

# Physics Case for Precision Measurements at a Higgs Factory

Nathaniel  
Craig

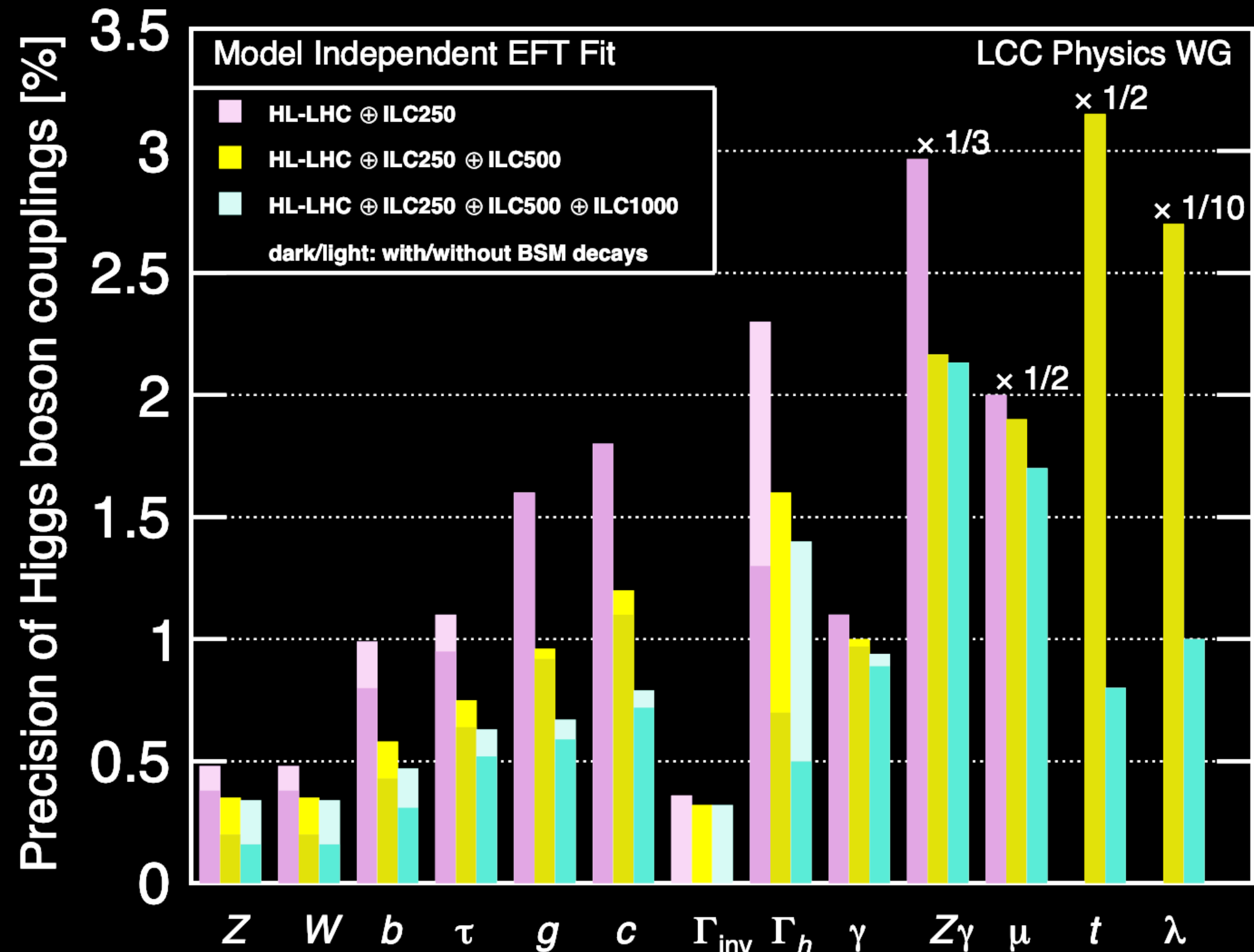
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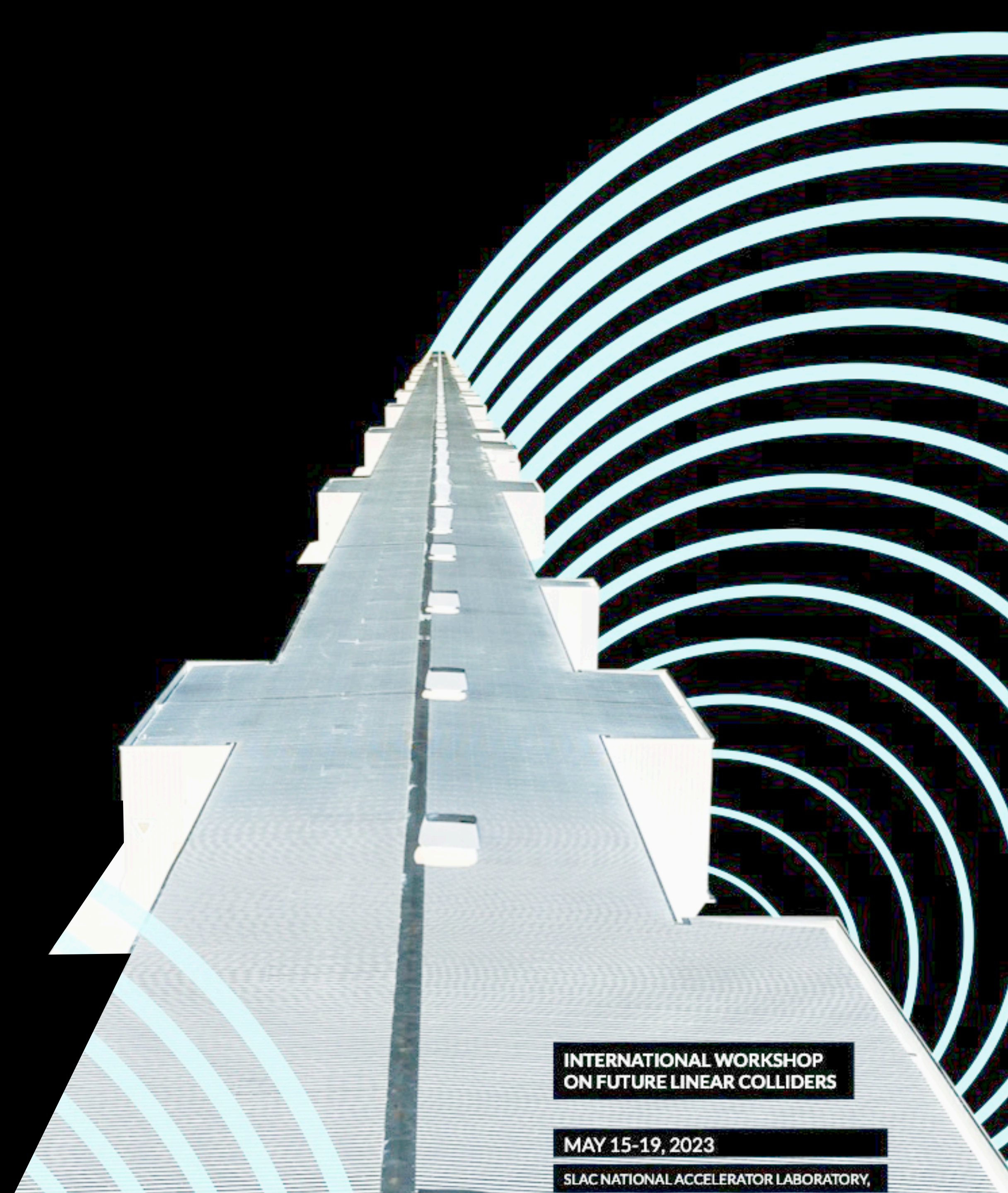
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*What are qualitative targets for Higgs precision in an era of exploration?*

\*ILC250/500/1000 as illustration of linear colliders more broadly



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# Seven Questions

Does the Higgs...

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# Seven Questions

Does the Higgs...

1. ...have a size?

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# Seven Questions

**Does the Higgs...**

1. ...have a size?
2. ...interact with itself?

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# Seven Questions

## Does the Higgs...

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3. ...mediate a yukawa force?

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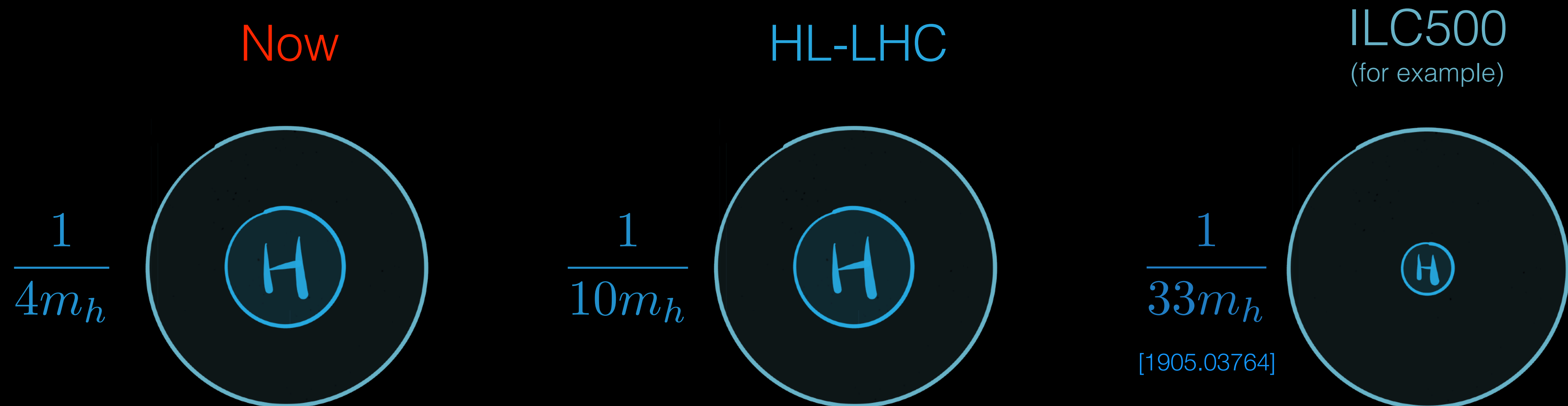
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# A Fundamental Scalar?

