

# SMEFT fits for the top quark sector at LHC and Future Colliders

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Fernando Cornet-Gomez



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# Based on:

*"... standing on shoulders of giants"*

Isaac Newton

- Based on: [2205.02140] and [2206.08326]
- And also: [1907.10619] and [2107.13917]
- By members of the EF04 team:
  - Jorge de Blas, Yong Du, Christophe Grojean, Jiayin Gu, Victor Miralles, Michael E. Peskin, Junping Tian, Marcel Vos, Eleni Vryonidou
- and also additional members of the EF03 team:
  - Gauthier Durieux, Abel Gutiérrez Camacho, Luca Mantani, Marcos Miralles López, María Moreno Llácer, René Poncelet



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# Introduction

- Goal: constrain the top-quark Wilson coefficients of the SMEFT
- Numerical fits performed using `HEPfit` [1910.14012]
- The following topics will be discussed:
  - Relevant observables constraining each Wilson Coefficient
  - Estimations on the improvement of the measurements for the HL-LHC
  - Estimation of the relevant observables for this fit in future  $e + e -$  colliders
  - Prospects for our limits in the HL-LHC and future  $e + e -$  colliders



# Relevant operators

## 2-quark operators

Couplings of the t- and b-quark to the Z

$$O_{\varphi Q}^3 \equiv (\bar{Q} \tau^I \gamma^\mu Q) (\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)$$

$$O_{\varphi Q}^1 \equiv (\bar{Q} \gamma^\mu Q) (\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)$$

$$O_{\varphi t(b)} \equiv (\bar{t}(\bar{b}) \gamma^\mu t(b)) (\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)$$

EW dipole operators

$$O_{uW} \equiv (\bar{Q} \tau^I \sigma^{\mu\nu} t) (\varepsilon \varphi^* W_{\mu\nu}^I)$$

$$O_{tB} \equiv (\bar{Q} \sigma^{\mu\nu} t) (\varepsilon \varphi^* B_{\mu\nu})$$

Chromo-magnetic dipole op.

$$O_{tG} \equiv (\bar{Q} \sigma^{\mu\nu} T^A t) (\varepsilon \varphi^* G_{\mu\nu}^A)$$

t-quark yukawa

$$O_{t\varphi} \equiv (\bar{Q} t) (\varepsilon \varphi^* \varphi)$$

## 4-quark operators

Couplings of light quarks with t- and b-quarks

$$O_{tu}^8 \quad O_{td}^8 \quad O_{Qq}^{1,8} \quad O_{Qu}^8 \quad O_{Qd}^8 \quad O_{Qq}^{3,8} \quad O_{tq}^8$$

## 2-quark 2-lepton operators

Couplings of light leptons with t- and b-quarks

$$O_{eb} \quad O_{lb} \quad O_{et} \quad O_{lt} \quad O_{eQ} \quad O_{lQ}^+ \quad O_{lQ}^-$$

Rotation of Warsaw basis following [1802.07237] (LHC Top WG)

$$O_{\varphi Q}^1 \rightarrow O_{\varphi Q}^- = O_{\varphi Q}^1 - O_{\varphi Q}^3$$

$$O_{xB}$$

$$\begin{aligned} \Downarrow \\ \tilde{O}_{xZ} &= -\sin \theta_W O_{xB} \\ &+ \cos \theta_W O_{xW} \end{aligned}$$

