAL detector for events @ 200 pileup
- CLUE clusters the RecHits in the same layer to produce **Layer Clusters (LCs)**



The



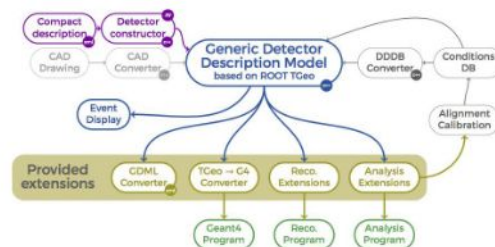
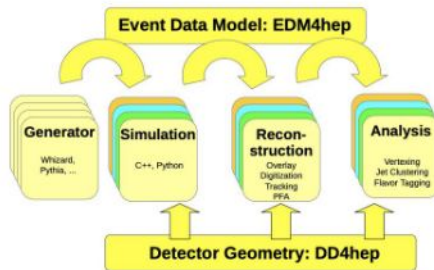
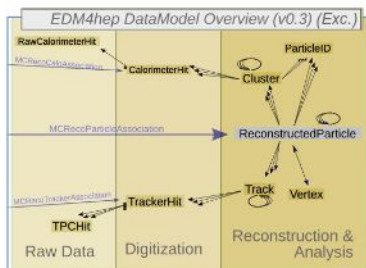
package

Key4hep in a nutshell

The common software vision: key4hep

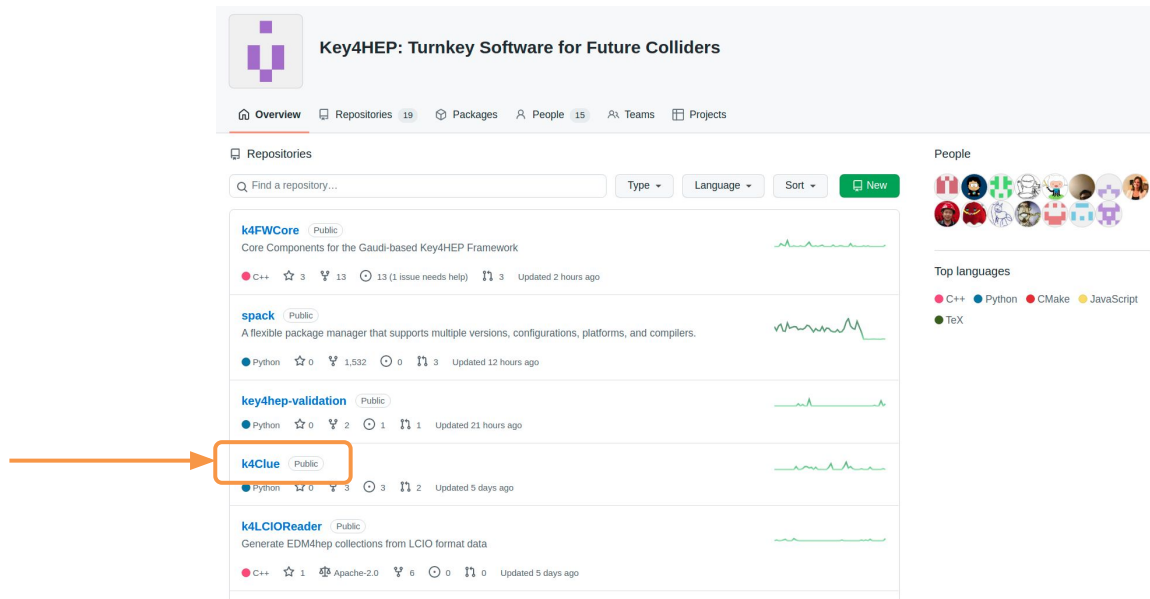
key4hep is a huge ecosystem of software packages adopted by all future collider projects, complete workflow from generator to analysis

- Event data model: EDM4HEP for exchange among framework components
 - Podio as underlying tool, for different collision environments
 - Including truth information
- Data processing framework: Gaudi
- Geometry description: DD4hep, ability to include CAD files
- Package manager: [Spack](https://spack.io/): `source /cvmfs/sw.hsf.org/key4hep/setup.sh`



Integrating CLUE in Key4hep

- **k4Clue v01-00** (doi: [10.5281/zenodo.7851995](https://doi.org/10.5281/zenodo.7851995))
 - It's adapted to the common event data model, **EDM4hep**
 - It includes a wrapper class to run in the **Gaudi** software framework
 - It's included in the new **Key4hep** releases managed by Spack



Key4HEP: Turnkey Software for Future Colliders

Overview Repositories 19 Packages People 15 Teams Projects

Repositories

Find a repository... Type Language Sort New

k4FWCore Public
Core Components for the Gaudi-based Key4HEP Framework
C++ 3 13 (1 issue needs help) Updated 2 hours ago

spack Public
A flexible package manager that supports multiple versions, configurations, platforms, and compilers.
Python 0 1,532 0 3 Updated 12 hours ago

key4hep-validation Public
Python 0 2 1 1 Updated 21 hours ago

k4Clue Public
Python 0 3 0 2 Updated 5 days ago

k4LCIOReader Public
Generate EDM4hep collections from LCIO format data
C++ 1 Apache-2.0 6 0 0 Updated 5 days ago

People

Top languages

C++ Python CMake JavaScript TeX

Additional features w.r.t. [kalos/Clue](#)

- **Cluster hits in the entire 4π detector region**

- Definition of the tessellated space (`LayerTile`) in the standalone version defines coordinates and searches only in the transverse plane
- Modified basic structure of the `LayerTile` and the search algorithm to allow for the definition of a cylindrical surface

$$x \rightarrow r\Phi \qquad y \rightarrow z$$

- **Template CLUE algorithm classes**

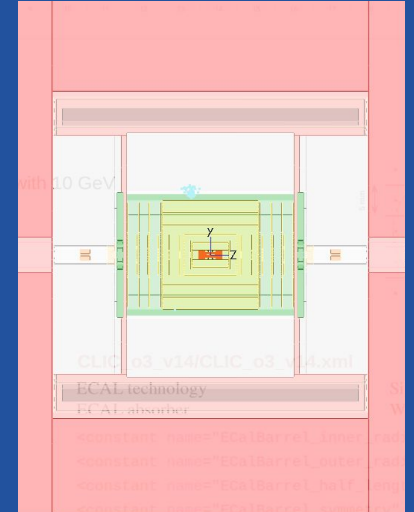
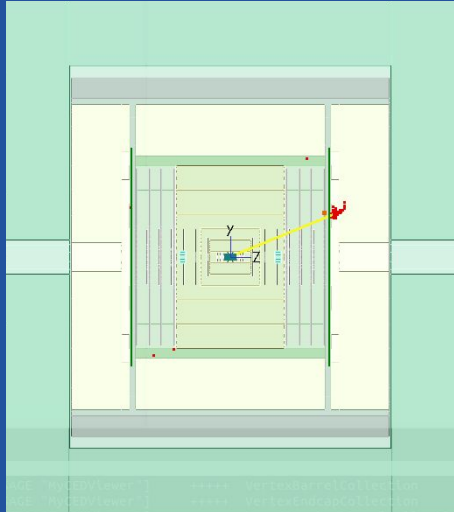
- To allow the possibility of defining several different calorimeter layouts
- A dedicated documentation page in the package ([include/readme.md](#)) allows the user to follow a simple but detailed step-by-step procedure to introduce and test the preferred layout.