Figure of merit: Higgs “size” vs Compton wavelength. Beginning to probe the size of the Higgs at the LHC, but not yet to  $\pi$ -like compositeness

More precisely: bound “size” corrections, e.g.  $\mathcal{O}_H = \frac{1}{2\Lambda^2} (\partial_\mu |H|^2)^2$



Higgs factories will ultimately probe size of the Higgs well beyond this, providing strong evidence that the Higgs is elementary. *If not, abundant new physics awaits.*

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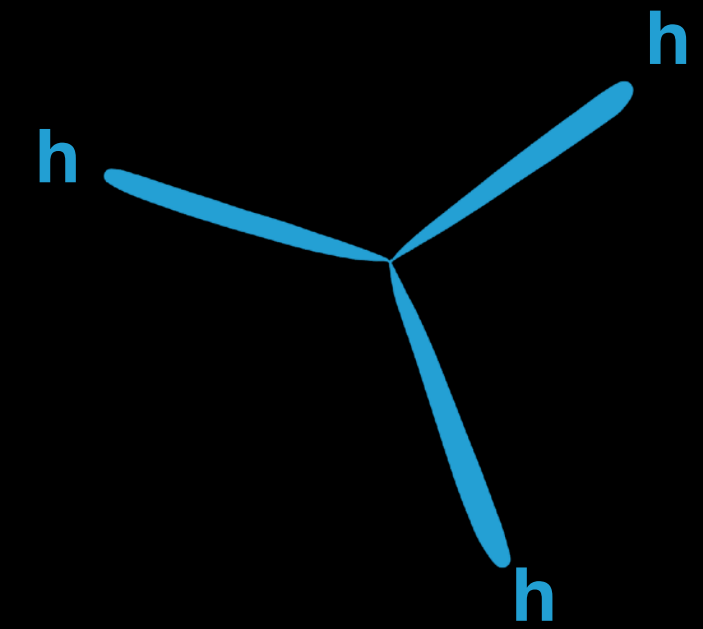
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# A Self-Interacting Particle?

A self-interacting Higgs (as SM predicts) would be unlike anything yet seen in nature; all other interactions change particle identity.

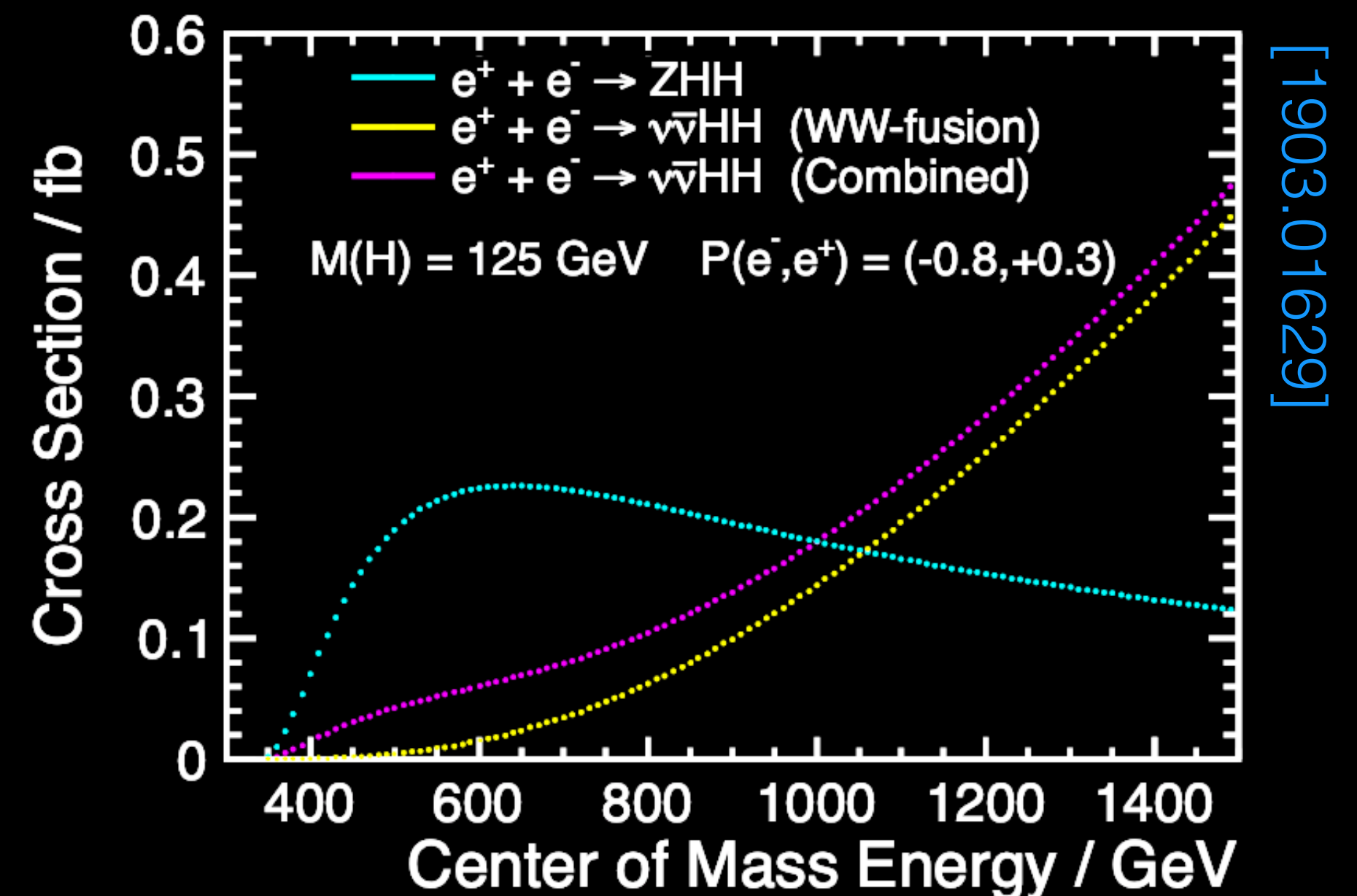


*Classically* test Higgs self-coupling via Higgs pair production.

ILC 4/ab @ 500 GeV: test Higgs self-interactions at **~27%** level  
(Improved b-tag, added modes  $\rightarrow$  20% [Dürig '16])

ILC 8/ab @ 1 TeV: **~10%** level

Further implications: see  
M. Perelstein's talk



*Quantum mechanically* test Higgs self-coupling via virtual corrections [McCullough 1312.3322]

Multiple c.o.m. energies matter: 49% @ ILC250  $\rightarrow$  38% @ ILC250/350/500

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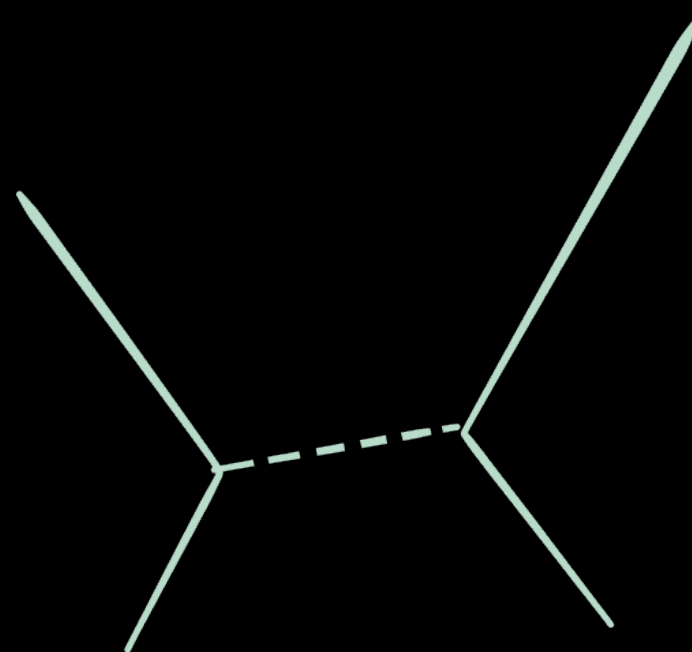
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# A Yukawa Force?

Yukawa force between fundamental particles: never seen until now



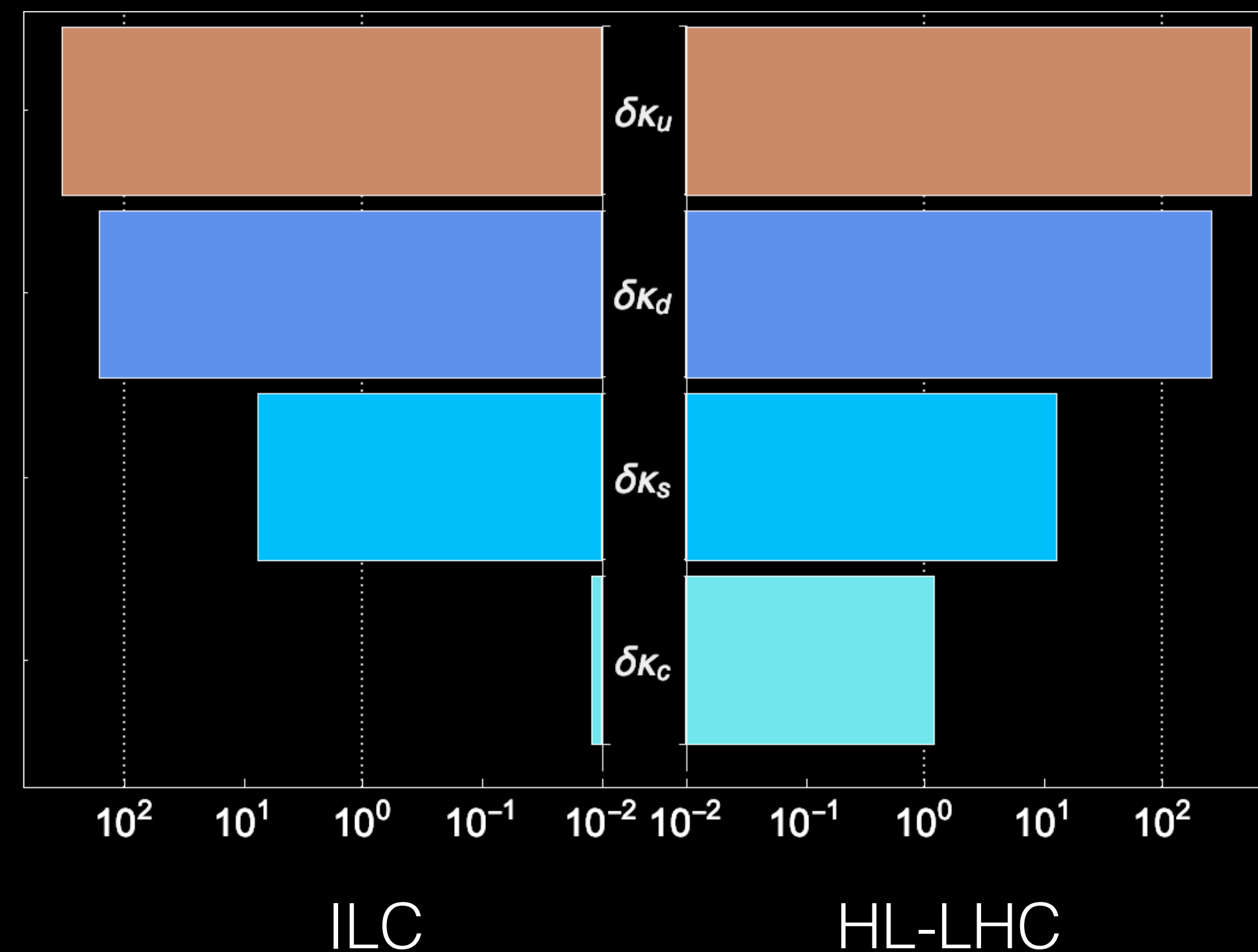
$$\frac{V_{\text{Higgs}}(r)}{V_{\text{Weak}}(r)} \sim \frac{y^2}{g^2} e^{-(m_h - m_Z)r}$$