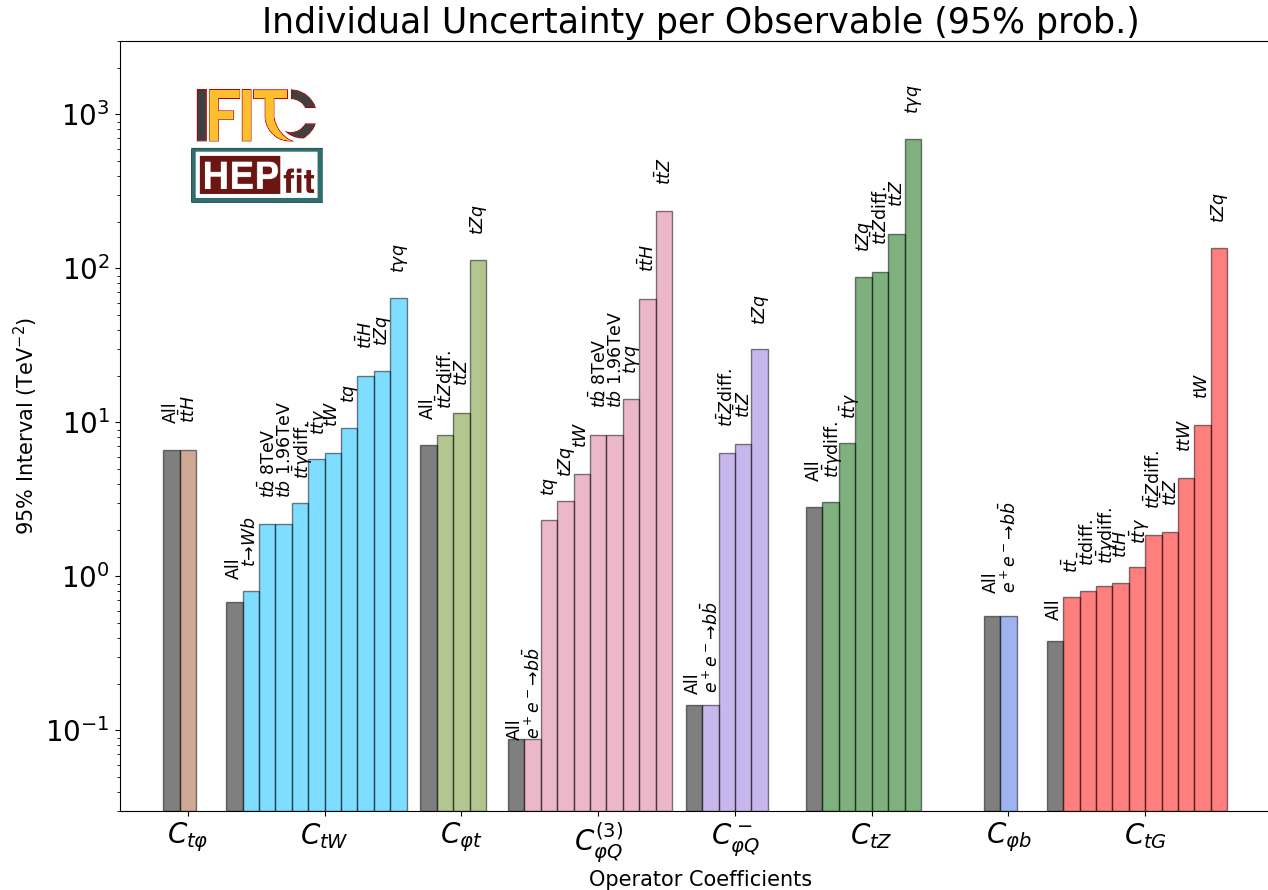


# Relevant observables

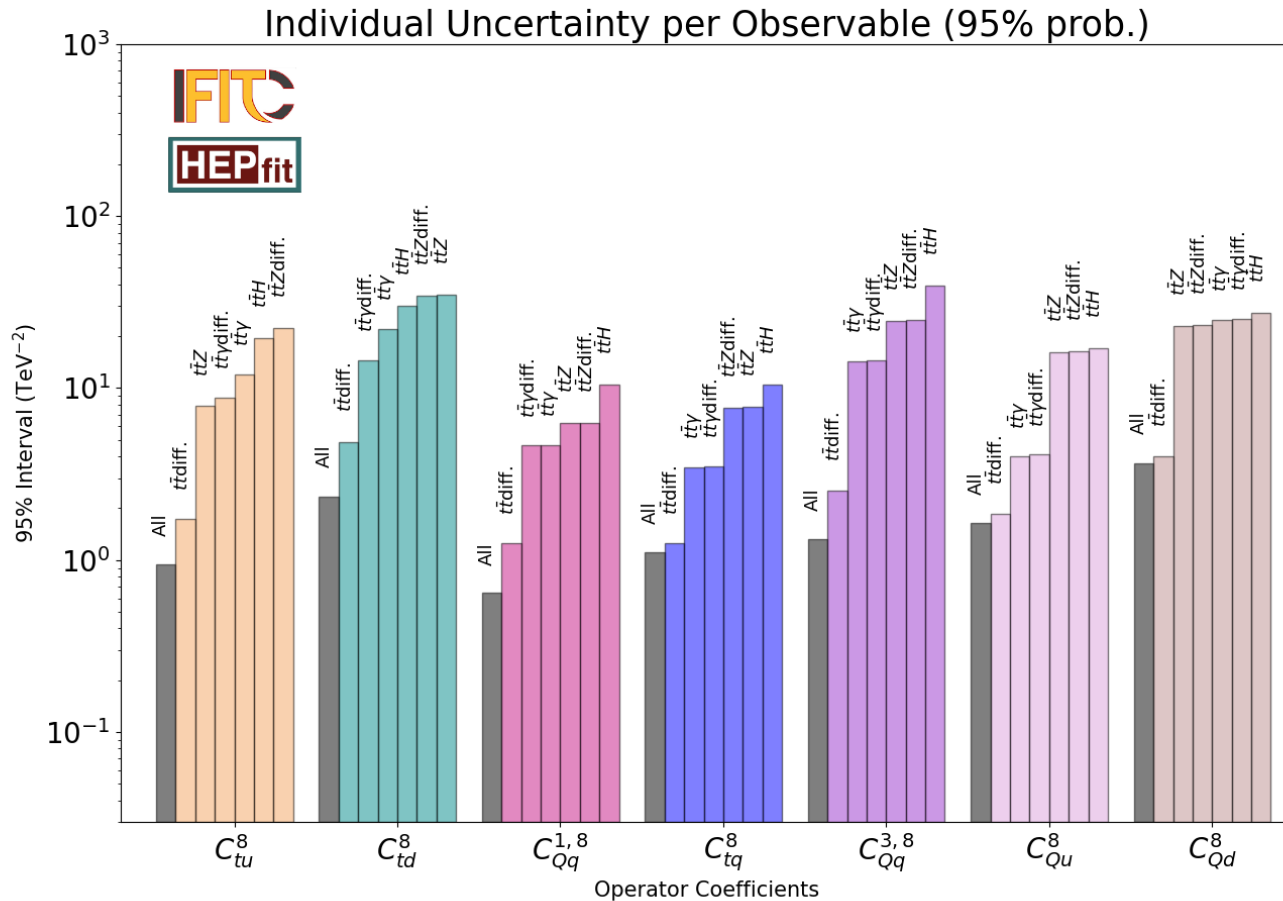
Process	Observable	$\sqrt{s}$	$\int \mathcal{L}$	Experiment
$pp \rightarrow t\bar{t}$	$d\sigma/dm_{t\bar{t}}$ (15+3 bins)	13 TeV	140 fb <sup>-1</sup>	CMS
$pp \rightarrow t\bar{t}$	$dA_C/dm_{t\bar{t}}$ (4+2 bins)	13 TeV	140 fb <sup>-1</sup>	ATLAS
$pp \rightarrow t\bar{t}Z$	$d\sigma/dp_T^Z$ (7 bins)	13 TeV	140 fb <sup>-1</sup>	ATLAS
$pp \rightarrow t\bar{t}\gamma$	$d\sigma/dp_T^\gamma$ (11 bins)	13 TeV	140 fb <sup>-1</sup>	ATLAS
$pp \rightarrow t\bar{t}H + tHq$	$\sigma$	13 TeV	140 fb <sup>-1</sup>	ATLAS
$pp \rightarrow tZq$	$\sigma$	13 TeV	77.4 fb <sup>-1</sup>	CMS
$pp \rightarrow t\gamma q$	$\sigma$	13 TeV	36 fb <sup>-1</sup>	CMS
$pp \rightarrow t\bar{t}W$	$\sigma$	13 TeV	36 fb <sup>-1</sup>	CMS
$pp \rightarrow t\bar{b}$ (s-ch)	$\sigma$	8 TeV	20 fb <sup>-1</sup>	LHC
$pp \rightarrow tW$	$\sigma$	8 TeV	20 fb <sup>-1</sup>	LHC
$pp \rightarrow tq$ (t-ch)	$\sigma$	8 TeV	20 fb <sup>-1</sup>	LHC
$t \rightarrow Wb$	$F_0, F_L$	8 TeV	20 fb <sup>-1</sup>	LHC
$p\bar{p} \rightarrow t\bar{b}$ (s-ch)	$\sigma$	1.96 TeV	9.7 fb <sup>-1</sup>	Tevatron
$e^-e^+ \rightarrow b\bar{b}$	$R_b, A_{FBLR}^{bb}$	$\sim 91$ GeV	202.1 pb <sup>-1</sup>	LEP/SLD