- **GitHub CI & EDM4hep Validation**

- `edm4hep:CLUECalorimeterHit : CalorimeterHit` class with specific methods related to the CLUE algorithm

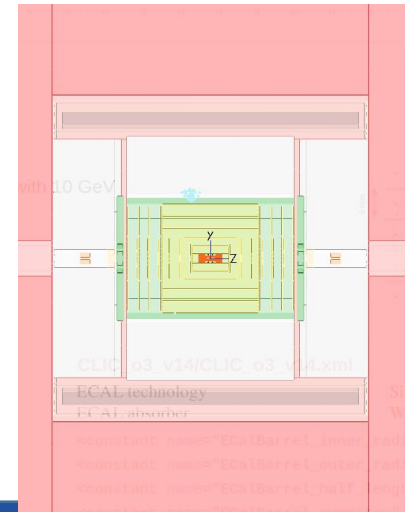
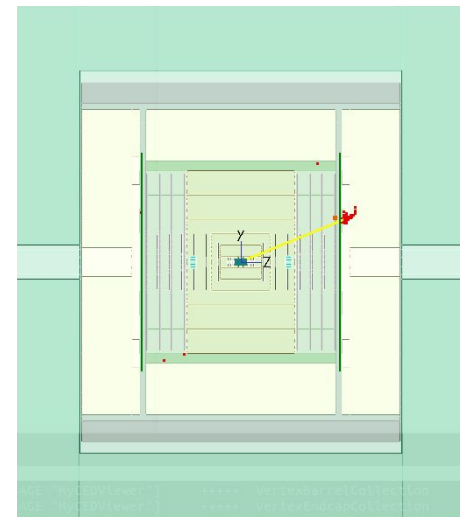
Performance evaluation

- CLD & CLICdet -



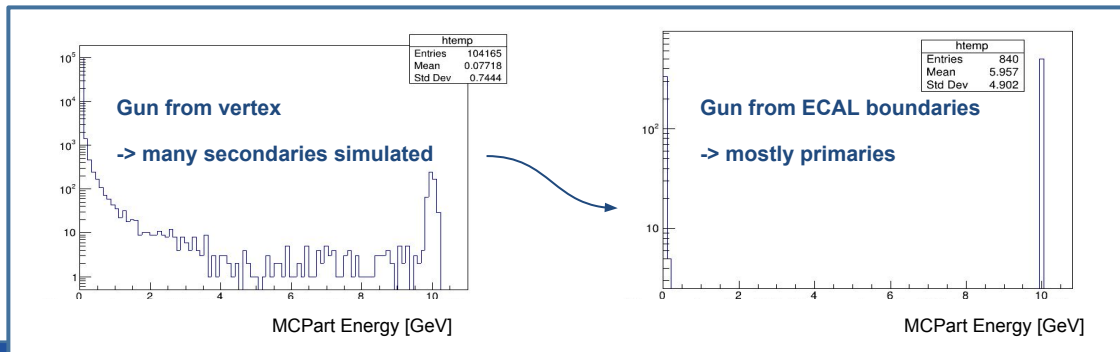
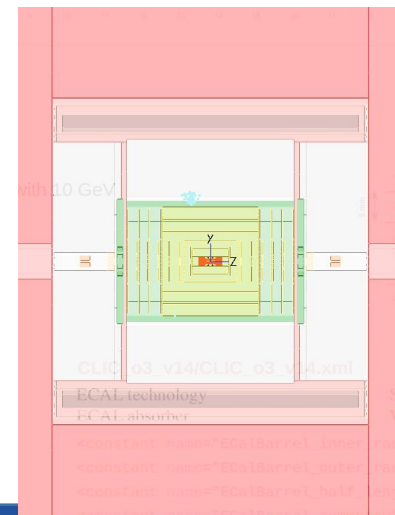
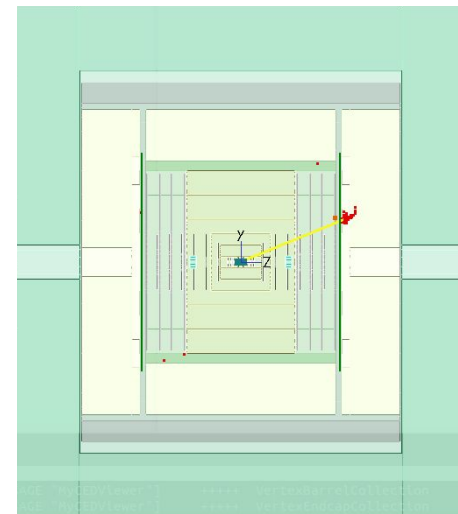
ECAL of CLICdet & CLD

- 40 layers of $5 \times 5 \text{ mm}^2$ Silicon cells & W
- The main difference between the two calorimeters lies in the layout parameters → To compensate for a lower detector solenoid field, the **CLD design** starts from a larger radius both in the barrel and in the endcap region w.r.t. **CLICdet**.
 - Further details in backup



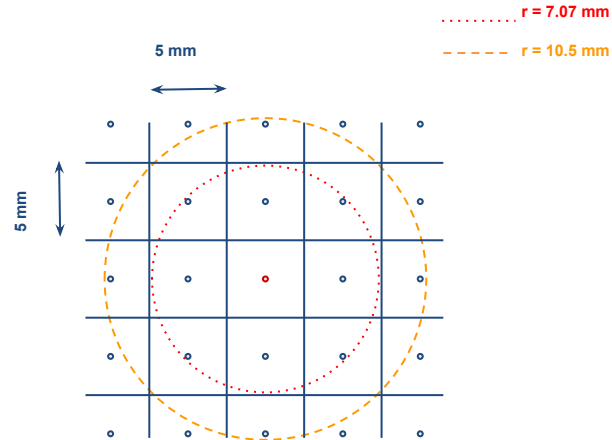
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 - Further details in backup
- 500 events of single gamma at 10 GeV generated perpendicular to the surface with [Geant4 General Particle Source](#)
 - Main reason: no conversion in the tracker volume

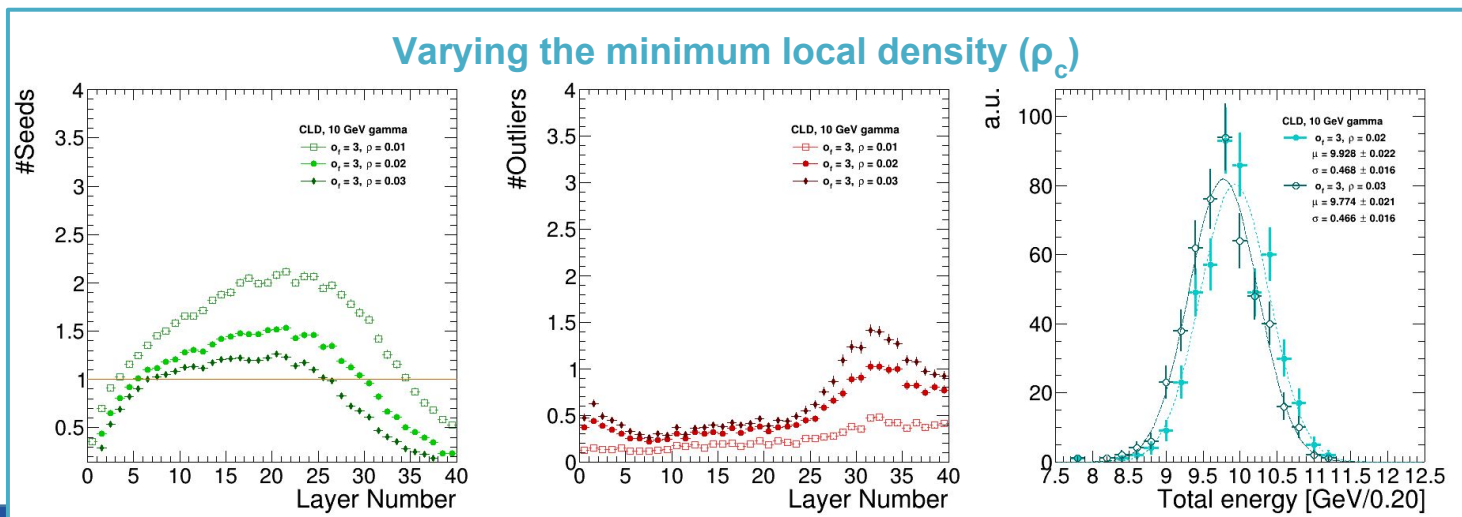
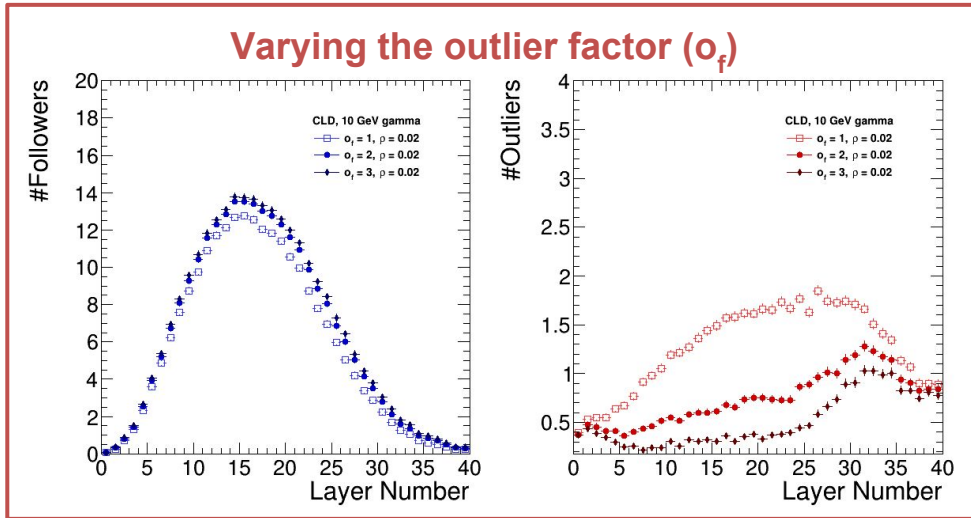