Established by  $>5\sigma$  observation of  $t\bar{t}H$ ,  $H \rightarrow b\bar{b}$  and  $H \rightarrow \tau\tau$  in LHC Run 2

“Is this any less important than the discovery of the Higgs boson itself? My opinion: no, because fundamental interactions are as important as fundamental particles”

— G. Salam

Focus now on 2nd generation.  
Lightness makes flavor puzzle compelling, couplings could hold key to flavor puzzle.



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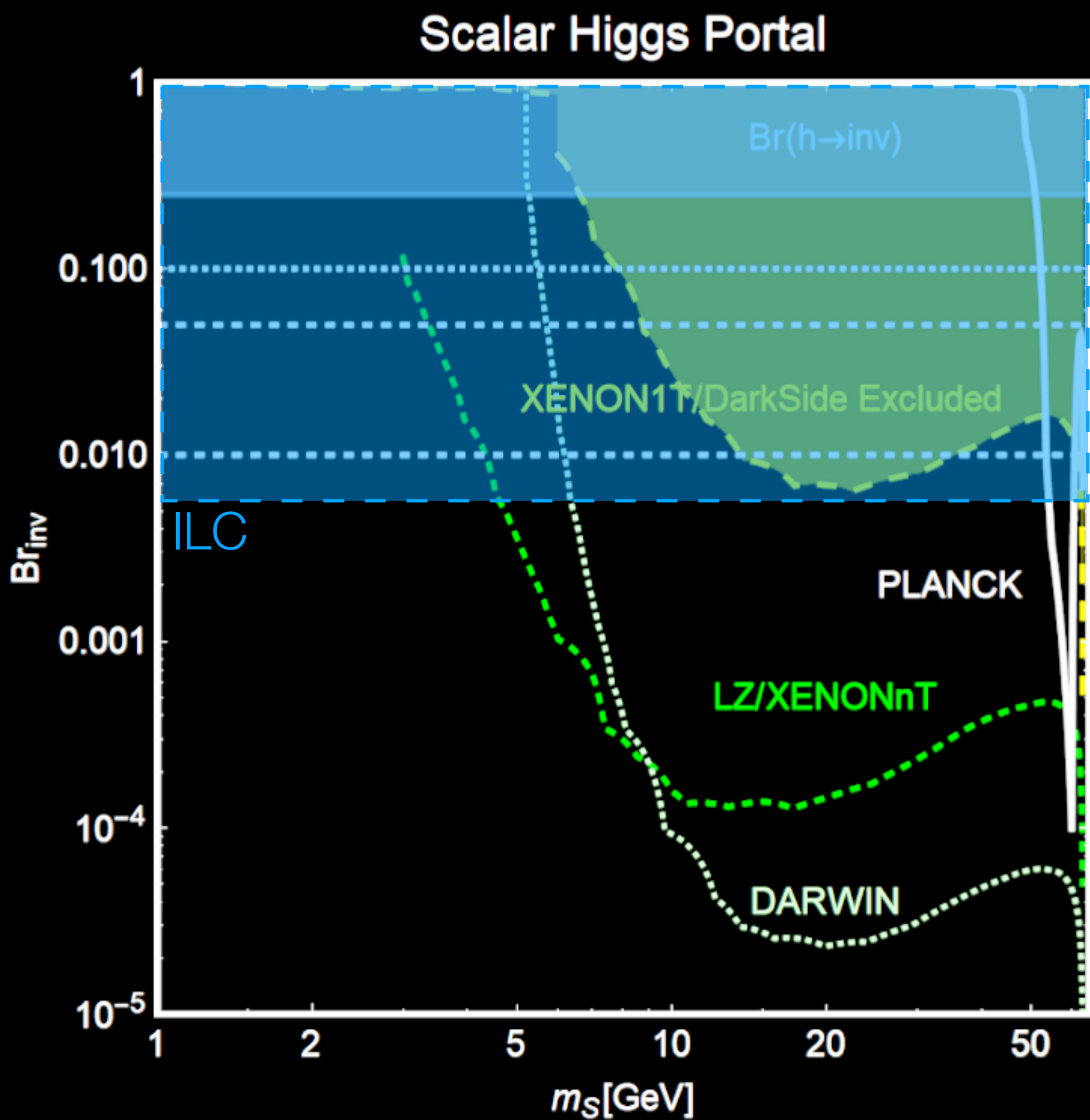
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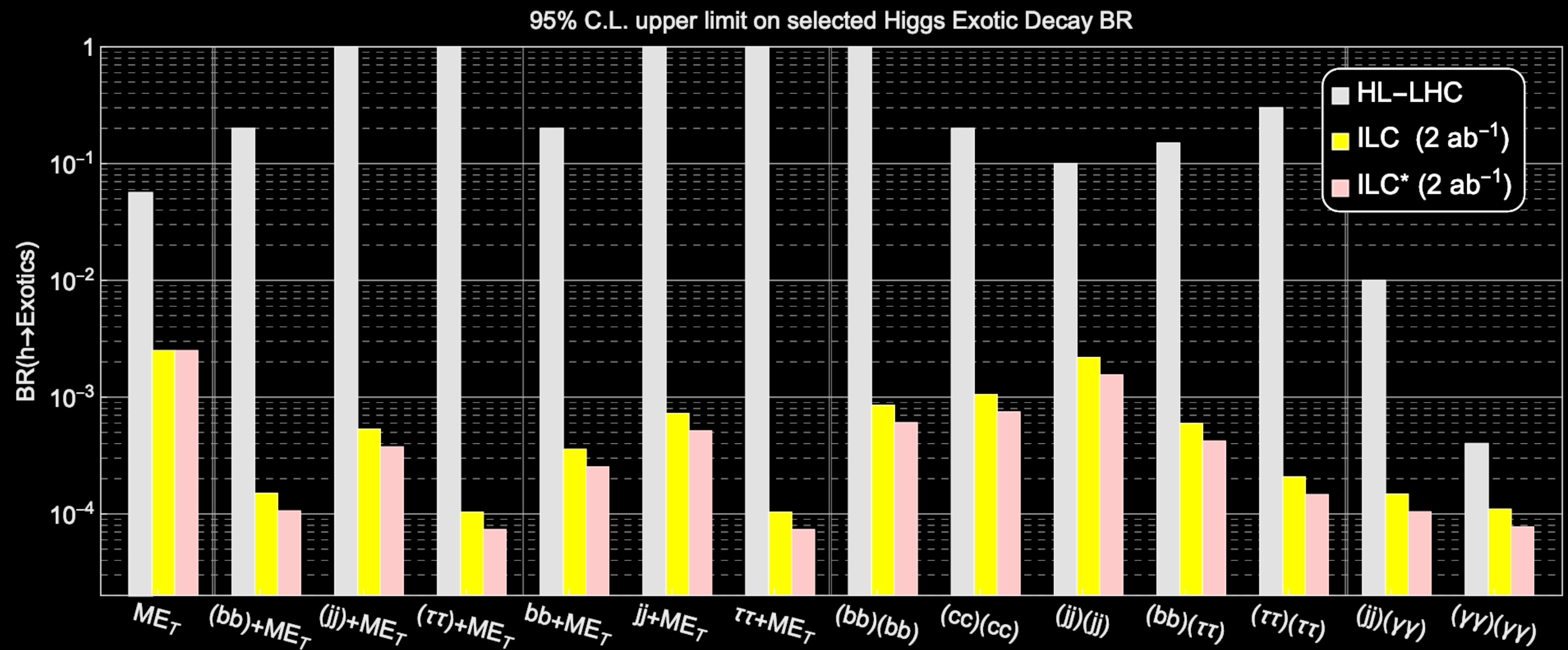
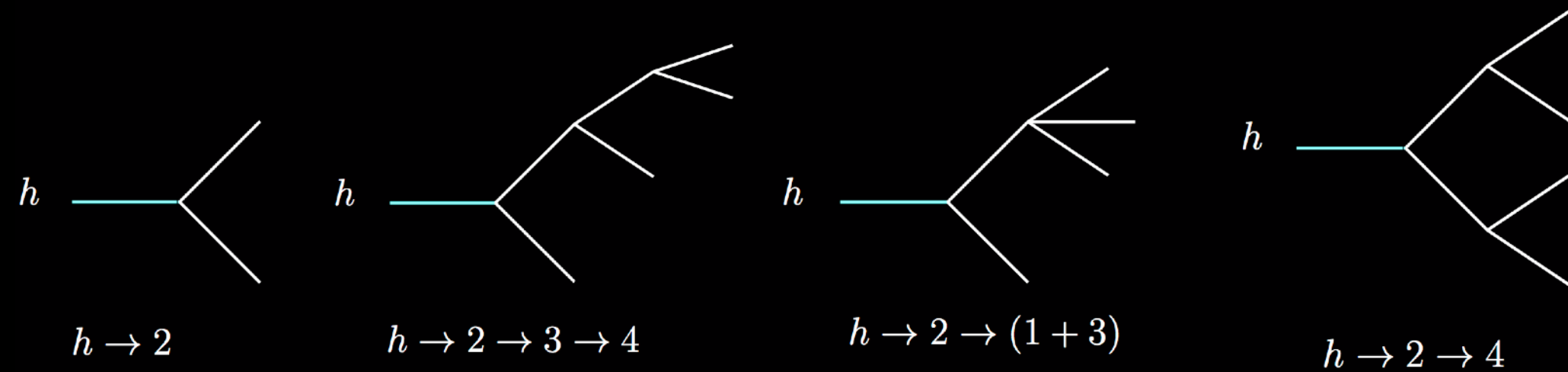
# A portal to the dark sector?