# Individual 2 quarks-WC constraints



# Individual 4 quarks-WC constraints



# Prospects for Measurements at HL-LHC

Uncertainty	Reduced by a factor of
Theoretical	$1/2$
Modelling	$1/2$
Systematic	$1/\sqrt{\mathcal{L}}$
Statistical	$1/\sqrt{\mathcal{L}}$





# Inclusive Crosssections & Helicities

Process	Measured (fb)	SM (fb)	LHC Unc.					HL-LHC Unc.				
			theo.	exp.				theo.	exp.			
				stat.	sys.	mod.	tot.		stat.	sys.	mod.	tot.
$pp \rightarrow t\bar{t}H + tHq$	640	664.3	41.7	90	40	70.7	121.2	20.9	19.4	8.6	35.4	41.3
$pp \rightarrow t\bar{t}Z$	990	810.9	85.8	51.5	48.9	67.3	97.8	42.9	11.1	10.6	33.6	37.0
$pp \rightarrow t\bar{t}\gamma$	39.6	38.5	1.76	0.8	1.25	2.16	2.62	0.88	0.17	0.27	1.08	1.13
$pp \rightarrow tZq$	111	102	3.5	13.0	6.1	6.2	15.7	1.75	2.09	0.98	3.1	3.87
$pp \rightarrow t\gamma q$	115.7	81	4	17.1	21.1	21.1	34.4	2	1.9	2.3	10.6	11.0
$pp \rightarrow t\bar{t}W + EW$	770	647.5	76.1	120	59.6	73.0	152.6	38.1	13.1	6.5	36.5	39.4
$pp \rightarrow t\bar{b}$ (s-ch)	4900	5610	220	784	936	790	1454	110	35	42	395	399
$pp \rightarrow tW$	23100	22370	1570	1086	2000	2773	3587	785	49	89	1386	1390
$pp \rightarrow tq$ (t-ch)	87700	84200	250	1140	3128	4766	5810	125	51	140	2383	2390
$F_0$	0.693	0.687	0.005	0.009	0.006	0.009	0.014	0.003	0.0004	0.0003	0.004	0.004
$F_L$	0.315	0.311	0.005	0.006	0.003	0.008	0.011	0.003	0.0003	0.0002	0.004	0.004



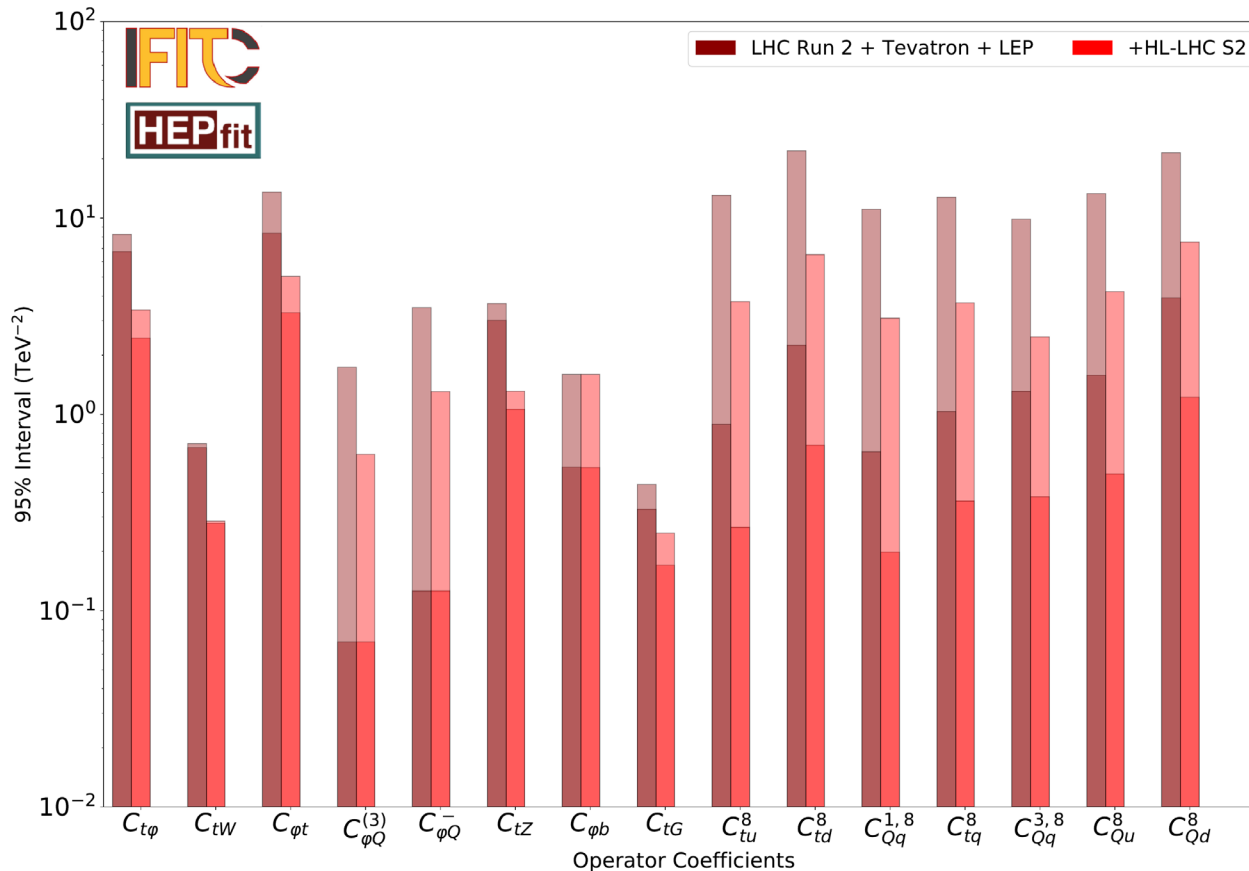
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# Expected HL-LHC constraints improvement