Parameters tuning

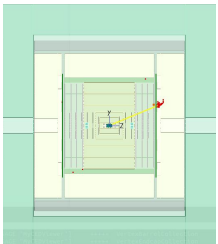
- Input parameters tuned for CLD
- Same ones tested also for CLICdet (**similar geometry, same granularity**)
- Critical Distance (d_c) is established by geometry granularity to contain (minimum) the close neighbors cells:
 - $d_c = 15$ mm



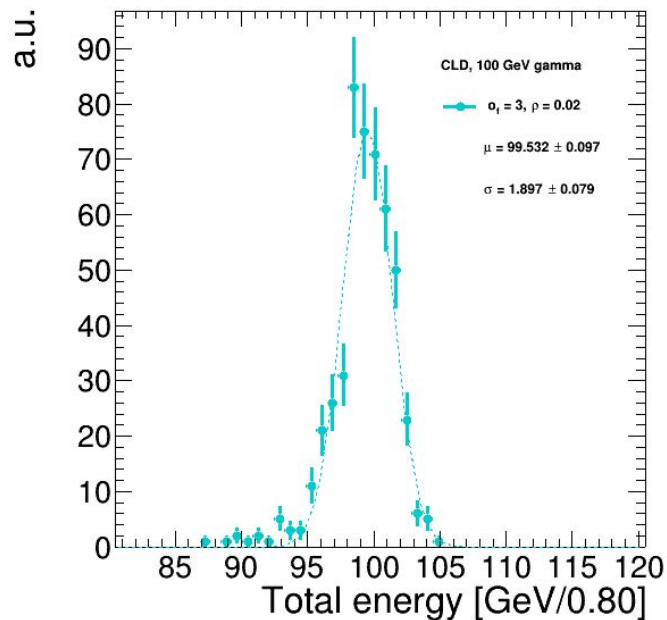
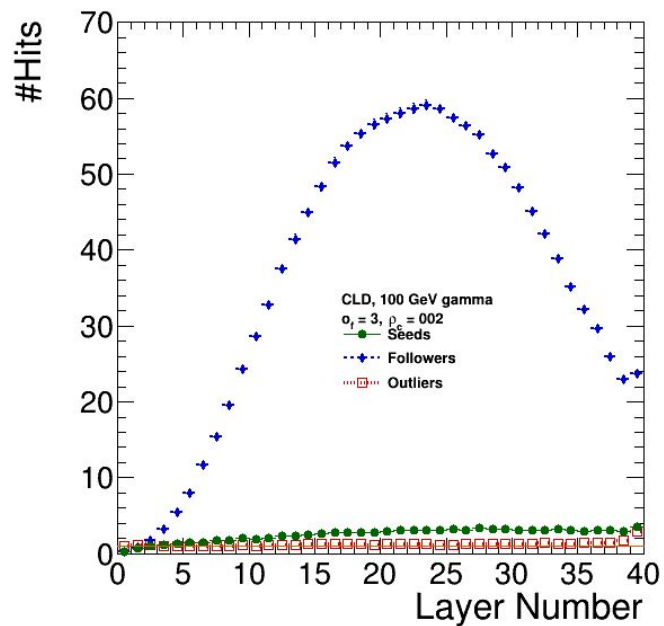
Parameters tuning



Higher energies

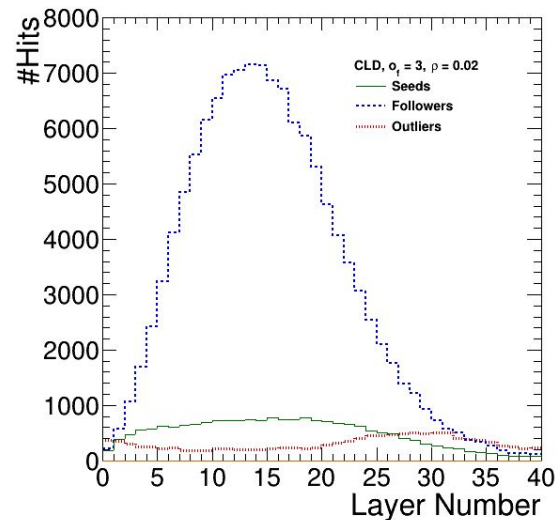
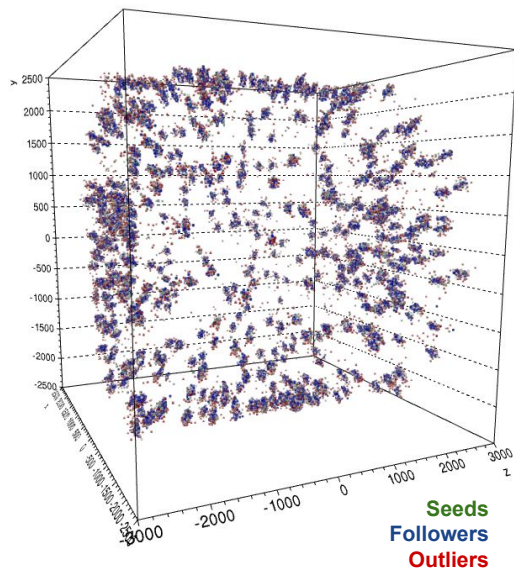
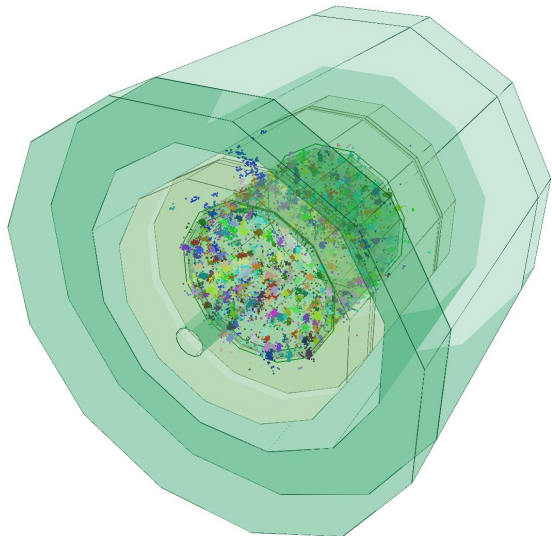


- 500 events with single gamma (from ECAL surface) at **100 GeV**
- $d_c = 15.00$, $\rho_c = 0.02$, $\sigma_f = 3.0$

