



FPD Experimental Seminar – SLAC
7th July 2020

Probing QCD using top quark pairs: latest results from CMS

Matteo M. Defranichis

context

- the Standard Model and the top quark
→ focus on top quark mass
- the LHC and the CMS experiment



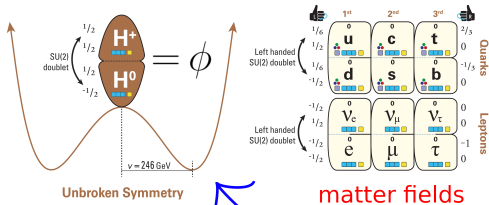
recent CMS results

- measurement of the $t\bar{t}$ cross section at $\sqrt{s} = 13$ TeV
- extraction of m_t and α_S
- **first measurement of the running of the top quark mass**
- measurement of a triple-differential $t\bar{t}$ cross section at $\sqrt{s} = 13$ TeV
- global QCD analysis with HERA DIS data: PDFs, α_S , m_t

the Standard Model of particle physics

quantum field theory based on principle of **local gauge invariance**

$$\underbrace{SU(3)_c}_{\text{strong}} \otimes \underbrace{SU(2)_L \otimes U(1)_Y}_{\text{electroweak}}$$



gauge fields (interactions)

$$V(\phi) = \underbrace{-\mu^2|\phi|^2}_{\text{mass term}} + \underbrace{\lambda|\phi|^4}_{\text{quartic coupling}}$$

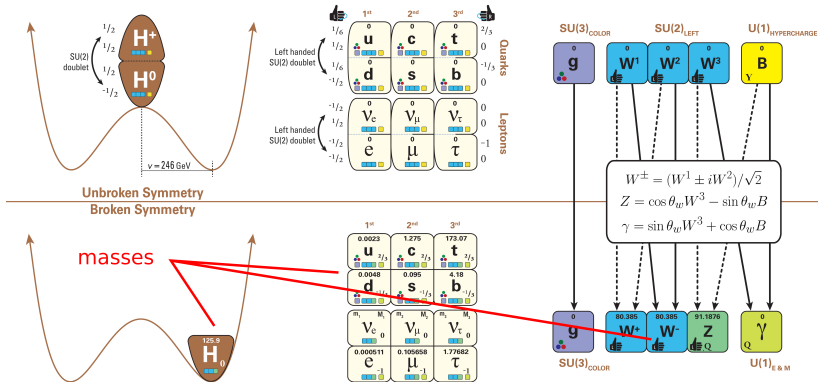
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physical fields obtained after

- electroweak mixing
- spontaneous symmetry breaking



the Standard Model of particle physics

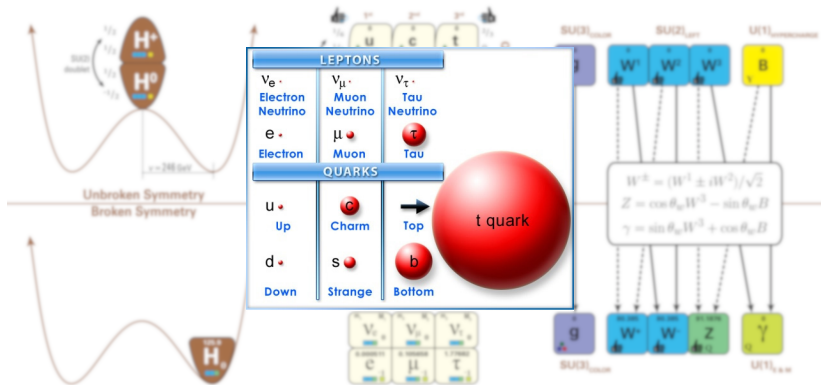
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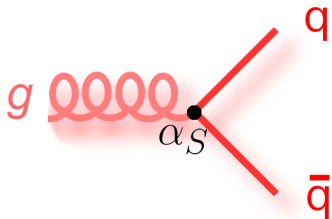
$m_t \simeq 173 \text{ GeV} \rightarrow$ most massive SM particle



strong interaction of quarks and gluons
→ 8 gluon fields

fundamental parameters

- 1 strong coupling constant α_S
- 2 quark masses



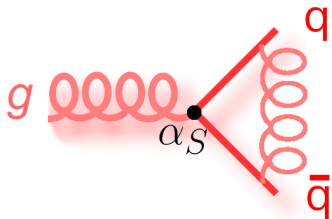
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quantum corrections contain divergent loop diagrams \Rightarrow **renormalization**

- infinities subtracted at scale μ_R and absorbed into bare parameters



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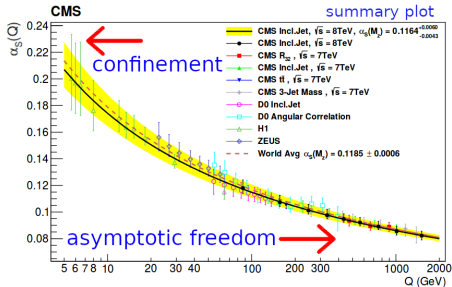
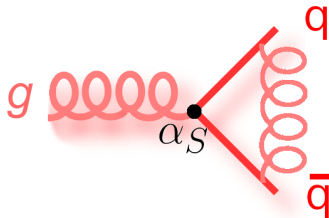
quantum corrections contain divergent loop diagrams ⇒ **renormalization**

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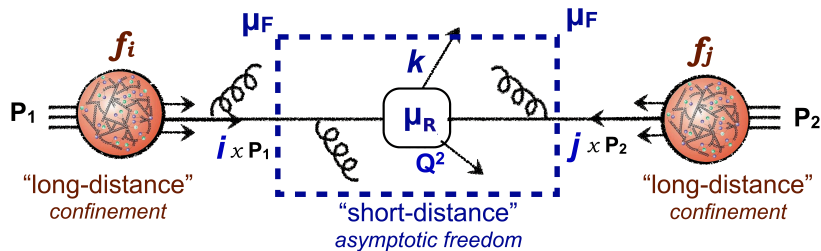
running of $\alpha_S(Q)$