Shadowed  $\rightarrow$  Marginalized from global fit

Solid  $\rightarrow$  Individual fit



# Bottom-pair production at e+e- colliders

Machine	Polarisation	Energy	Luminosity	Observable
ILC	P(e <sup>+</sup> , e <sup>-</sup> ):(-30%, +80%) P(e <sup>+</sup> , e <sup>-</sup> ):(+30%, -80%)	250 GeV	2 ab <sup>-1</sup>	$\sigma_{b\bar{b}}$ $A_{FB}^{bb}$
		500 GeV	4 ab <sup>-1</sup>	
		1 TeV	8 ab <sup>-1</sup>	
CLIC	P(e <sup>+</sup> , e <sup>-</sup> ):(0%, +80%) P(e <sup>+</sup> , e <sup>-</sup> ):(0%, -80%)	380 GeV	2 ab <sup>-1</sup>	$\sigma_{b\bar{b}}$ $A_{FB}^{bb}$
		1.5 TeV	2.5 ab <sup>-1</sup>	
		3 TeV	5 ab <sup>-1</sup>	
CEPC/FCC-ee	Unpolarised	Z-pole	57.5/150 ab <sup>-1</sup>	$\sigma_{b\bar{b}}$ $A_{FB}^{bb}$
		240 GeV	20/5 ab <sup>-1</sup>	
		360/365 GeV	1/1.5 ab <sup>-1</sup>	

- Cross-section and Assymetry FB constrain:

- The WC related with EW precision observables:  $C_{\varphi Q}^+ = C_{\varphi Q}^1 + C_{\varphi Q}^3$ ,  $C_{\varphi b}$
- Relevant for 2-quark 2-lepton WC:  $C_{lQ}^+$ ,  $C_{lb}$ ,  $C_{eb}$
- The higher-energy measurement are more relevant for the 2-quark 2-lepton operators



# Bottom-pair production at e+e- colliders

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ILC	P(e <sup>+</sup> , e <sup>-</sup> ):(-30%, +80%)	250 GeV	2 ab <sup>-1</sup>	$\sigma_{b\bar{b}}$ $A_{FB}^{b\bar{b}}$
	P(e <sup>+</sup> , e <sup>-</sup> ):(+30%, -80%)	500 GeV	4 ab <sup>-1</sup>	
		1 TeV	3 ab <sup>-1</sup>	

To do:  
 Update  $e^+e^- \rightarrow b\bar{b}$  projections by Adrian Irlles, Roman Poschl et al.  
 See Jesus Marquez talk ([link](#))