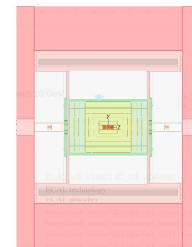


Multiple gamma event

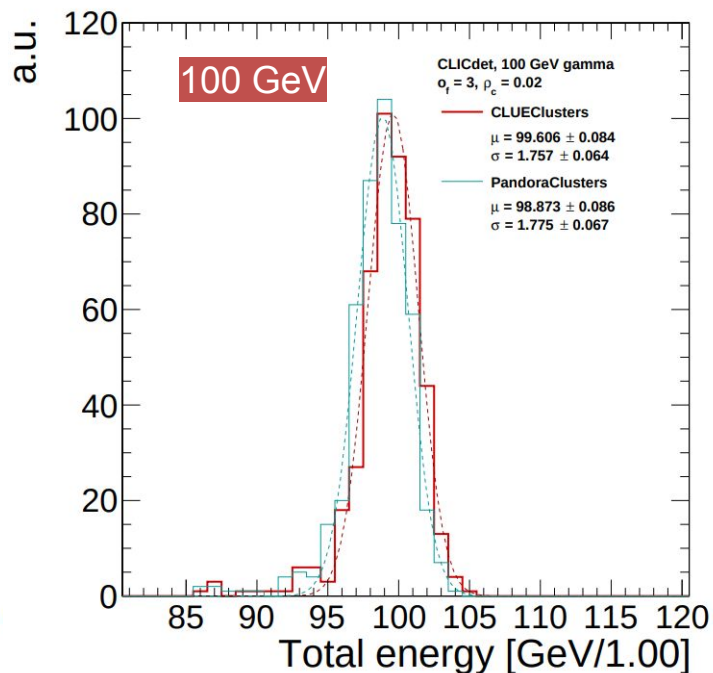
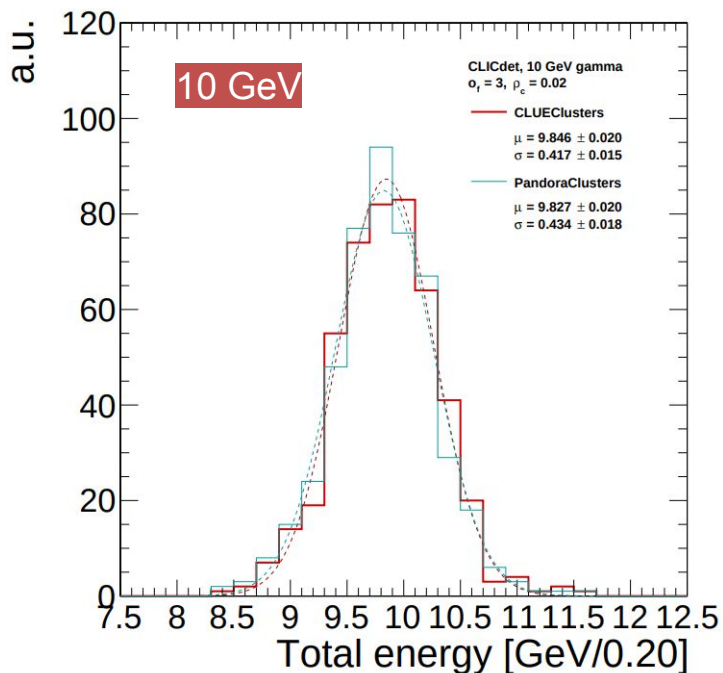
- Produced with normal gun, i.e. particles generated from vertex
- 1 event with 500 single gammas each produced with 10 GeV
Only simulated calorimeter hits are shown



CLICdet results

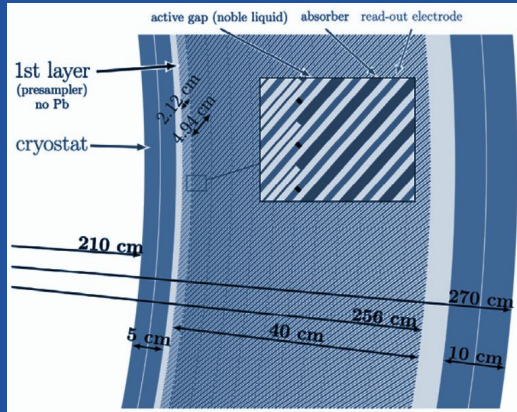


- Using same input parameters selected for CLD



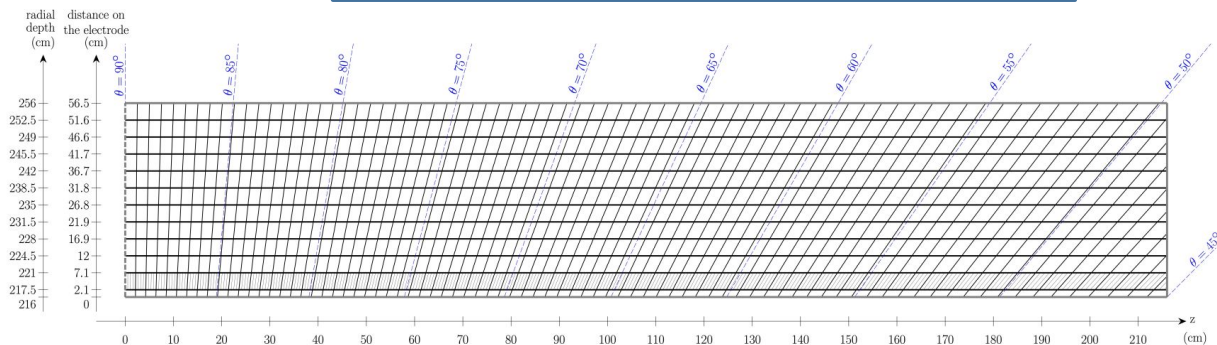
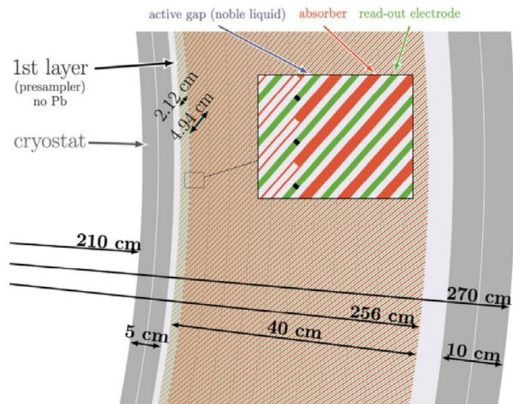
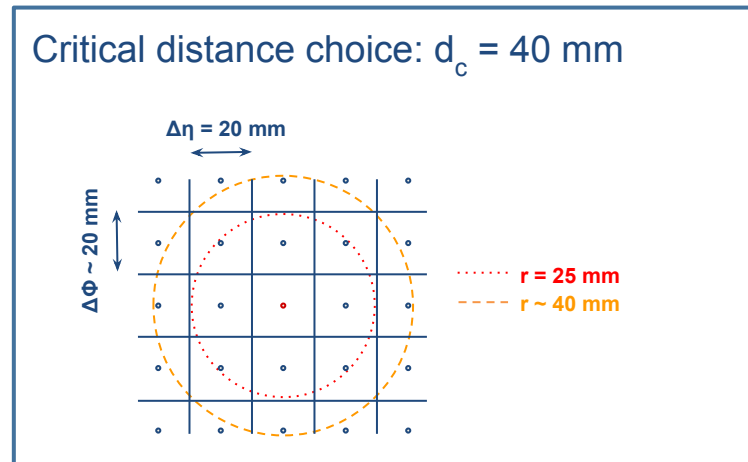
Comparison with **Pandora Clusters** not completely equitable comparison (it includes a dedicated calibration procedure), but comparable results in terms of energy linearity and resolution

Performance evaluation - Noble Liquid Calo -



Noble Liquid ECAL for FCC-ee

- 12 layers, only barrel considered
 - cell size in Φ : 17.9 mm - 20.7 mm
 - cell size in η : ~ 20 mm
- Sample (if not stated otherwise):
 - 500 single gamma at 10 GeV
 - $\theta_{[\text{min}, \text{max}]} = [50, 130]$