$$\mathcal{L} \supset |H|^2 \mathcal{O}$$

Higgs a (the?) primary portal for coupling to SM-neutral sectors



[G. Arcadi, A. Djouadi, M. Raidal, 1903.03616]



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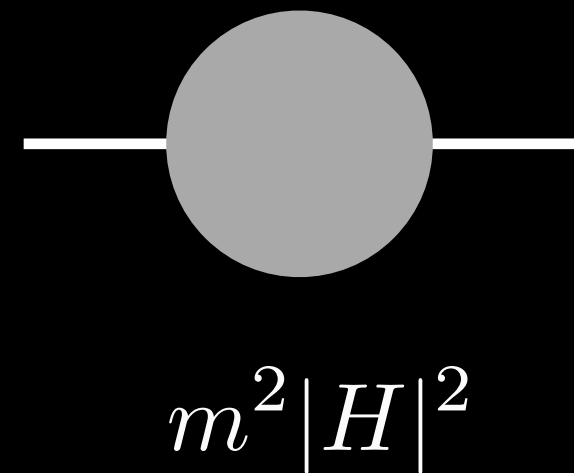
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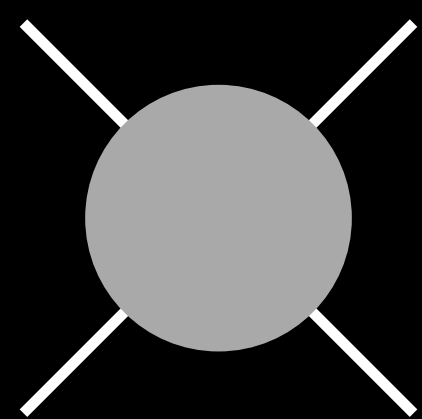
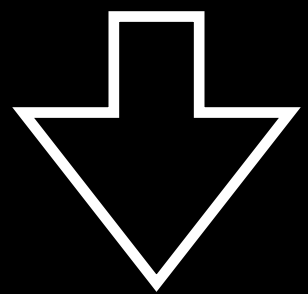
# Naturalness Strategy

There are now many ways of explaining EWSB and predicting the Higgs mass using symmetries.  
 But what is the bottom line? What's the ultimate target for symmetry-based naturalness?



$$\delta m_h^2 \sim 10 \times \frac{y_t^2}{16\pi^2} \times m_*^2$$

$$\Delta \equiv \frac{\delta m_h^2}{m_h^2} \sim 10 \times \frac{y_t^2}{16\pi^2} \times \frac{m_*^2}{m_h^2}$$



$$\mathcal{O}_H = (\partial |H|^2)^2$$

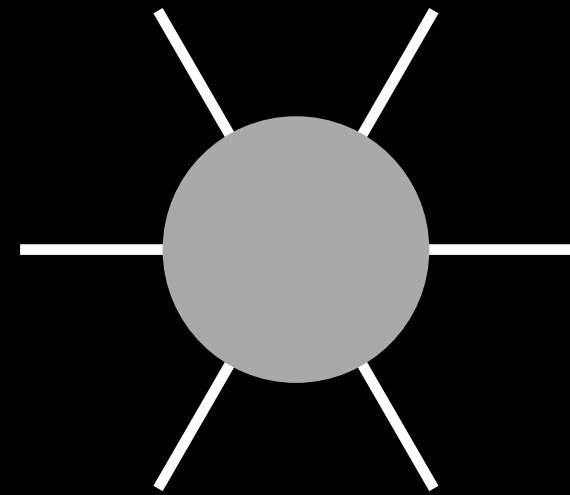
$$c_H \sim \frac{y_t^2}{16\pi^2} \times \frac{y_t^2}{m_*^2}$$

$$\delta \kappa_i \equiv c_H v^2 \sim \frac{y_t^2}{16\pi^2} \times \frac{y_t^2}{\lambda_h} \times \frac{m_h^2}{m_*^2}$$

$$\delta \kappa_i \sim 10 \times \left( \frac{y_t^2}{16\pi^2} \right)^2 \times \frac{y_t^2}{\lambda_h} \times \Delta^{-1} \Rightarrow$$

$\delta \kappa_i \sim 0.1 - 1\%$

# Naturalness Strategy



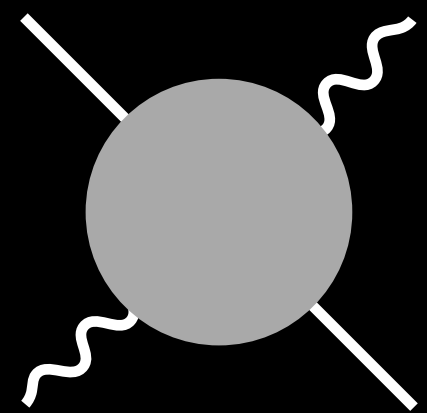
$$\mathcal{O}_6 = |H|^6$$

$$c_6 \sim \frac{y_t^2}{16\pi^2} \times \frac{y_t^4}{m_*^2}$$

$$\delta\kappa_\lambda \equiv c_6 v^2 / \lambda_h \sim \frac{y_t^2}{16\pi^2} \times \left(\frac{y_t^2}{\lambda_h}\right)^2 \times \frac{m_h^2}{m_*^2}$$

$$\delta\kappa_\lambda \sim 10 \times \left(\frac{y_t^2}{16\pi^2}\right)^2 \times \left(\frac{y_t^2}{\lambda_h}\right)^2 \times \Delta^{-1} \Rightarrow$$

$$\delta\kappa_\lambda \sim 1 - 10\%$$



$$\mathcal{O}_{FF} = g^2 |H|^2 F_{\mu\nu} F^{\mu\nu}$$

$$c_{FF} \sim 0.1 \times \frac{y_t^2}{16\pi^2} \times \frac{1}{\mu_*^2}$$

$$\delta\kappa_\gamma \equiv 16\pi^2 c_{FF} v^2 \sim 0.1 \times \frac{y_t^2}{\lambda_h} \times \frac{m_h^2}{\mu_*^2}$$

$$\delta\kappa_\gamma^{\text{super}} \sim \frac{y_t^2}{16\pi^2} \times \frac{y_t^2}{\lambda_h} \times \Delta^{-1} \Rightarrow$$

$$\delta\kappa_\gamma \sim 1 - 10\%$$

$$\delta\kappa_\gamma^{\text{hyper}} \sim \left(\frac{y_t^2}{16\pi^2}\right)^2 \times \Delta^{-1} \Rightarrow$$