- Cross-section and Assymetry FB constrain:
  - The WC related with EW precision observables:  $C_{\varphi Q}^+ = C_{\varphi Q}^1 + C_{\varphi Q}^3$ ,  $C_{\varphi b}$
  - Relevant for 2-quark 2-lepton WC:  $C_{lQ}^+$ ,  $C_{lb}$ ,  $C_{eb}$
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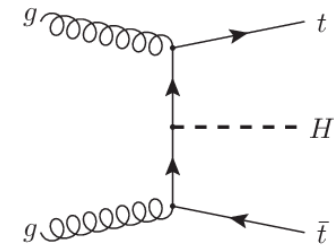
# Top-pair production at e+e- colliders

Machine	Polarisation	Energy	Luminosity	Observable
ILC	P(e <sup>+</sup> , e <sup>-</sup> ):(-30%, +80%)	500 GeV	4 ab <sup>-1</sup>	Optimal
	P(e <sup>+</sup> , e <sup>-</sup> ):(+30%, -80%)	1 TeV	8 ab <sup>-1</sup>	Observables
CLIC	P(e <sup>+</sup> , e <sup>-</sup> ):(0%, +80%)	380 GeV	2 ab <sup>-1</sup>	Optimal
		1.5 TeV	2.5 ab <sup>-1</sup>	
	P(e <sup>+</sup> , e <sup>-</sup> ):(0%, -80%)	3 TeV	5 ab <sup>-1</sup>	Observables
CEPC/FCC-ee	Unpolarised	350 GeV	0.2 ab <sup>-1</sup>	Optimal
		365 GeV	1/1.5 ab <sup>-1</sup>	Observables

- Optimal observables maximally exploit the information in the fully differential  $e^+e^- \rightarrow t\bar{t} \rightarrow bW^+\bar{b}W^-$  dist. [1807.02121], constraining:
  - The 2-fermion coefficients:  $C_{\varphi Q}^-$ ,  $C_{\varphi t}$ ,  $C_{tW}$ ,  $C_{tZ}$
  - The 2-quark 2-lepton:  $C_{lQ}^-$ ,  $C_{lt}$ ,  $C_{et}$ ,  $C_{eQ}$
  - Two different energies above the top-pair threshold are needed to constrain all the 2- and 4-fermion operators (constant/linear vs quadratically with energy)
  - We eliminate the blind directions in the  $O_{\varphi Q}^1 - O_{\varphi Q}^3$  plane