Parameters tuning

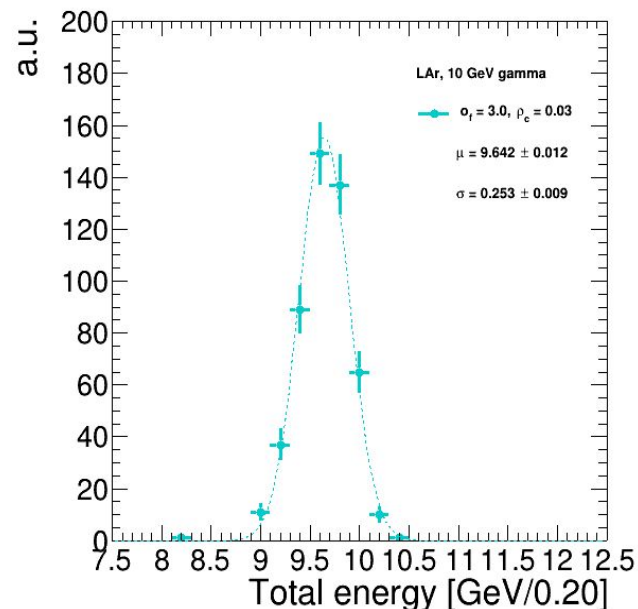
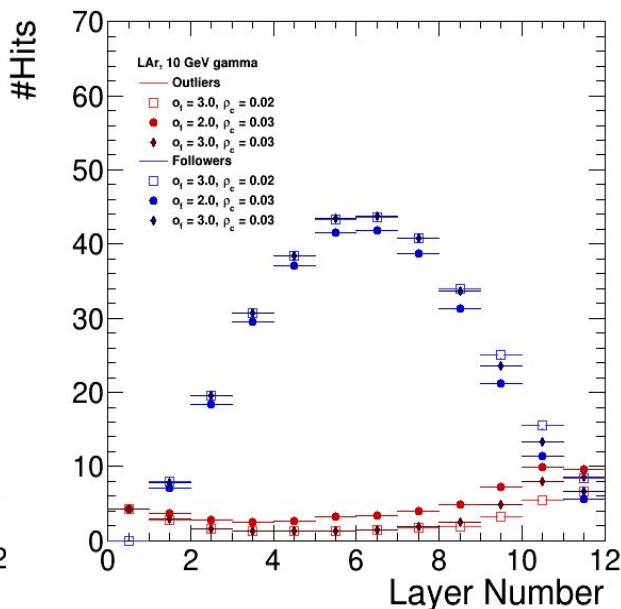
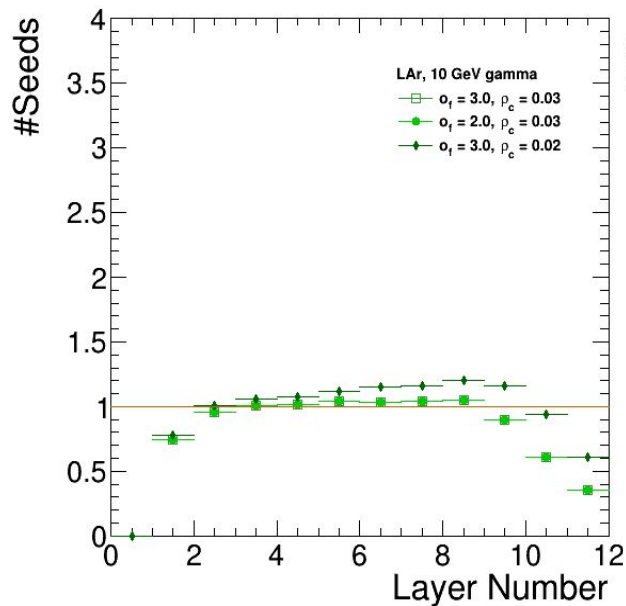
- 500 events with single gamma (from vertex) at **10 GeV**
- $d_c = 40.00$, $\rho_c = 0.03$, $\sigma_f = 3.0$

Input parameters:

d_c : Critical Distance

σ_f : Outlier Delta Factor

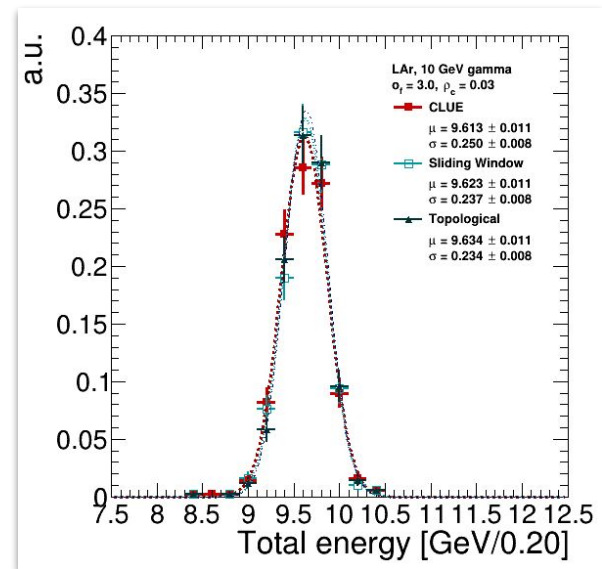
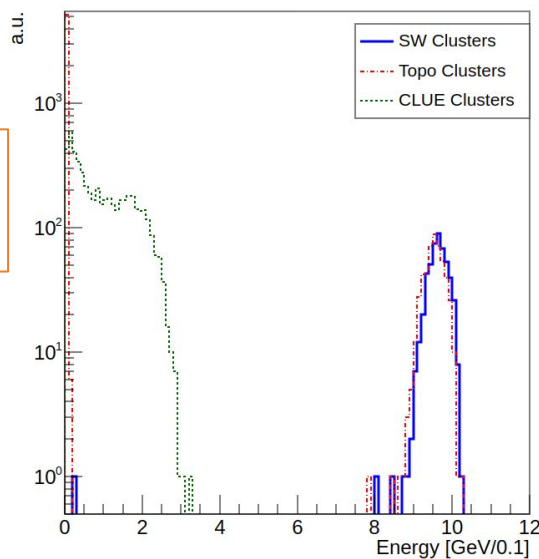
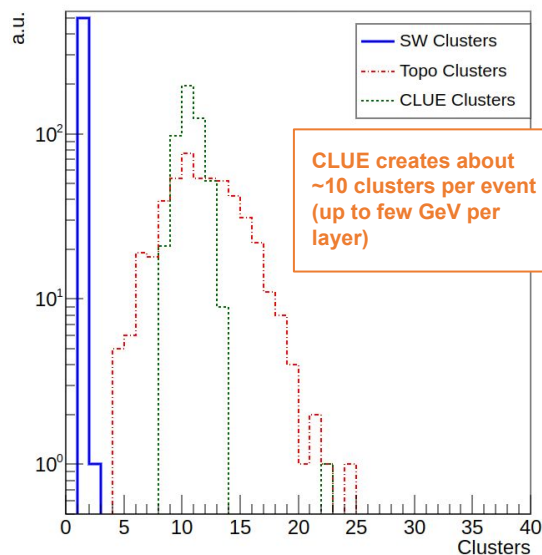
ρ_c : Minimum Local Density



Comparison with other cluster algorithms

[Calorimeters for the FCC-hh](#), Dec 2019

- **Sliding window:** It considers the calorimeter as a two-dimensional grid in η - ϕ space, neglecting the longitudinal segmentation of the calorimeter.
- **Topological clustering:** It starts with a seed cell and then adds topologically connected calorimeter cells



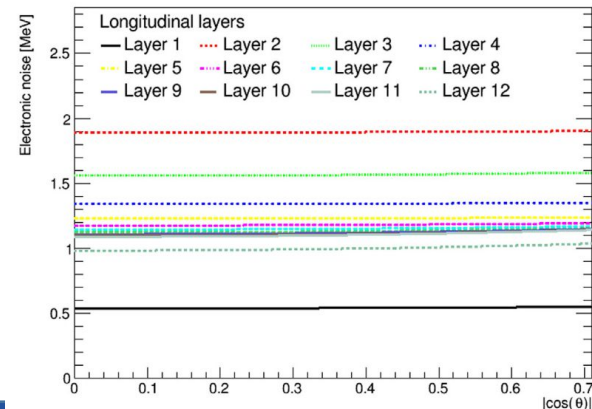
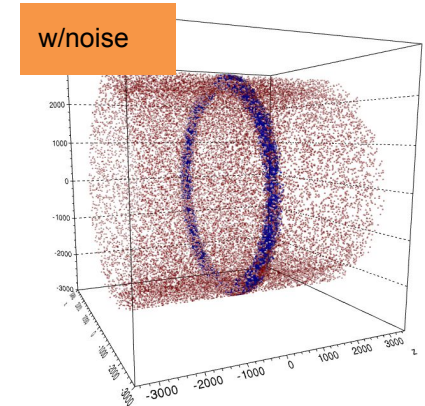
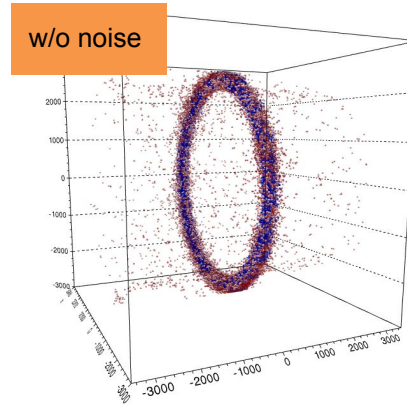
Noise in Liquid Argon Calorimeter