- 1 short distance → perturbative QCD
- 2 long distance → confinement
 $Q \sim \Lambda_{\text{QCD}} \simeq 250 \text{ MeV}$

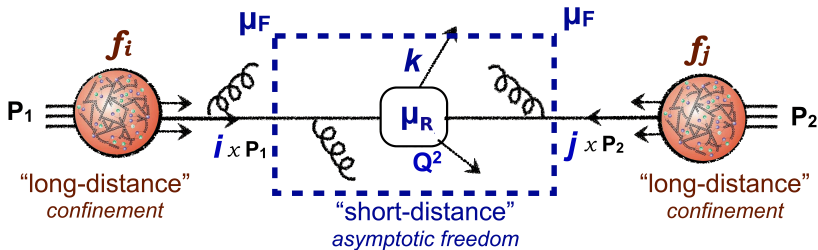
→ renormalization group equation (RGE)
 can be solved perturbatively



- long- and short-distance dynamics can be factorized at the scale μ_F



- long- and short-distance dynamics can be factorized at the scale μ_F
- convolution between proton (hadron) structure and partonic scattering



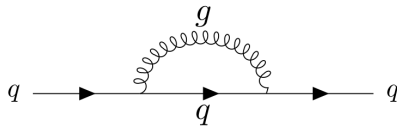
$$\sigma_{pp \rightarrow X} = \sum_{ij} f_i(x_1, \mu_F^2) \times f_j(x_2, \mu_F^2) \otimes \hat{\sigma}_{ij \rightarrow X}(x_1, x_2, \alpha_S(\mu_R), \frac{Q^2}{\mu_R}, \frac{Q^2}{\mu_F})$$

prediction proton structure partonic cross section (pQCD)

→ variations of μ_R and μ_F estimate size of missing higher-order terms

renormalization of m_q

- definition of m_q depends on renormalization procedure

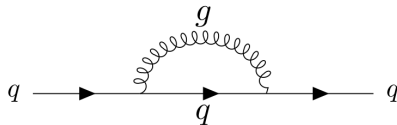


renormalization of m_q

- definition of m_q depends on renormalization procedure

on-shell (pole) scheme $\rightarrow m_q^{\text{pole}}$

- fundamental ambiguity $\mathcal{O}(\Lambda_{\text{QCD}})$



$$\frac{i}{\not{p} - m_0 - \delta m}$$

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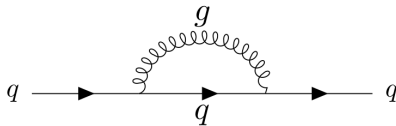
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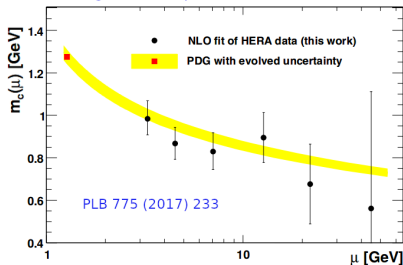
short distance ($\overline{\text{MS}}$) $\rightarrow m_q(\mu_R)$

- running of m_q described by renormalization group equations

- 1 test of perturbative QCD
- 2 indirect search for new physics



running of charm quark mass



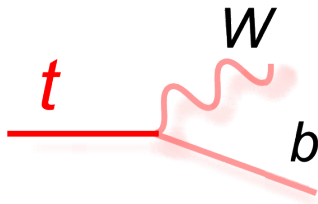
short lifetime $1/\Gamma_t \simeq 1/1.3 \text{ GeV} < 1/\Lambda_{\text{QCD}}$

⇒ top quarks decay before hadronizing

- study properties of unconfined quark
- clear experimental signature



large value of m_t



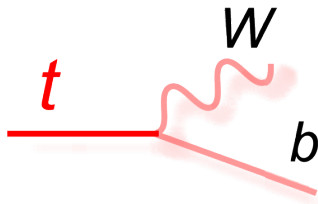
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large value of m_t \Rightarrow natural hard scale for pQCD calculations

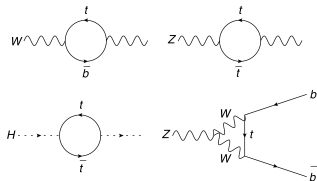


the role of the top quark mass

short lifetime $1/\Gamma_t \simeq 1/1.3 \text{ GeV} < 1/\Lambda_{\text{QCD}}$

⇒ top quarks decay before hadronizing

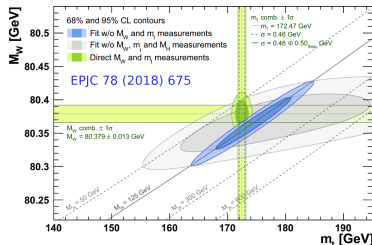
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- clear experimental signature



\Uparrow
large value of m_t ⇒ natural hard scale for pQCD calculations
 \Downarrow

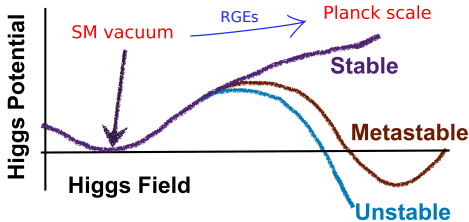
large corrections to electroweak observables

- values of m_t , m_W , m_H can be determined simultaneously via electroweak fits
- comparison with direct measurements provides self-consistency test of SM

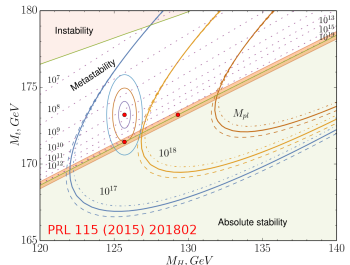
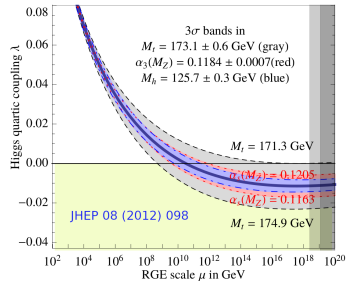


RGE evolution of Higgs self-quartic coupling λ depends on values of m_t , α_S , and m_H