Too small

Charged states:  $\mu_*$

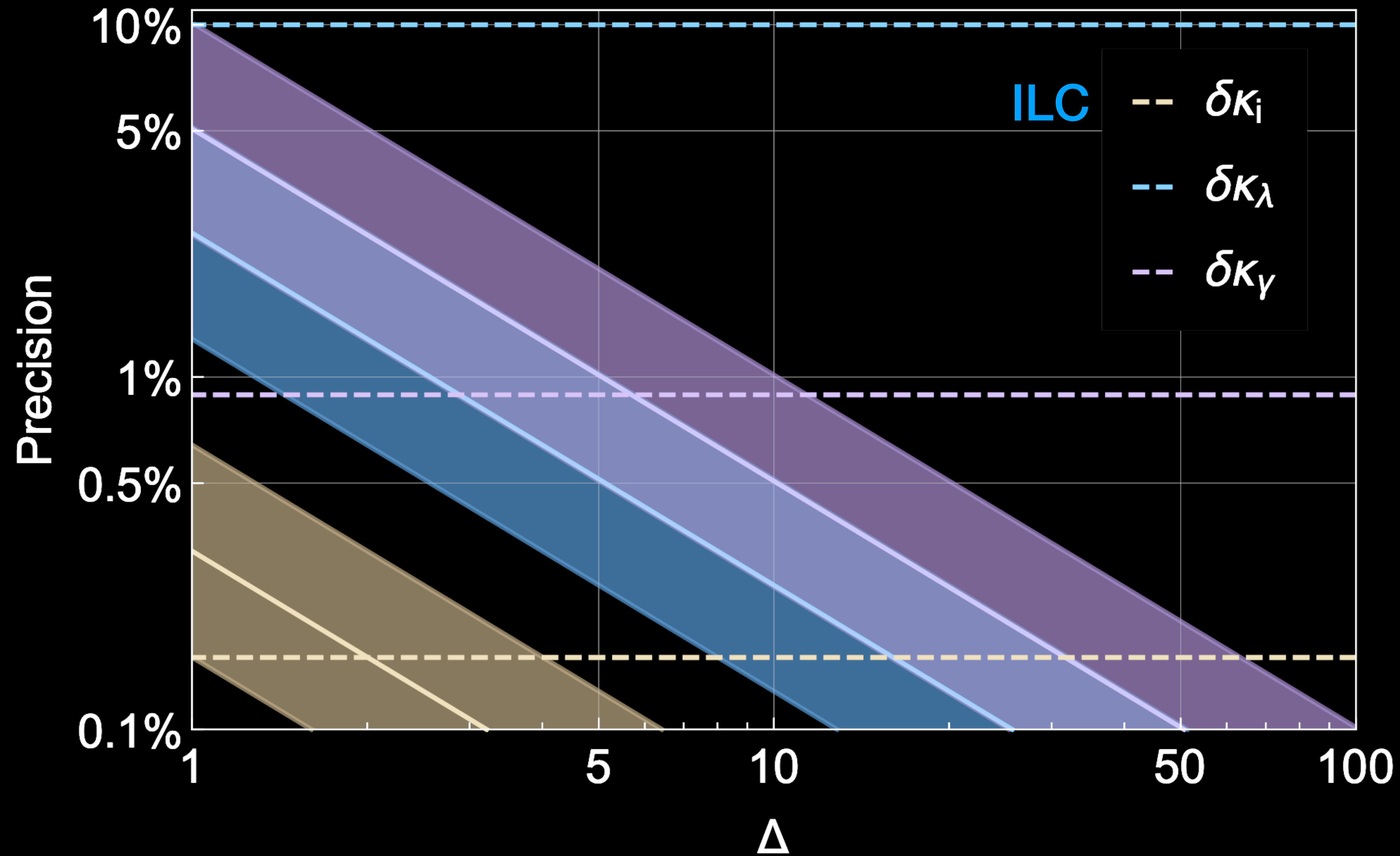
Super-soft

Hyper-soft

$$\mu_* = m_* \quad \mu_* = (g_*/\sqrt{\lambda_h})m_*$$

# Naturalness Strategy

Concrete theories: see  
M. Perelstein's talk



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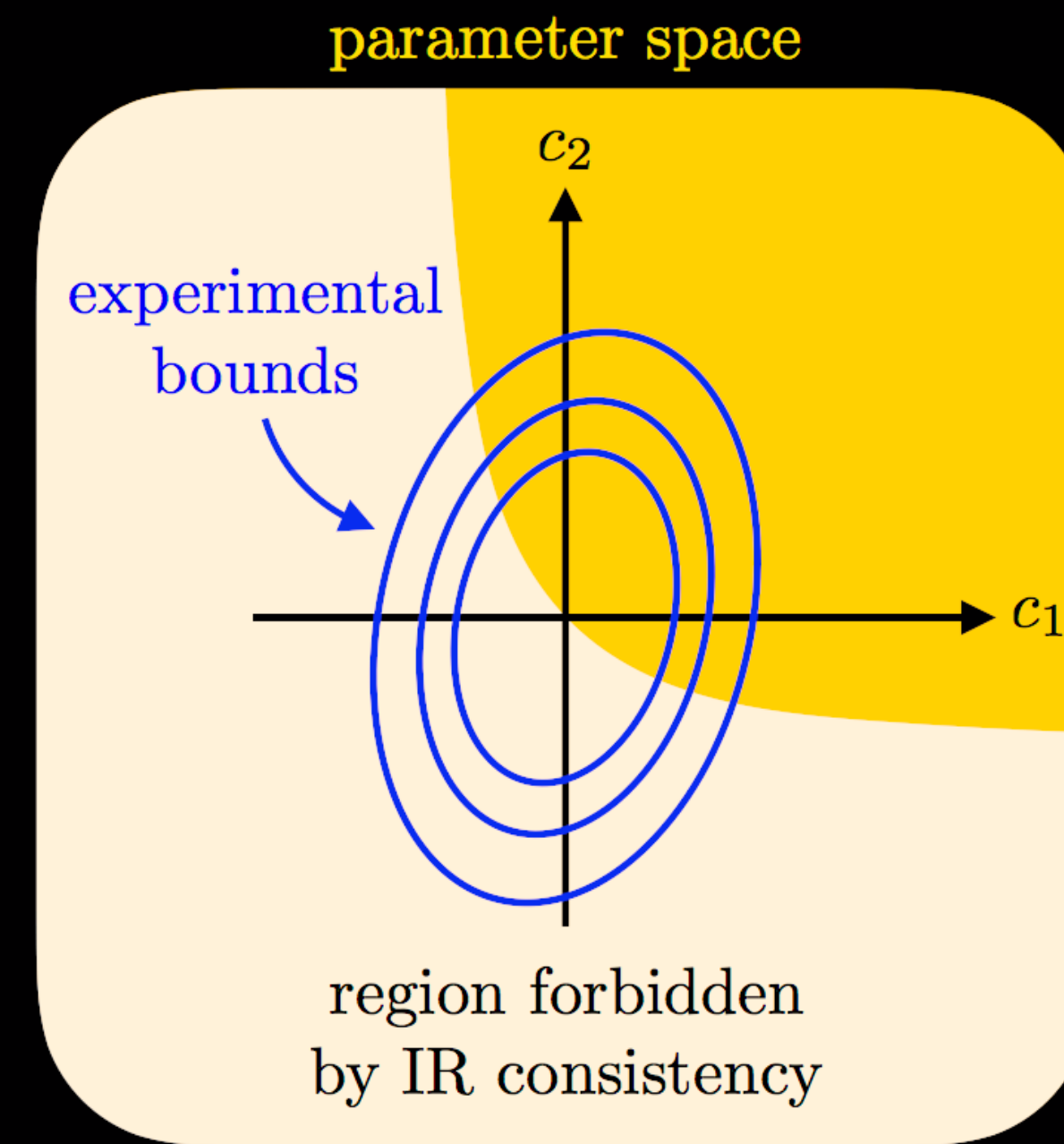
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# Thinking Positively

**Locality, unitarity, and analyticity** constrain EFT corrections to SM (“positivity bounds”)

**Long history**, revived in [Adams, Arkani-Hamed, Dubovsky, Nicolis, Rattazzi ‘06;  
Distler, Grinstein, Porto, Rothstein ‘06; ...]

**More recently:** extensive application directly to Wilson coefficients in SMEFT, e.g. [Bellazzini, Riva 1806.09640; Zhang, Zhou 1808.00010; Bi, Zhang, Zhou 1902.08977; Remmen, Rodd 1908.09845; Remmen, Rodd, 2004.02885; Zhang, Zhou 2005.03047; Fuks, Liu, Zhang, Zhou 2009.02212; Yamashita, Zhang, Zhou 2009.04490; Remmen, Rodd 2010.04723; Gu, Wang, Zhang 2011.03055; Trott 2011.10058; Bonnefoy, Gendy, Grojean 2011.12855; Li, Yang, Xu, Zhang, Zhou 2101.01191, ...]



[Remmen & Rodd, 1908.09845]

Improve global fits  
by imposing  
positivity bounds

**OR**

Interpret as  
experimental tests  
of bedrock  
principles of QFT.

(Ideally do both)

# Thinking Positively

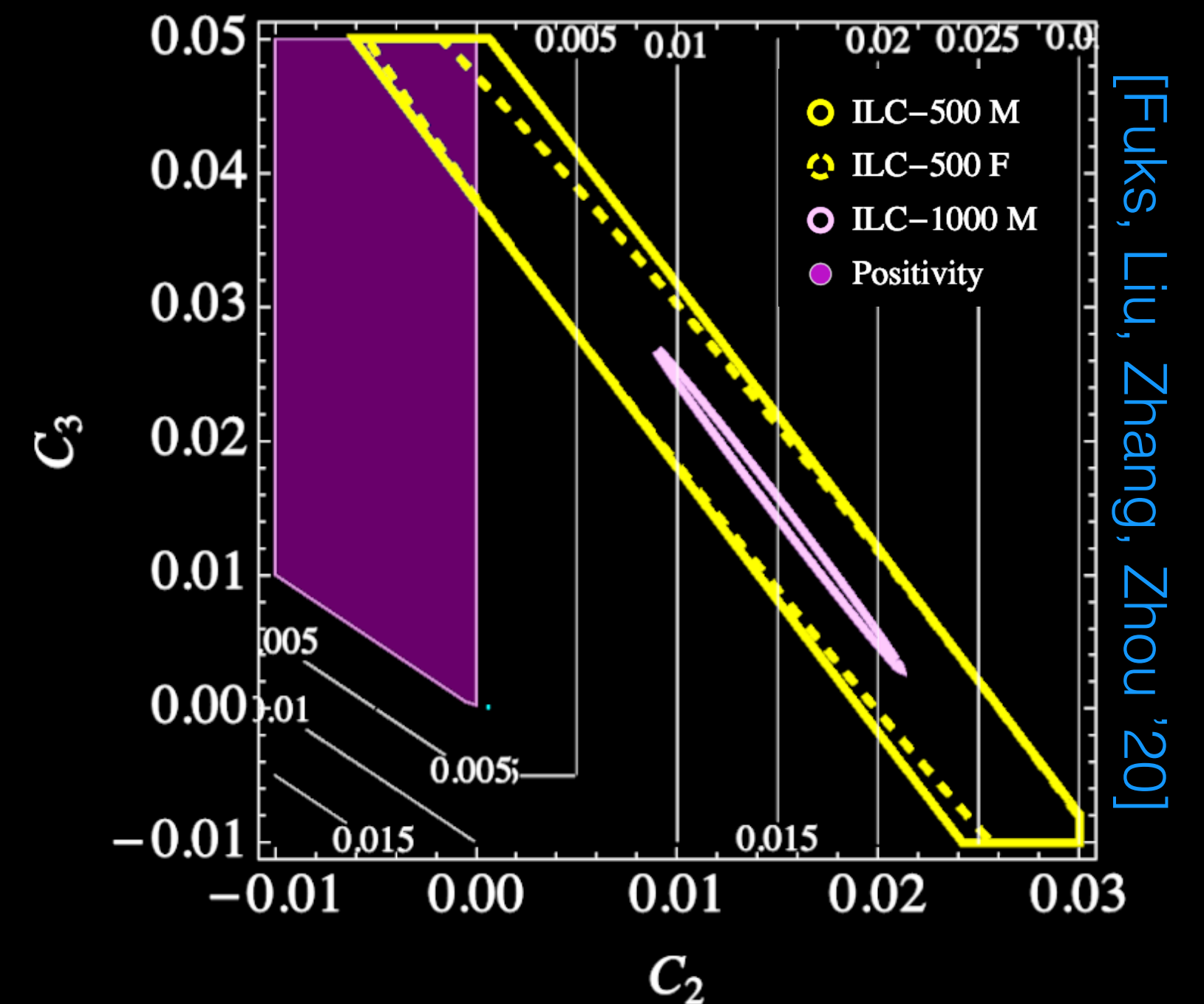
**d=6:** UV-sensitive positivity bounds, sum rules.      **d=8:** UV-insensitive positivity bounds

**Naive expectation:** dim-8 operator effects always subleading

**Reality:** often leading due to non-interference thms and more pragmatic non-interference effects (color, phase space, ...)