Signal produced only with $\theta \sim 90.25^\circ$

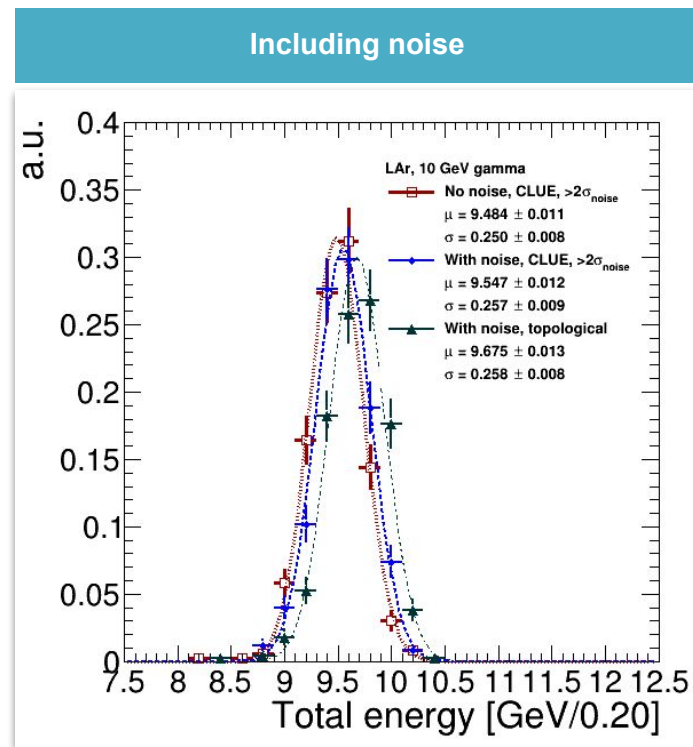
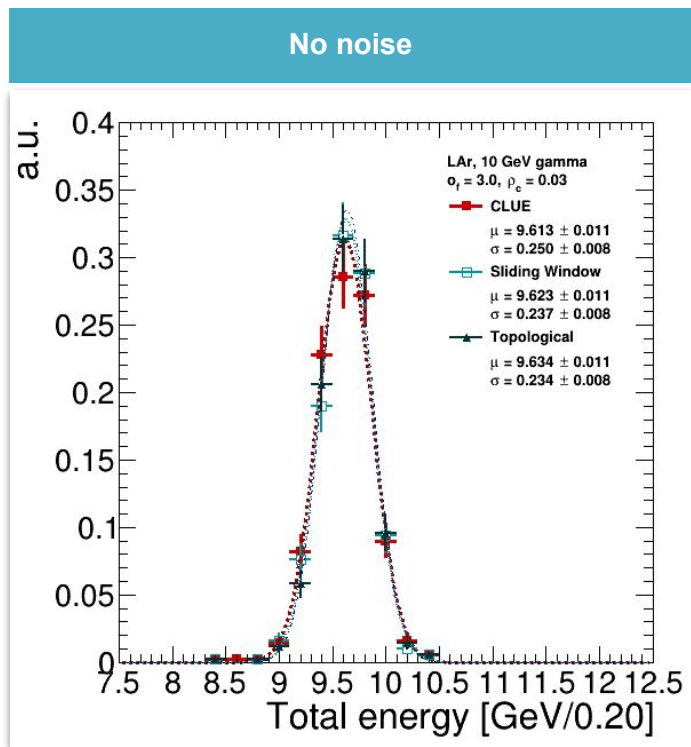
- High level of noise in the detector
- In the topoclustering, there is no filter directly at the beginning for the noise, but this is done using cuts in the algorithm itself
- The main observable is the cell significance ξ_{cell} which is defined as the absolute value of the ratio of the cell signal to the expected noise in this cell

$$\xi_{\text{cell}} = \left| \frac{E_{\text{cell}}}{\sigma_{\text{cell}}^{\text{noise}}} \right|$$

- CLUE hits w/noise **selected with filter of $> 2\sigma_{\text{noise}}$**

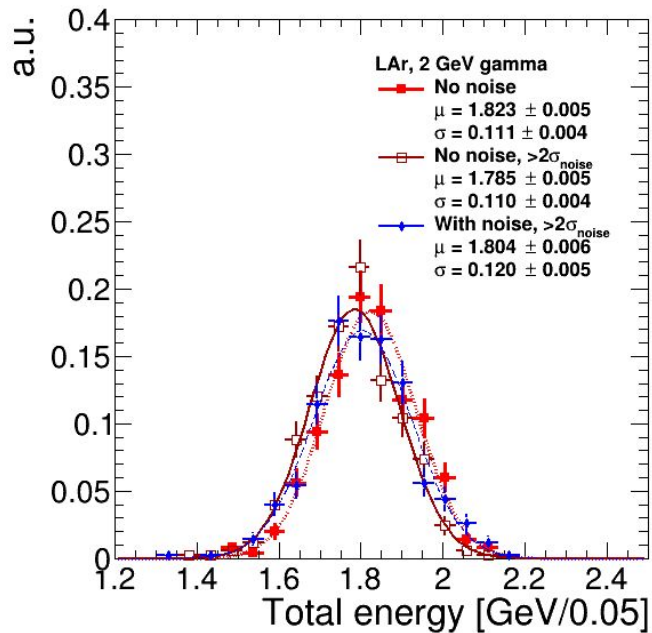
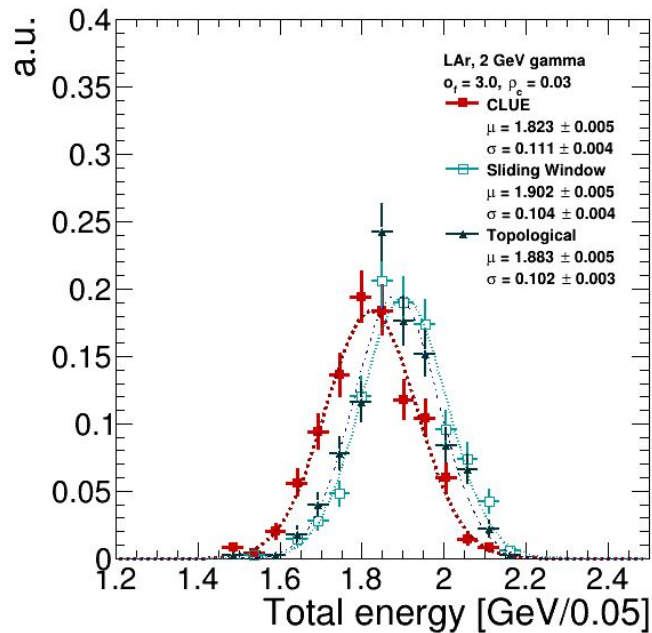


Comparison with other cluster algorithms

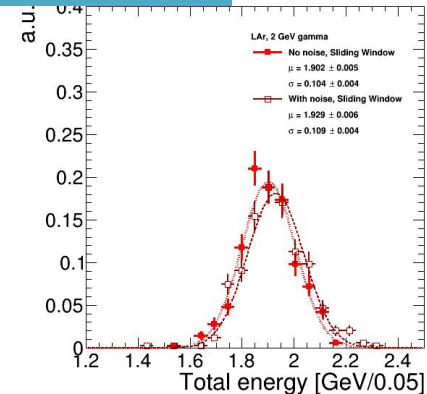


Low(er) energy

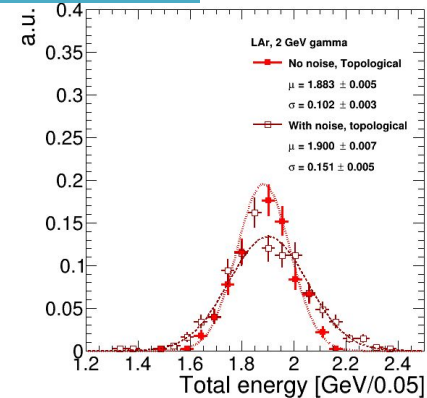
- 500 events with single gamma (from vertex) at **2 GeV**
Motivated by flavor physics searches at Z peak