# $t\bar{t}H$ production at $e^+e^-$ colliders

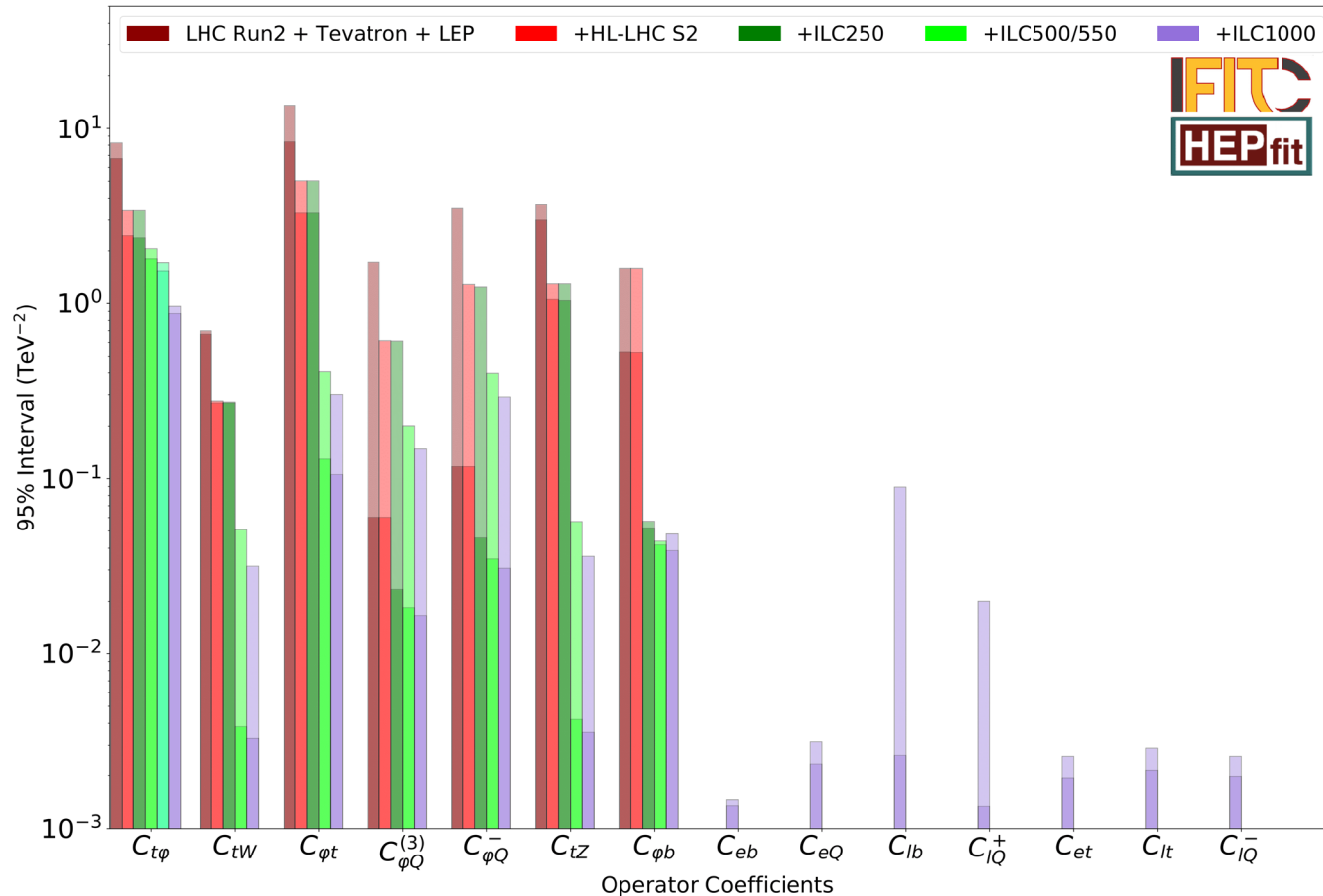


Machine	Polarisation	Energy	Luminosity	Observable
ILC	$P(e^+, e^-):(-30\%, +80\%)$	500/550 GeV	$4 \text{ ab}^{-1}$	Inclusive cross section
	$P(e^+, e^-):(+30\%, -80\%)$	1 TeV	$8 \text{ ab}^{-1}$	
CLIC	$P(e^+, e^-):(0\%, +80\%)$ $P(e^+, e^-):(0\%, -80\%)$	1.5 TeV	$2.5 \text{ ab}^{-1}$	Inclusive cross section