⇒ sign of λ at Planck scale determines stability of electroweak vacuum



→ need precise measurements of m_t , α_S , m_H

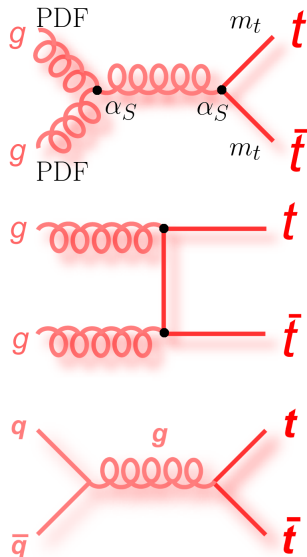
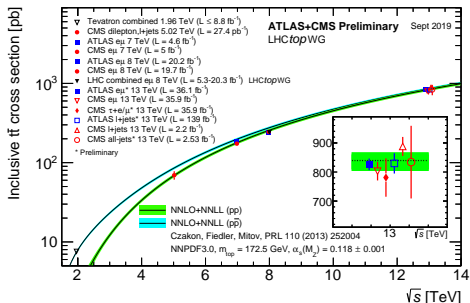


top quarks mainly produced in $t\bar{t}$ pairs

- 1 gluon fusion \rightarrow dominant at LHC
- 2 $q\bar{q}$ annihilation

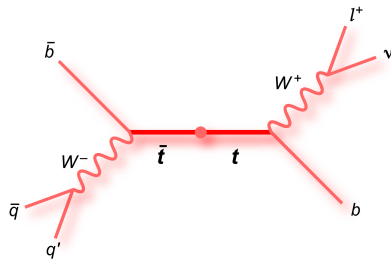
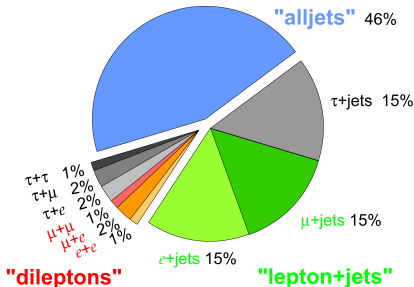
calculations of $\sigma_{t\bar{t}}$

- available up to NNLO+NNLL precision
- comparison with measurement is test of pQCD



$t\bar{t}$ final states are classified based on decays of W bosons

- 1 $W \rightarrow \ell \nu_\ell$: leptonic
- 2 $W \rightarrow q\bar{q}'$: hadronic



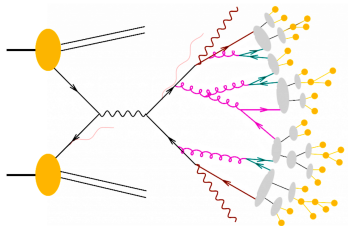
$t\bar{t}$ final states

- **fully hadronic**: large background
- **dileptonic**: clean signature
- **semileptonic**: intermediate properties

results obtained with in $e^\mp \mu^\pm$ channel
 \rightarrow highest signal purity

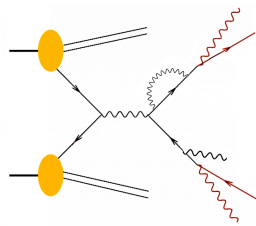
direct measurement: reconstruct invariant mass of top quark decay products

- compare to MC templates generated with different values of m_t



indirect determination: measure observable sensitive to m_t (e.g. $\sigma_{t\bar{t}}$)

- compare measured $\sigma_{t\bar{t}}$ to fixed-order calculations

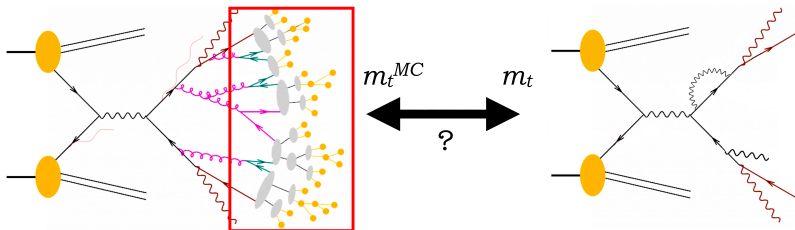


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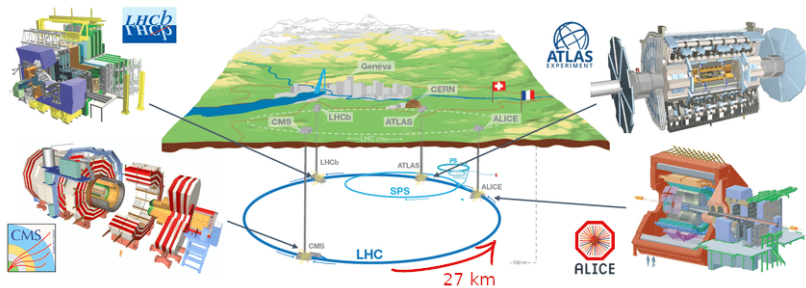
$$m_t^{\text{MC}} = m_t^{\text{pole}} \pm \Delta_{\text{MC}}$$

→ Δ_{MC} includes non-perturbative effects that are difficult to estimate
 e.g. [PRL 117 \(2016\) 232001](#)

**Measurement of the $t\bar{t}$ production
cross section at $\sqrt{s} = 13 \text{ TeV}$**

**and extraction of the top quark mass
and the strong coupling constant**

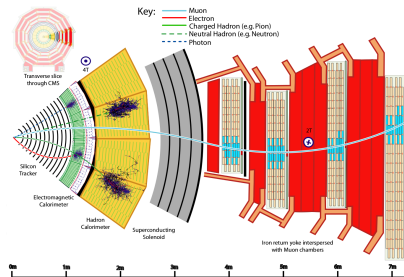
results obtained with pp collision data at $\sqrt{s} = 13$ TeV recorded by CMS in 2016



- superconducting accelerator at CERN laboratories in Geneva
- hadron-hadron collisions at the high-energy frontier, up to 13 TeV

the detector

- 3.8 T solenoidal magnetic field
- cylindrical layers around interaction point → particle discrimination