Sliding Window
cluster energy > 1 GeV



Topological



Conclusions & Outlook

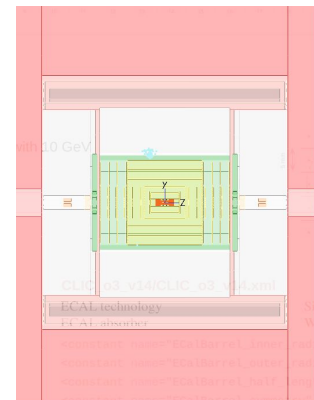
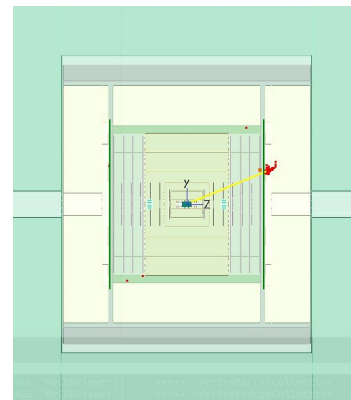
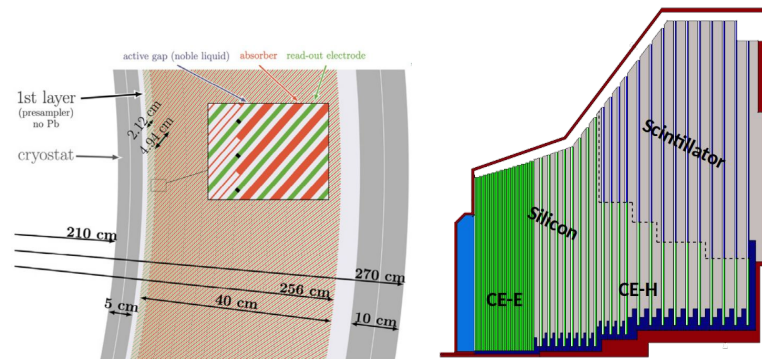


Conclusions

- k4Clue package ([v01-00](#)) has improved upon the standalone CLUE
 - Run on the full detector (barrel & endcap)
 - Adapted for different types of calorimeters
- Analysis on three different future calorimeters has demonstrated the good performance for single gamma events
 - Good performance even in the presence of noise
 - Compared favorably to other baseline algorithms

This work highlights the adaptability and versatility of the CLUE algorithm for a wide range of experiments and detectors, as well as its potential for future high-energy physics experiments beyond CMS

- Improvements from k4clue also under discussion to use the developments also in CMS (Phase-2 barrel region)



Conclusions

- Final article summarizing k4clue and its performance for future collider detectors almost ready
 - Computing time under study
- This research was supported by the CERN Strategic R&D Programme on Technologies for Future Experiments
- Special thanks go to the Key4hep team and the FCC-ee liquid calorimeter software experts for the support



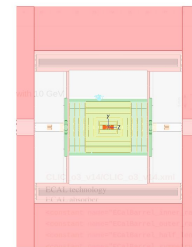


Backup

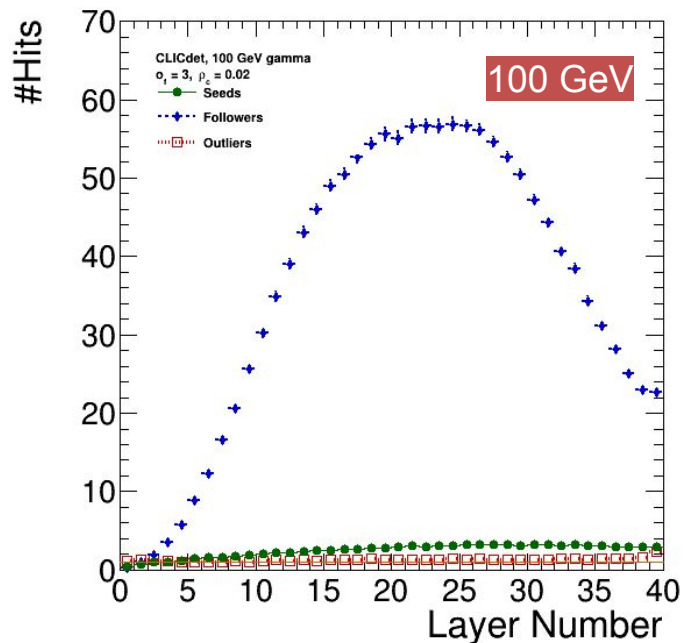
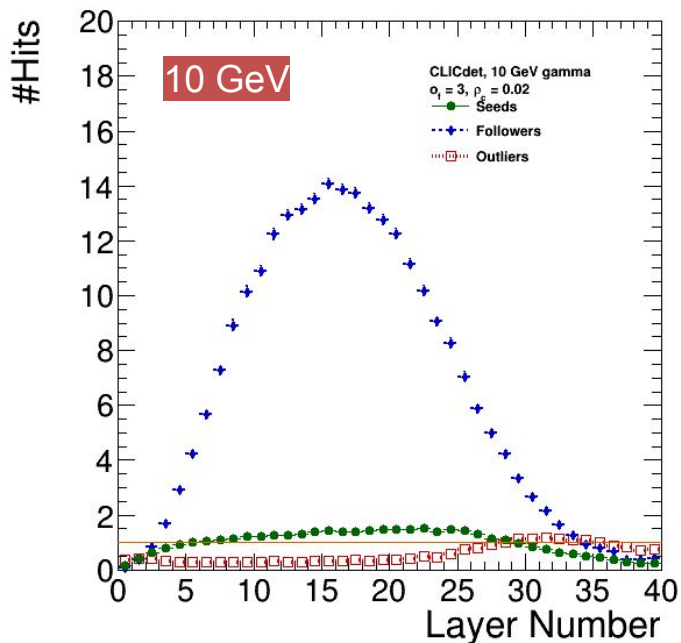
Integrating CLUE in Key4hep

- **GitHub CI** to ensure that the modifications or additions to the software do not break the clusterization process
 - In the latest release was modified to focus on C++ code and `EDM4hep` data
 - Test on both current `key4hep` release and nightlies
- **Validation**
 - `edm4hep:CLUECalorimeterHit`
 - `CalorimeterHit` class with specific methods related to the CLUE algorithm
 - `CLUEHistograms` class to produce ntuples

CLICdet results



- Using same input parameters selected for CLD

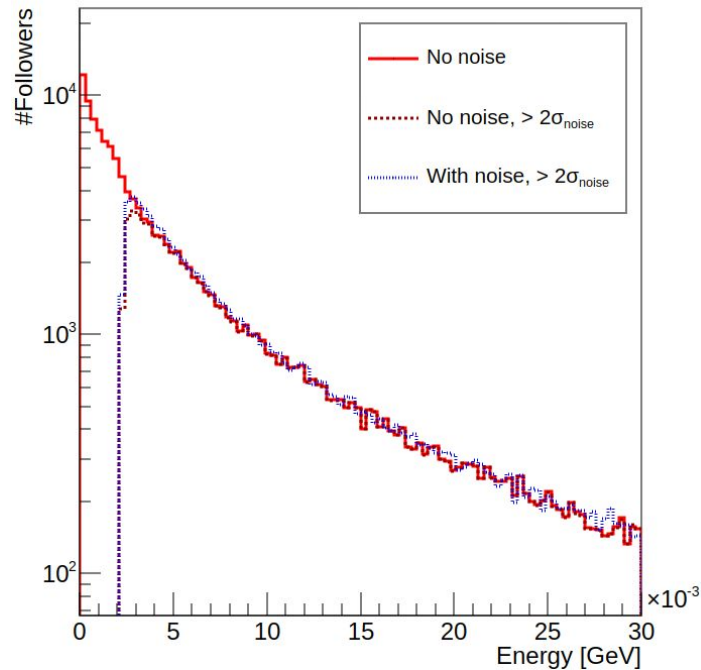
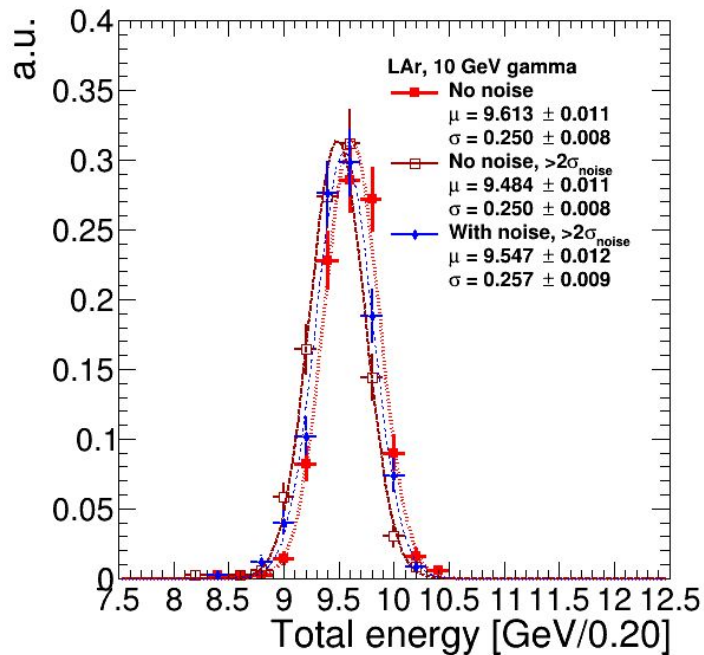