Thus far: primarily applied to aQGCs @ LHC  
[Bellazzini & Riva '18, Zhang & Zhou, '18,...]

Interesting prospects in  $e^+e^- \rightarrow e^+e^-, \gamma\gamma$  @ ILC  
[Fuks, Liu, Zhang, Zhou '20, Gu, Wang, Zhang '20]



*Positivity bounds also imply d=8 deviations are robust against cancellations, giving a guaranteed probe of UV physics with precision measurement.*



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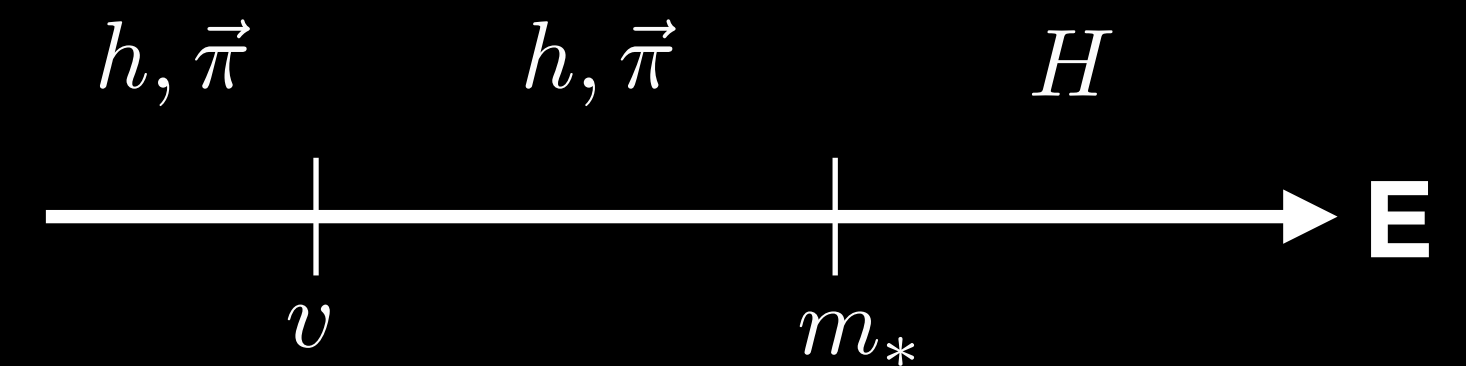
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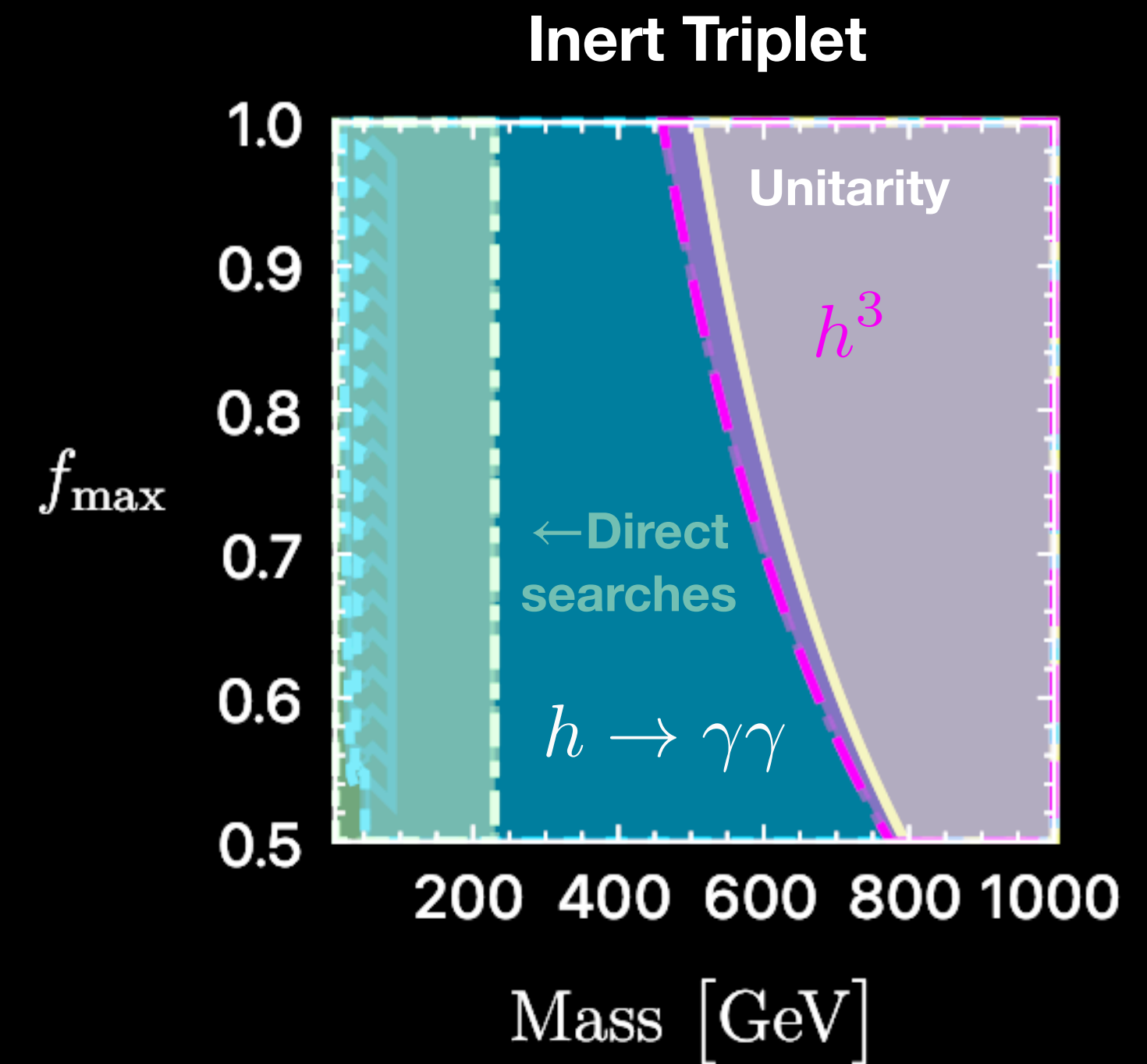
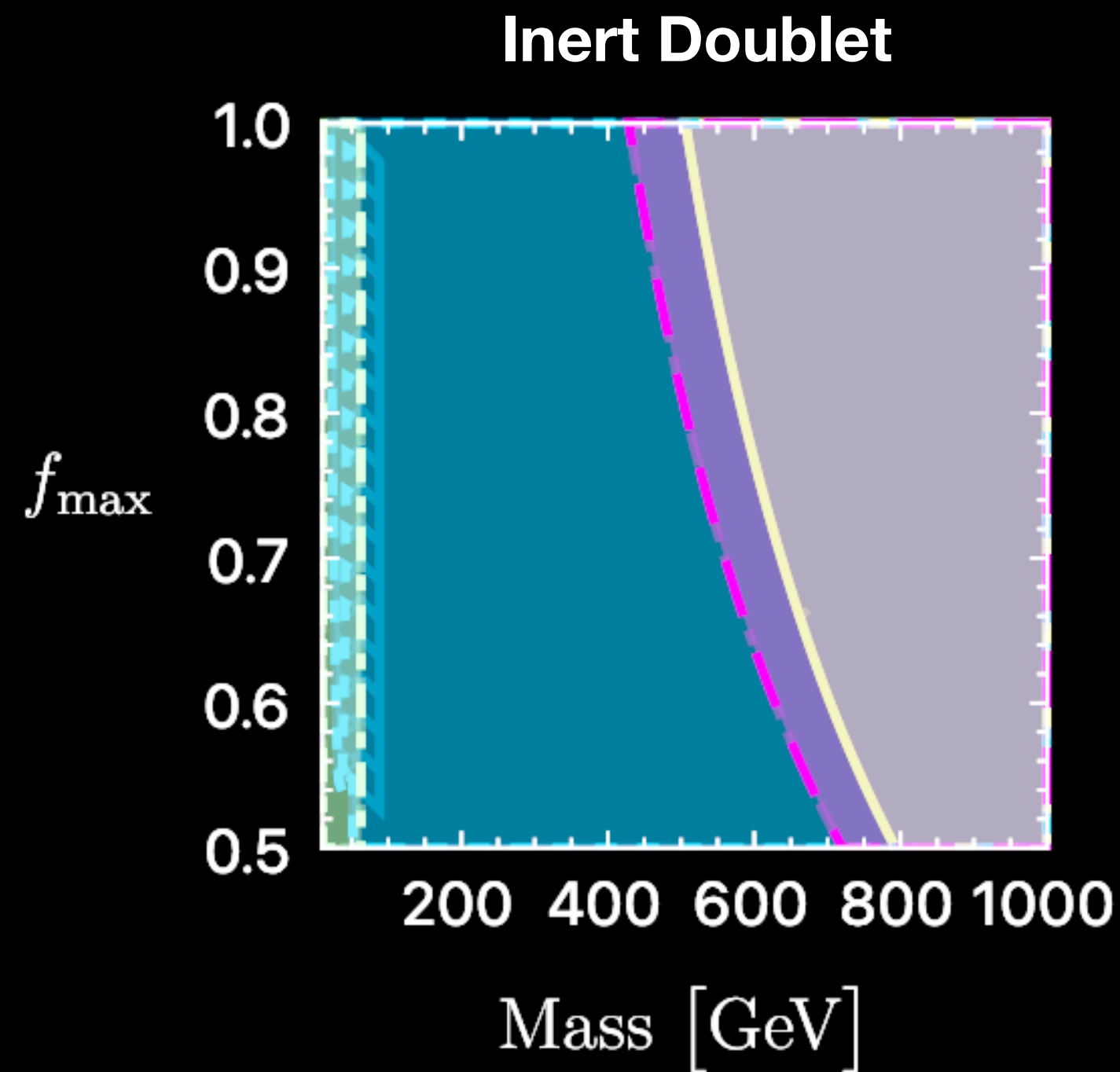
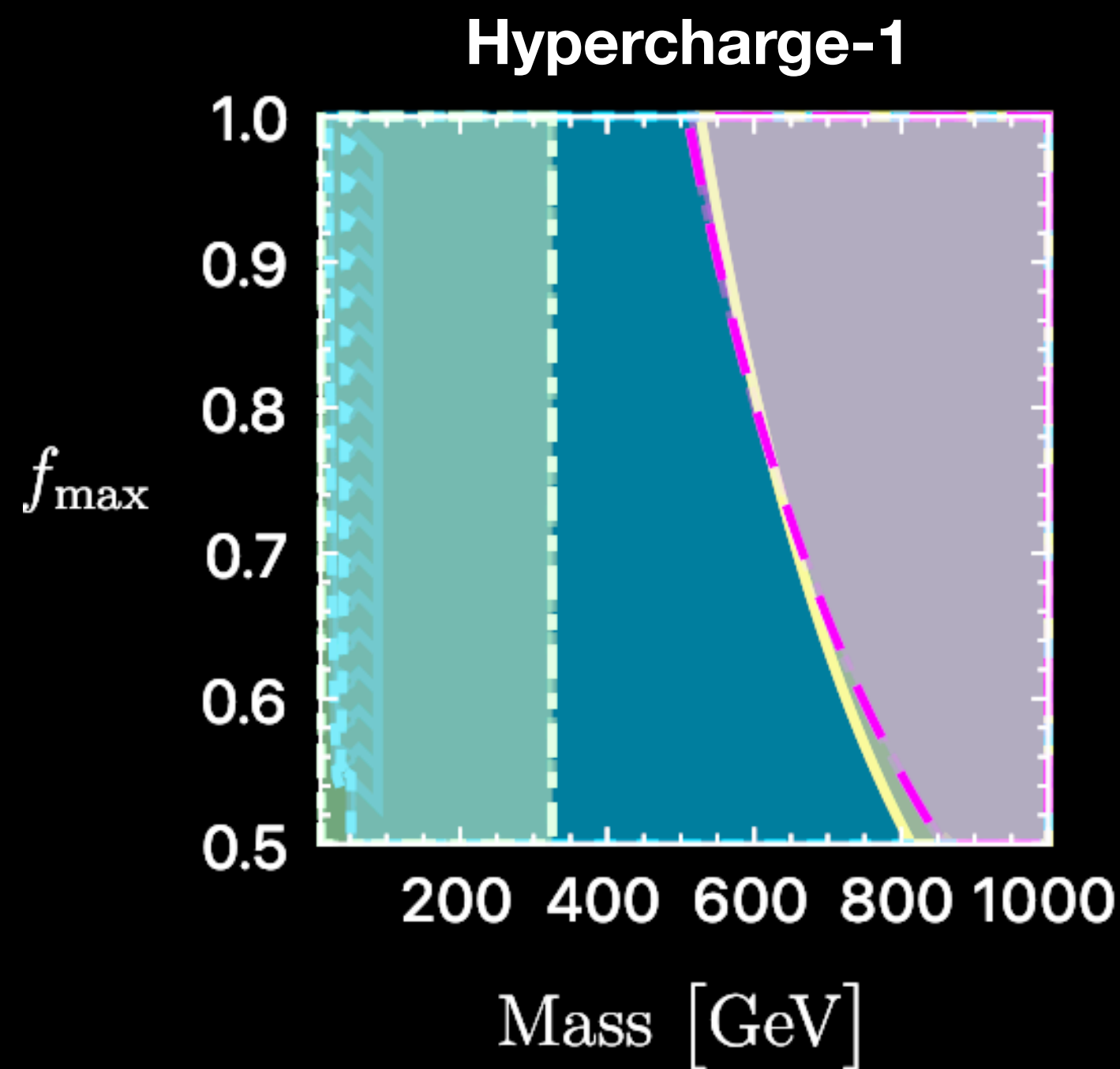
# Non-decoupling new particles?