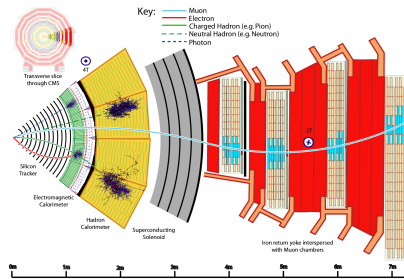


the detector

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- cylindrical layers around interaction point → particle discrimination

trigger system → select interesting events

- 1 L1: hardware → 100 kHz
- 2 high-level: software farm → $\mathcal{O}(\text{kHz})$



the detector

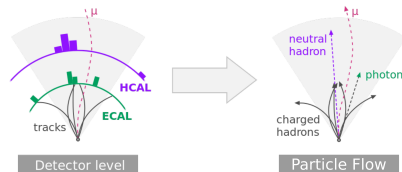
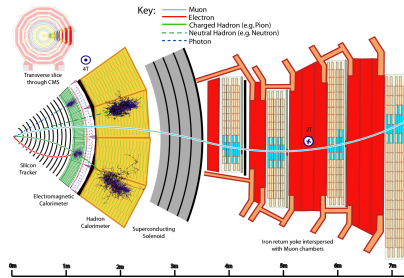
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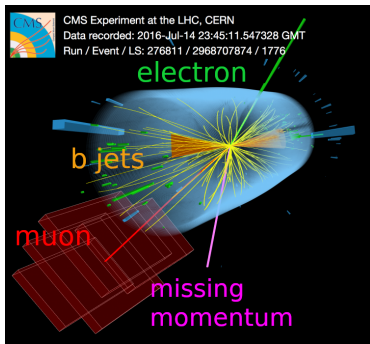
- 1 L1: hardware → 100 kHz
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offline reconstruction

- Particle Flow (PF) algorithm
- PF candidates clustered in jets
- b-jets reconstructed exploiting long lifetime of B hadrons



- $\mathcal{L} = 35.9 \text{ fb}^{-1}$, $\sqrt{s} = 13 \text{ TeV}$
- $t\bar{t} \rightarrow e^{\mp} \mu^{\pm} b\bar{b} \nu\bar{\nu}$

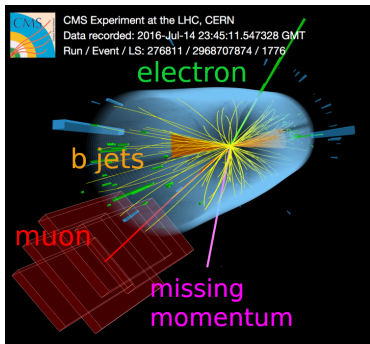


- missing p_T : escaping neutrinos
- possible additional jets

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visible phase space

- 1 detector geometry
- 2 selection of final-state objects



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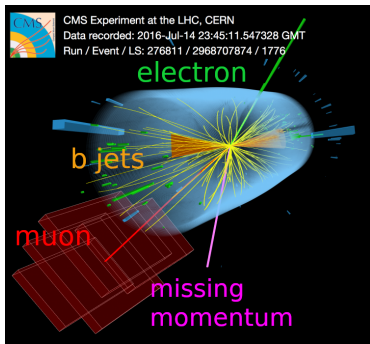
$$\sigma_{t\bar{t}}^{\text{vis}} = \frac{N_{\text{data}} - N_{\text{bkg}}}{\epsilon_{\text{sel}} \cdot \mathcal{L}_{\text{int}}}$$

$$\rightarrow \sigma_{t\bar{t}} = \frac{\sigma_{t\bar{t}}^{\text{vis}}}{A_{\text{sel}} \cdot \text{BR}(t\bar{t} \rightarrow e^\mp \mu^\pm)}$$

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selection acceptance A_{sel} :

- determined from simulation
- depends on assumed m_t^{MC}

\rightarrow dependence mitigated via **simultaneous measurement of $\sigma_{t\bar{t}}$ and m_t^{MC}**

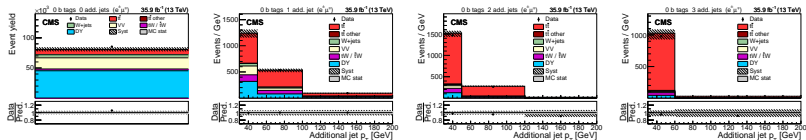
binned maximum-likelihood fit to multi-differential distributions

$$L(\sigma_{t\bar{t}}, m_t^{\text{MC}}, \vec{\lambda}) = \underbrace{\prod_i \frac{e^{-\nu_i} \nu_i^{n_i}}{n_i!}}_{\text{Poisson}} \underbrace{\prod_m \pi_m(\lambda_m)}_{\text{priors}}$$

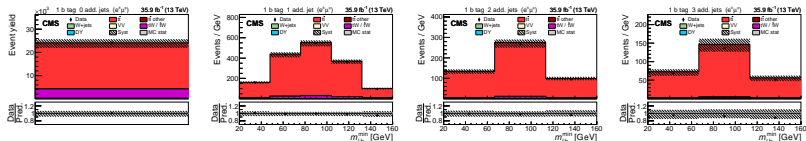
$$\nu_i = \underbrace{s_i(\sigma_{t\bar{t}}, m_t^{\text{MC}}, \vec{\lambda})}_{\text{signal}} + \underbrace{\sum_j b_j^i(\vec{\lambda})}_{\text{backgrounds}}$$

- systematic uncertainties ($\vec{\lambda}$) constrained using data
- signal and background contributions measured simultaneously

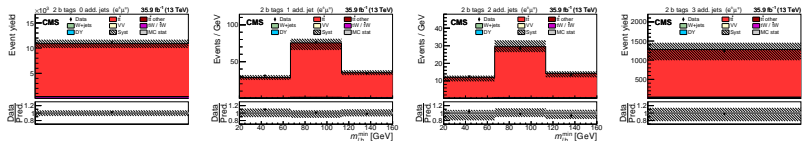
0 b-tags: 0,1,2,3 additional jets → jet p_T distribution: constrain jet energy scale



1 b-tag: 0,1,2,3 additional jets → $m_{\ell b}^{\min}$ distribution: sensitive to m_t^{MC}