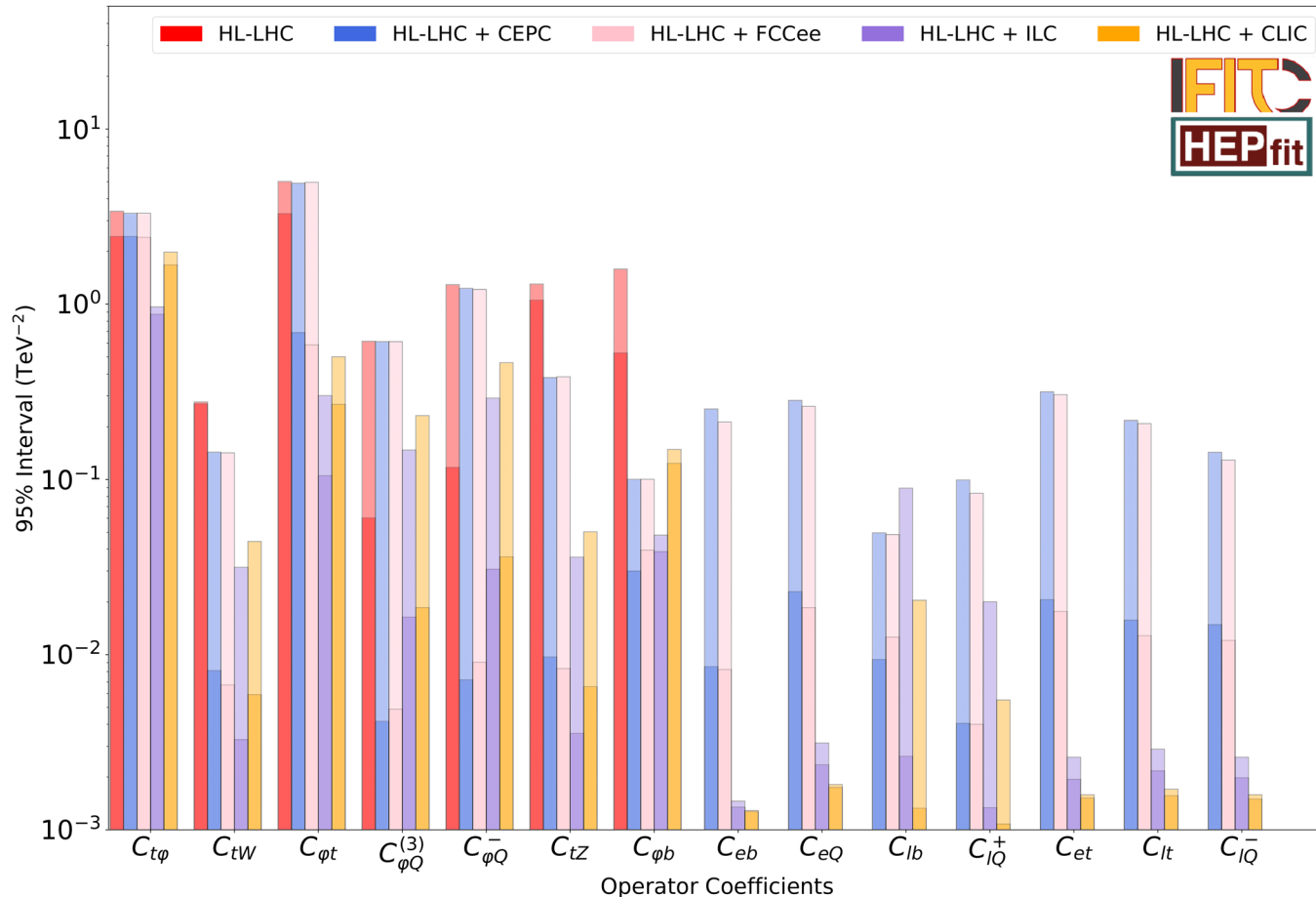
- Key observable for the top quark Yukawa coupling
- The production cross section is 3 times bigger at ILC 550 than at ILC500
  - Improved statistical sensitivity by more than a 50%
- ILC550, CLIC1500 and HL-LHC have similar sensitivities
- ILC1000 improves the expected HL-LHC sensitivity by a factor of two



# Expected constraints for ILC



# Comparison of Future Colliders





# Prospects for Top Yukawa uncertainties

Values in % units		LHC	HL-LHC	ILC500	ILC550	ILC1000	CLIC
$\delta y_t$	Global fit	12.2	5.06	3.14	2.60	1.48	2.96
	Indiv. fit	10.2	3.70	2.82	2.34	1.41	2.52

- Sensitivity at ILC500 is lower than at HL-LHC:
  - No huge improvement for the individual constraint
  - Global fit: larger improvement due to multiple observables constraining the Top Yukawa coupling
- Increasing the energy by 50 GeV provides an important improvement in the constraints thanks to the growth in the cross section
- Similar results are found for CLIC
- An improvement higher than a factor of 2.5 would be obtain at the final stage of ILC w.r.t. the HL-LHC



# Outlook

- Expand the Optimal observables study ( $e^+e^- \rightarrow t\bar{t} \rightarrow bW^+\bar{b}W^-$ ) for the Muon collider
- Incorporate  $pp \rightarrow t\bar{t}\ell\bar{\ell}$  ( $m_{\ell\ell} \neq m_z$ ) production at the LHC
  - Master thesis Abel + future ATLAS/CMS measurements
  - We expect to restrict them at HL-LHC to compare with e+e- colliders
- We are expanding the parametrization to NLO
- Include the quadratic terms in the parametrizations
- Update LHC measurements with recent full run 2 results



# Summary

- HL-LHC expected to improve the bounds by roughly a factor 3
- An  $e^+e^-$  collider can significantly improve bounds on bottom-quark and on top-quark operators (operated above the  $t\bar{t}$  threshold)
  - FCCee and CECP (at and slightly above the  $t\bar{t}$  threshold) can improve bottom- and top-operators by factor 5 (2 for 2-fermion operators)
  - Power to constrain 4-fermion operators limited by energy reach
  - ILC and CLIC operated at two center-of-mass energies above the  $t\bar{t}$  threshold can provide very tight bounds on all operators, with bounds on 4F taking advantage of energy-growing sensitivity
- Significant improvements for the limits on the top-quark yukawa are found when operating above 550 GeV



# Thank you



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