Local EFT of the Higgs + SM particles does not linearly realize electroweak symmetry if new UV particles acquire more than half of their mass from the Higgs. Many examples currently viable

[Banta, Cohen, NC, Lu, Sutherland, 2110.02967]



## ILC coverage of non-decoupling scalars



# Seven Questions

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# Physics Case for Precision Measurements at a Higgs Factory, and how do we communicate about it?

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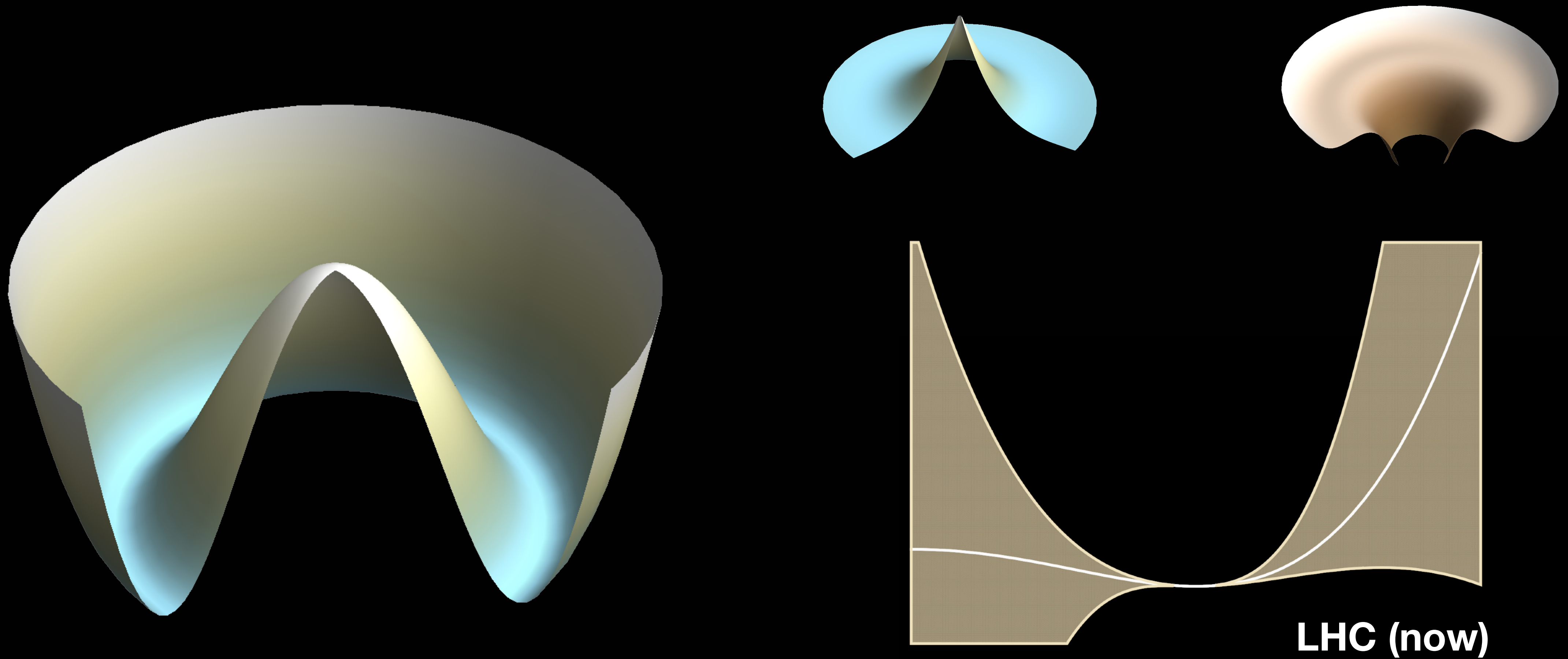