2 b-tags: 0,1,2,3 additional jets → $m_{\ell b}^{\min}$ distribution: sensitive to m_t^{MC}



results for $\sigma_{t\bar{t}}$ at $\sqrt{s} = 13 \text{ TeV}$

$$\sigma_{t\bar{t}} = 815 \pm 2 \text{ (stat)} \pm 29 \text{ (syst)} \pm 20 \text{ (lum)} \text{ pb}$$

- total uncertainty: 4.3%
- among most precise results in CMS

main sources of uncertainty

- integrated luminosity (2.5%)
 - lepton identification (2.2%)
- } normalization

→ good agreement with theoretical prediction at NNLO+NNLL (Top++)

$$\sigma_{t\bar{t}}^{\text{th}} = 832 \pm_{29}^{20} \text{ (scale)} \pm 35 \text{ (PDF} + \alpha_S) \text{ pb}$$

Source	Uncertainty [%]
Trigger	0.4
Lepton ident./isolation	2.2
Muon momentum scale	0.2
Electron momentum scale	0.2
Jet energy scale	0.7
Jet energy resolution	0.5
b tagging	0.3
Pileup	0.3
t \bar{t} ME scale	0.5
tW ME scale	0.7
DY ME scale	0.2
NLO generator	1.2
PDF	1.1
m_t^{MC}	0.4
Top quark p_T	0.5
ME/PS matching	0.2
UE tune	0.3
t \bar{t} ISR scale	0.4
tW ISR scale	0.4
t \bar{t} FSR scale	1.1
tW FSR scale	0.2
b quark fragmentation	1.0
b hadron BF	0.2
Colour reconnection	0.4
DY background	0.8
tW background	1.1
Diboson background	0.3
W+jets background	0.3
t \bar{t} background	0.2
Statistical	0.2
Integrated luminosity	2.5
MC statistical	1.2
Total $\sigma_{t\bar{t}}^{\text{th}}$ uncertainty	4.2
Extrapolation uncertainties	
t \bar{t} ME scale	${}^{+0.4}_{-0.1}$
PDF	$\pm_{-0.6}^{+0.8}$
Top quark p_T	$\pm_{-0.3}^{+0.2}$
t \bar{t} ISR scale	${}^{+0.2}_{-0.1}$
t \bar{t} FSR scale	$\pm_{-0.1}^{+0.1}$
UE tune	$<_{-0.1}^{+0.1}$
m_t^{MC}	$\pm_{-0.3}^{+0.2}$
Total $\sigma_{t\bar{t}}$ uncertainty	${}^{+4.3}_{-4.2}$

$$m_t^{\text{MC}} = 172.33 \pm 0.14 \text{ (stat)} \pm_{0.72}^{0.66} \text{ (syst)} \text{ GeV}$$

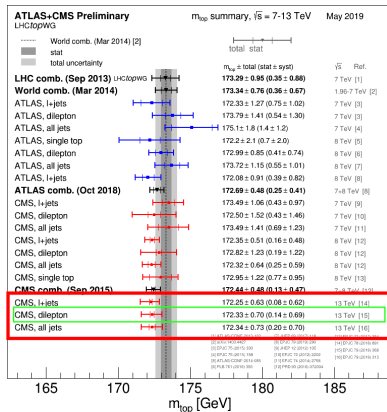
- total uncertainty: 0.41%
- correlation with $\sigma_{t\bar{t}}$: 12%

main sources of uncertainty

- jet energy scale (0.57 GeV)
- MC statistics (0.36 MeV)

} $m_{\ell b}^{\text{min}}$ shape

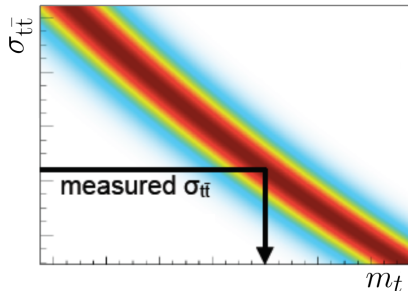
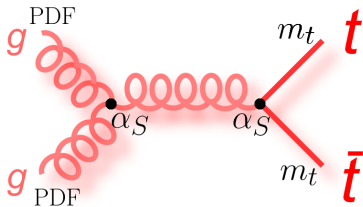
→ similar precision as dedicated analyses in ℓ +jets and fully-hadronic channels



extraction of m_t and α_S from inclusive $\sigma_{t\bar{t}}$

values of m_t and α_S extracted by comparing measured $\sigma_{t\bar{t}}$ to fixed-order calculations

- Hathor calculations at NNLO
- m_t defined in $\overline{\text{MS}}$ scheme
→ faster perturbative convergence

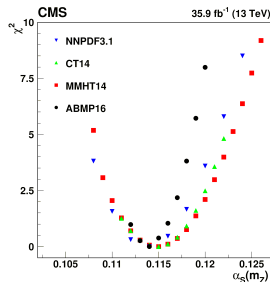


α_S and m_t cannot be determined simultaneously from measured $\sigma_{t\bar{t}}$

⇒ when extracting one, an assumption on the other (and PDFs) must be made

$\alpha_S(m_Z)$ determined via χ^2 fit of theoretical predictions to measured $\sigma_{t\bar{t}}$

- value of $\alpha_S(m_Z)$ consistently changed in calculation and PDFs
- several NNLO PDF sets considered
- m_t fixed to the value in PDF



extraction of $\alpha_S(m_Z)$ from $\sigma_{t\bar{t}}$

$\alpha_S(m_Z)$ determined via χ^2 fit of theoretical predictions to measured $\sigma_{t\bar{t}}$