Comparison with **Pandora Clusters** not completely equitable comparison (it includes a dedicated calibration procedure), but comparable results in terms of energy linearity and resolution

Noble Liquid Calo

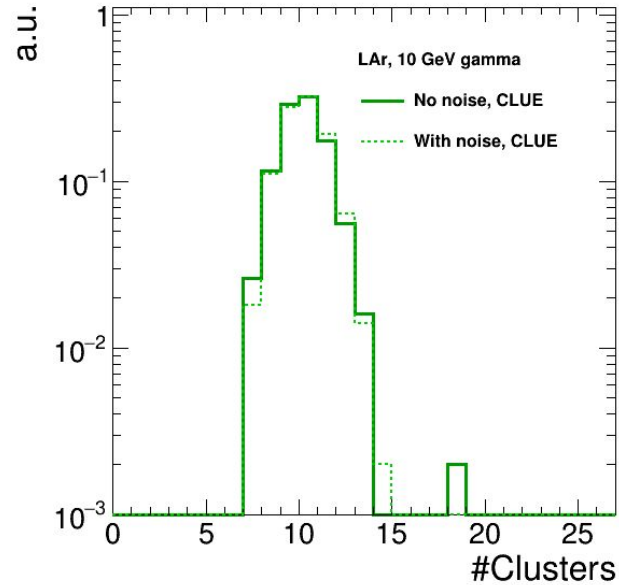
Pre-filtering

- CLUE hits w/noise selected with filter of $> 2\sigma_{\text{noise}}$

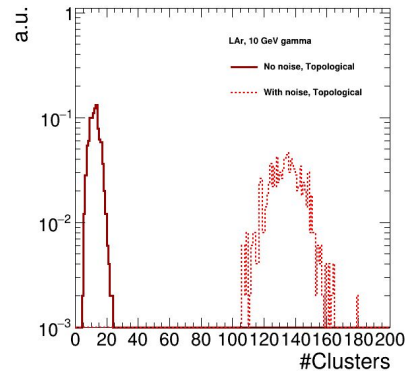
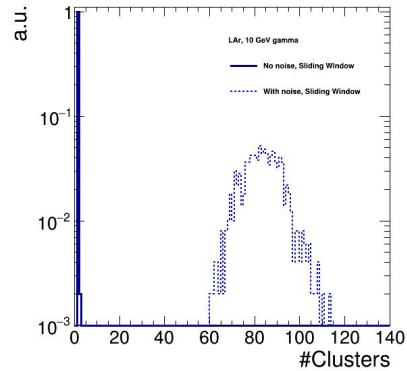


Noble Liquid Calo

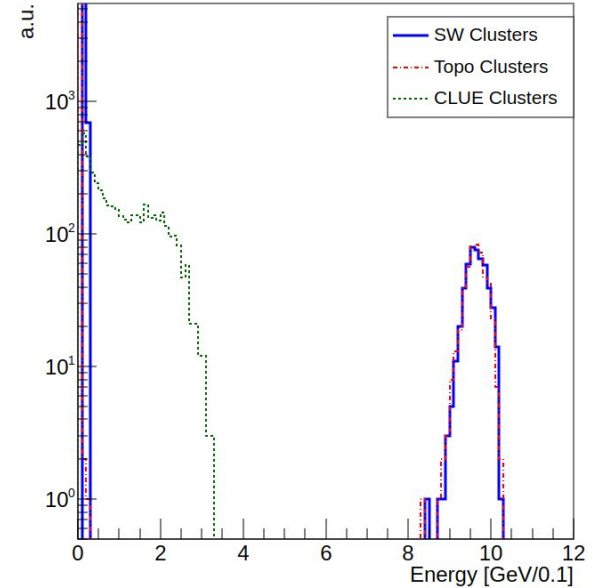
Comparison with other cluster algorithms



No significant effect on CLUE clusters - about ~10 per event (one per layer)



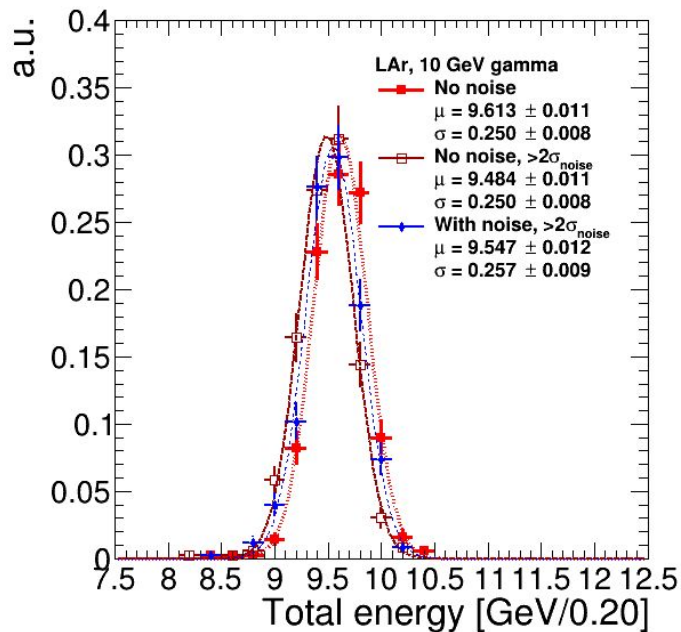
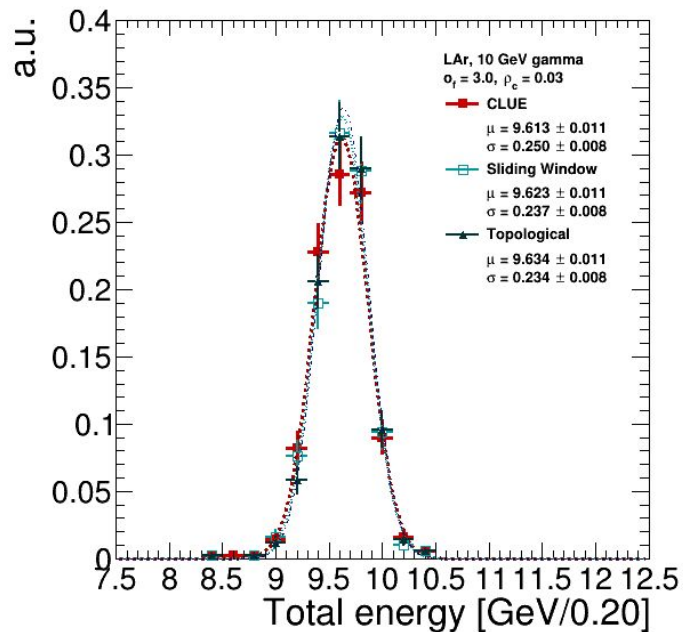
w/noise



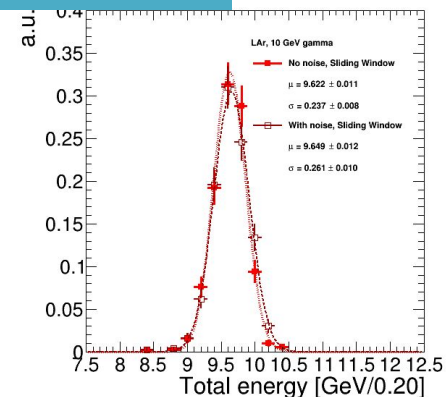
More than one SW and Topo cluster per event, but most of them with low energy

Noble Liquid Calo

Summary for 10 GeV gammas



Sliding Window
cluster energy > 1GeV



Topological