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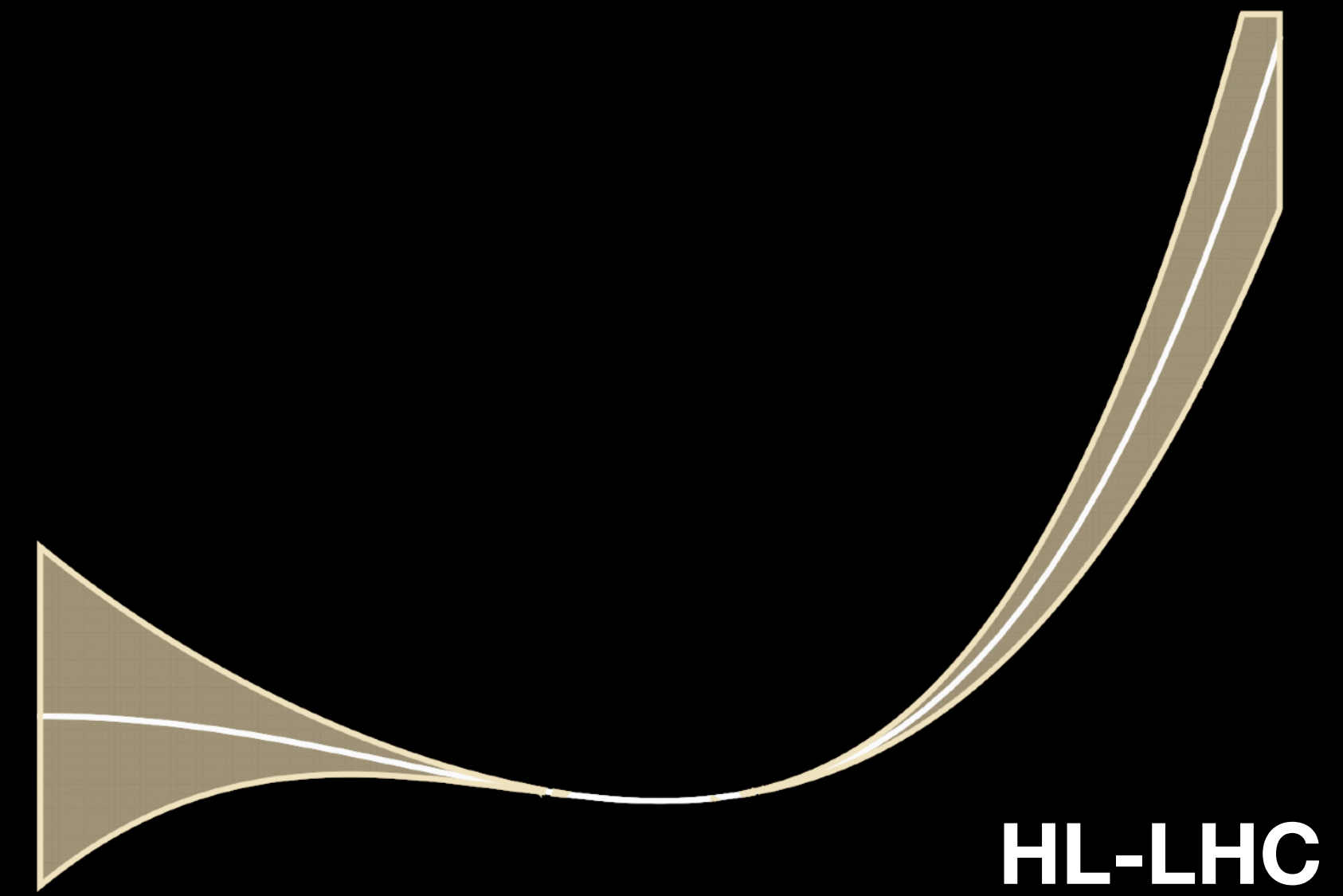
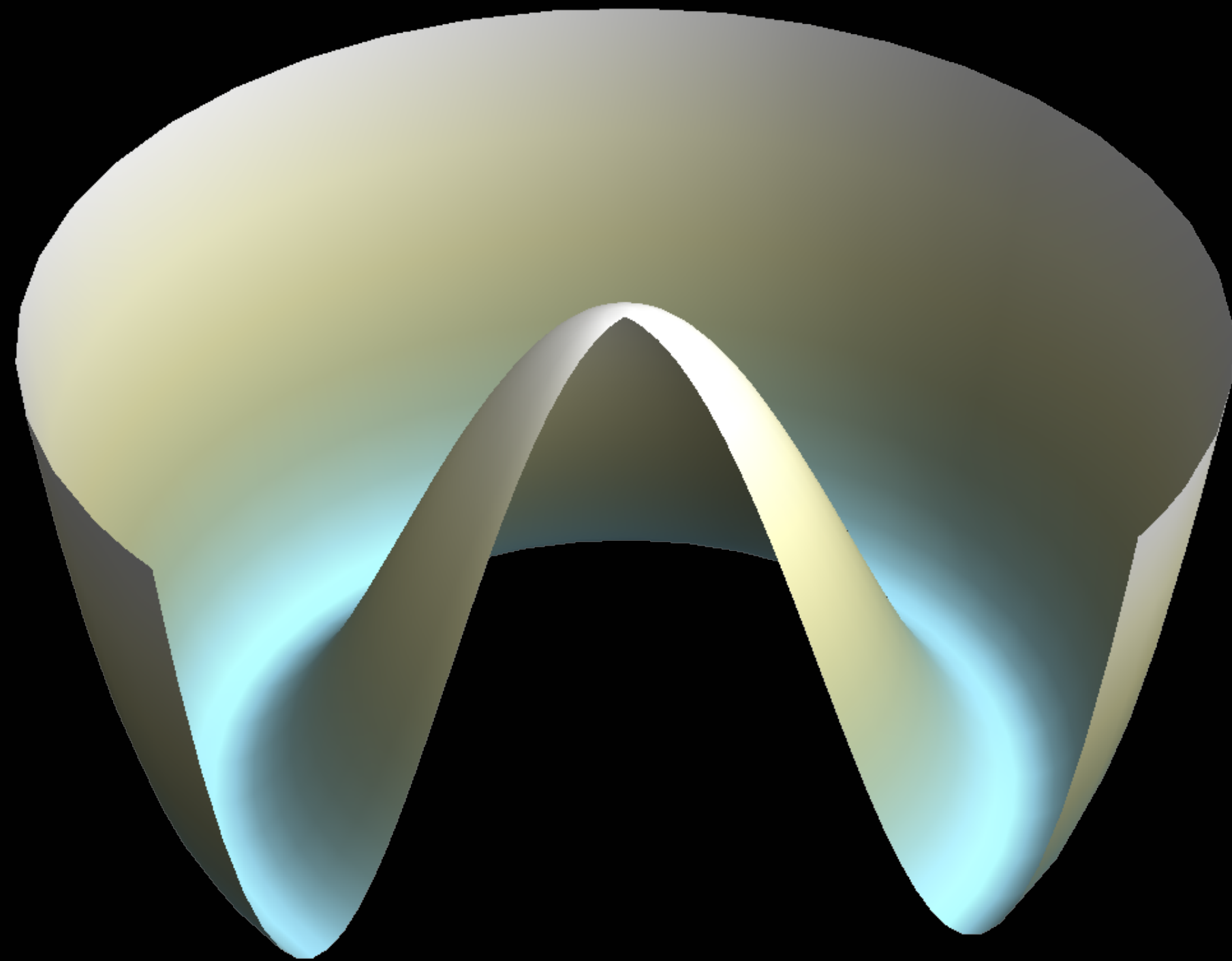
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# Is it the SM Higgs?

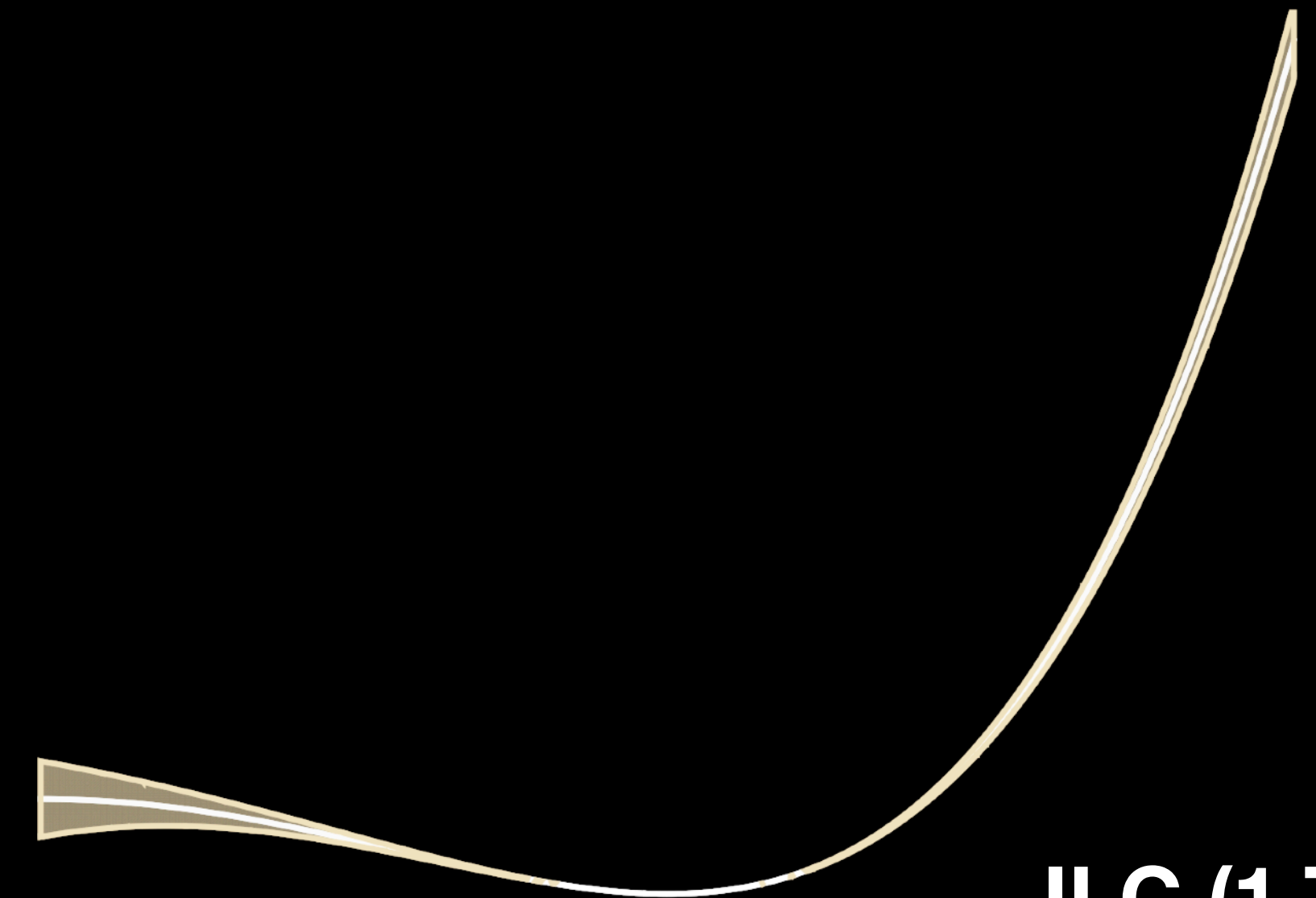


*(If you like this way of presenting Higgs self-coupling precision, please feel free to use it! The inspiration came from conversations with R. Petrossian-Byrne.)*

# Is it the SM Higgs?



HL-LHC



ILC (1 TeV)

# Imaging the Higgs?

## EHT image of M87



“Both because EHT measurements are sparse and because absolute phase calibration at millimeter wavelengths is impossible, recovering an image from EHT observations is a difficult and ill-posed problem. Images must be reconstructed using algorithms that find the best-fit images to data under a (hopefully minimal) set of additional assumptions about the source structure.”

— Andrew Chael (Princeton/EHT)

Summing over individual Higgs particle decays to a given final state (e.g.  $\gamma\gamma$ ) “images” the Higgs field in that channel. Are there better ways to visualize Higgs data & convey the majesty of precision measurement?

*Thank you!*

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