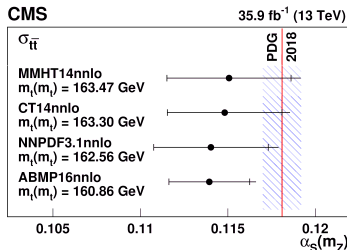
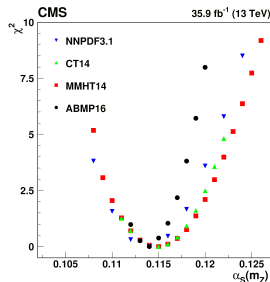
- value of $\alpha_S(m_Z)$ consistently changed in calculation and PDFs
- several NNLO PDF sets considered
- m_t fixed to the value in PDF

results

- precision of order 2-3%
- good agreement between different PDFs

$$\alpha_S(m_Z) = 0.1139^{+0.0027}_{-0.0023} \quad (\text{ABMP16})$$

→ **most precise NNLO result at hadron collider, to date**



extraction of $m_t(m_t)$ from $\sigma_{t\bar{t}}$

- same procedure used to extract top mass in \overline{MS} scheme, $m_t(m_t)$
- $\alpha_S(M_Z)$ fixed to values in PDF

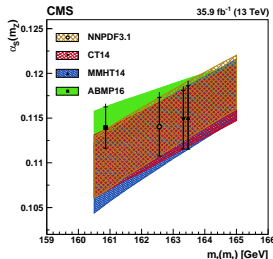
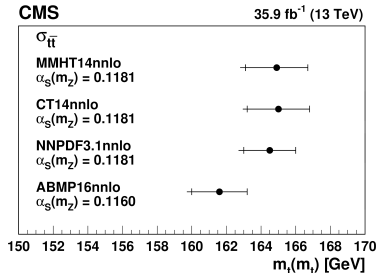
results

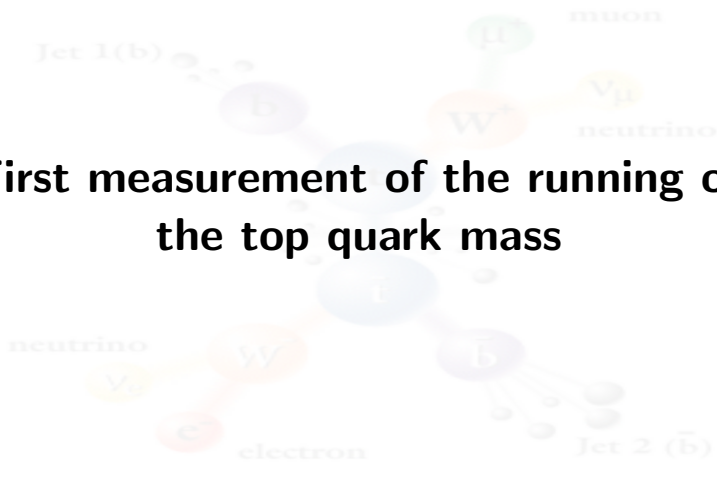
- uncertainty $\simeq 1.2\%$

$$m_t(m_t) = 161.6^{+1.6}_{-1.9} \text{ GeV (ABMP16)}$$

→ **first consistent and most precise determination of $m_t(m_t)$** , to date

- lower m_t result with ABMP16 due to lower $\alpha_S(m_Z)$ in PDFs
- linear dependence between α_S and m_t





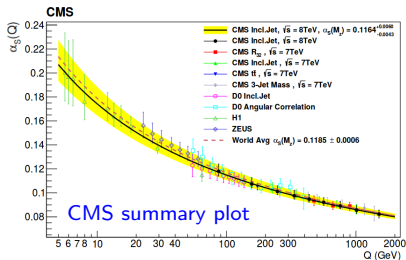
The background features a faded Feynman diagram of a top quark decay. A central blue circle labeled t (top quark) is connected to several particles: a purple circle labeled b (bottom quark) which leads to a grey cluster labeled "Jet 1(b)"; an orange circle labeled W^+ (W boson) which decays into a green circle labeled μ (muon) and a yellow circle labeled ν_μ (muon neutrino); a purple circle labeled \bar{b} (anti-bottom quark) which leads to a grey cluster labeled "Jet 2 (\bar{b})"; and an orange circle labeled W^0 (Z boson) which decays into a red circle labeled e^- (electron) and a yellow circle labeled ν_e (electron neutrino).

First measurement of the running of the top quark mass

example: **running of α_S**

- measure observable sensitive of α_S as a function of energy scale Q
- extract α_S in bins of Q
- compare $\alpha_S(Q)$ to RGE prediction

→ same procedure can be used to extract the running of m_t

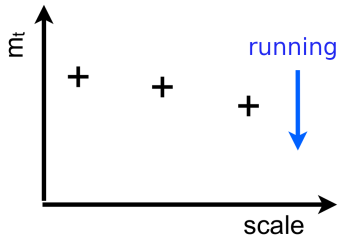
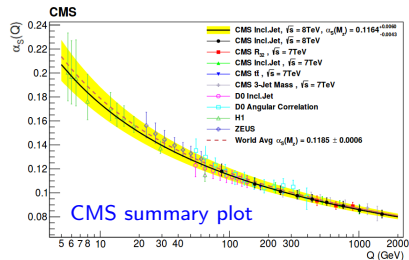


measurement of the running of m_t

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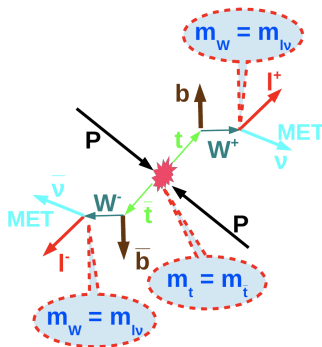
running of m_t : measure $m_t(\mu)$ as a function of the energy scale $\mu > m_t$

- observable = $\sigma_{t\bar{t}}$
 - $Q \rightarrow \mu = m_{t\bar{t}}$
- } $\Rightarrow d\sigma_{t\bar{t}}/dm_{t\bar{t}}$

→ natural extension of inclusive analysis

$m_{t\bar{t}}$ reconstruction

- kinematic reconstruction of $m_{t\bar{t}}^{\text{reco}}$
 - efficiency $\simeq 90\%$
 - resolution $\simeq 13\%$
- $m_{t\bar{t}}^{\text{reco}}$ unfolded to parton-level $m_{t\bar{t}}$

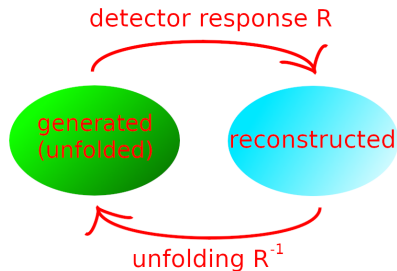


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solving the unfolding problem

estimate true spectrum using quantities measured in the detector



$m_{t\bar{t}}$ reconstruction

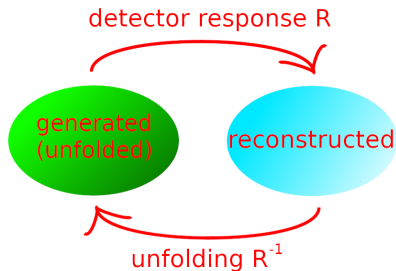
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solving the unfolding problem

estimate true spectrum using quantities measured in the detector

this analysis: **maximum-likelihood** method

- simultaneous fit of signal and background contributions
- systematic uncertainties constrained in the visible phase space

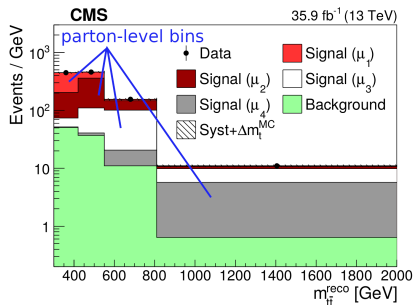


$$\mathcal{L}(\text{data} \mid \underbrace{d\sigma_{t\bar{t}}/dm_{t\bar{t}}}_{\text{determined directly at parton level}}, R)$$

determined directly at parton level

implementation of the unfolding

- $t\bar{t}$ simulation split into 4 subsamples in bins of parton-level $m_{t\bar{t}}$
- each subsample treated as an independent signal $\rightarrow d\sigma_{t\bar{t}}/dm_{t\bar{t}}$



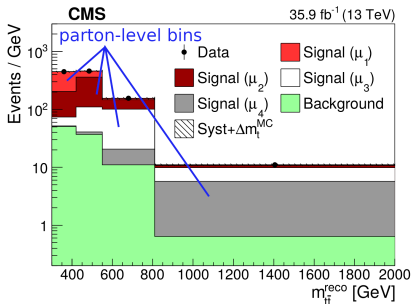
bin	range [GeV]	μ_k [GeV]
1	< 420	384
2	420-550	476
3	550-810	644
4	> 810	1024

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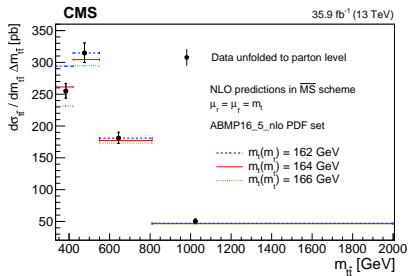
choice of the scale

- μ_k = centre-of-gravity of $m_{t\bar{t}}$
- final result does not depend on exact definition of μ_k



bin	range [GeV]	μ_k [GeV]
1	< 420	384
2	420-550	476
3	550-810	644
4	> 810	1024

result for $d\sigma_{t\bar{t}}/dm_{t\bar{t}}$ and extraction of $m_t(\mu)$

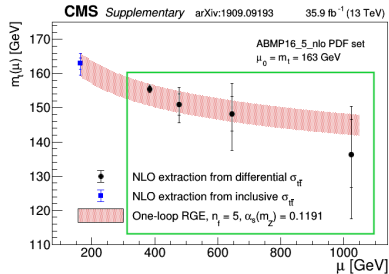
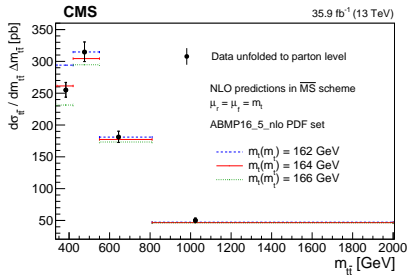


NLO predictions obtained with version of MCFM where m_t is treated in $\overline{\text{MS}}$ scheme

→ [EPJC 74 \(2014\) 3167](#)

- first top physics result obtained with rigorous likelihood-based unfolding
- **significantly improved precision** compared to other methods

result for $d\sigma_{t\bar{t}}/dm_{t\bar{t}}$ and extraction of $m_t(\mu)$

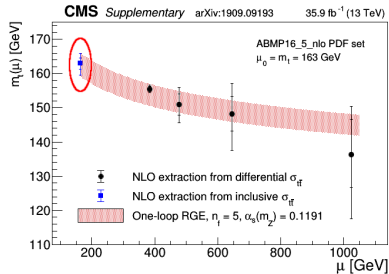
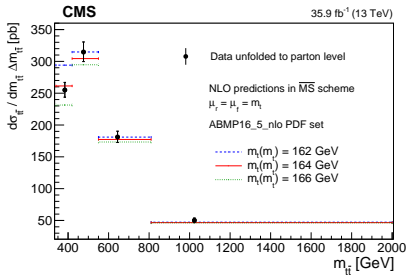


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- $m_t(m_t)$ extracted in each bin of $m_{t\bar{t}}$ independently via χ^2 fit
- $m_t(m_t)$ converted to $m_t(\mu_k)$ using one-loop RGE solutions

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- results compared to $m_t(m_t)$ obtained at NLO from inclusive $\sigma_{t\bar{t}}$

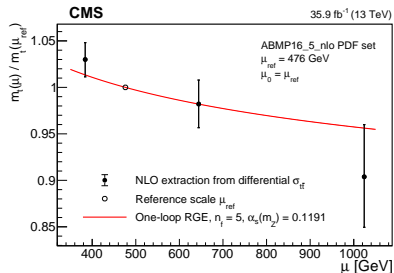
extraction of the running of m_t

running defined with respect to arbitrary reference scale $\mu_{\text{ref}} = \mu_2 = 476 \text{ GeV}$

$$\text{th: } r(\mu) = m_t(\mu) / m_t(\mu_{\text{ref}})$$

$$\text{exp: } r_k = m_t(\mu_k) / m_t(\mu_2)$$

- ① th: depends solely on RGE
- ② exp: benefits from cancellation of correlated uncertainties
- agreement with RGE prediction within 1.1 standard deviations
- no-running hypothesis excluded at $> 95\%$ confidence level



extraction of the running of m_t

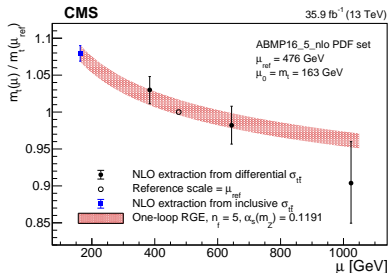
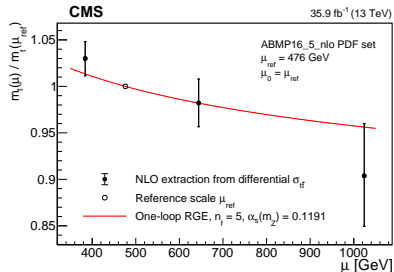
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- no-running hypothesis excluded at $> 95\%$ confidence level
- compared to $m_t(m_t) / m_t(\mu_{\text{ref}})$ as determined from inclusive $\sigma_{t\bar{t}}$

→ **running of a quark mass probed up to the TeV scale for the first time**

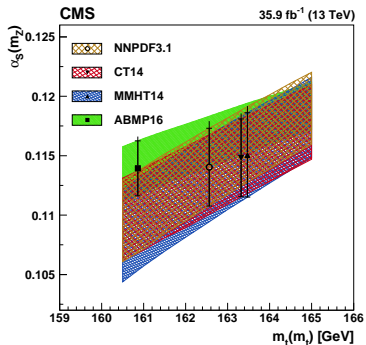




Measurement of the triple-differential $t\bar{t}$
production cross section at $\sqrt{s} = 13 \text{ TeV}$

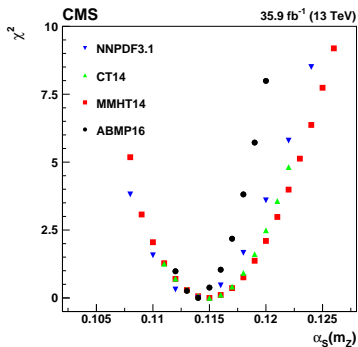
and global QCD analysis with HERA

DIS data: α_S , m_t , PDFs



inclusive cross section

- strong correlation between m_t and α_S
- modest dependence of α_S on PDFs

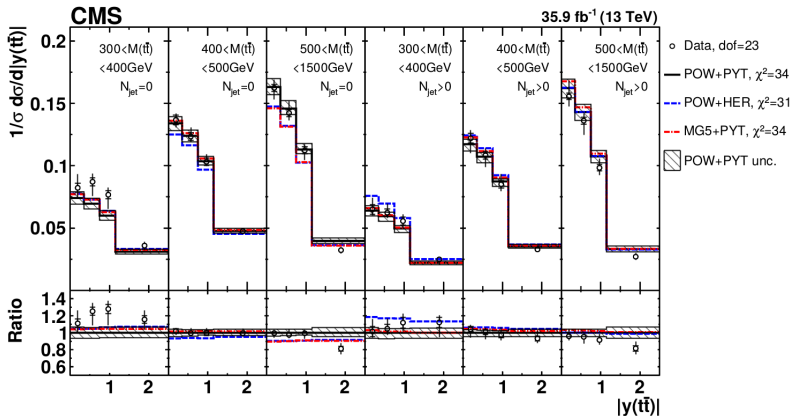


solution: simultaneous determination of QCD parameters and PDFs

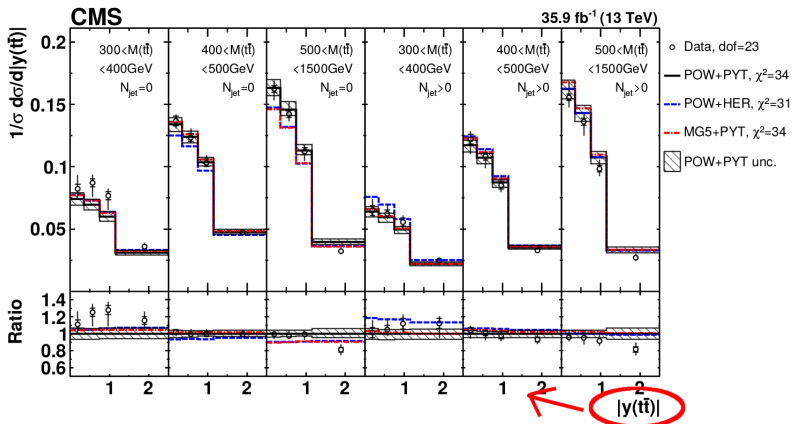
→ triple-differential $t\bar{t}$ cross section

normalized triple-differential $t\bar{t}$ cross section

- events in all di-leptonic channels ($e^\mp\mu^\pm$, e^+e^- , $\mu^+\mu^-$)
- more stringent event selection wrt inclusive/running analyses \rightarrow higher purity
- backgrounds are subtracted before χ^2 -based regularized unfolding

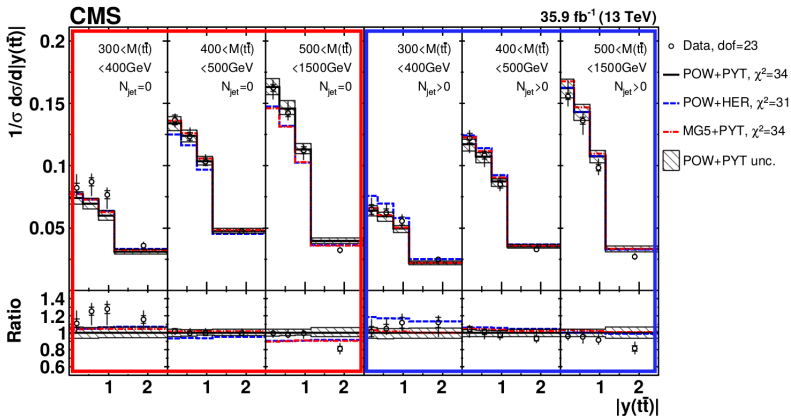


- measured as a function of $|\mathbf{y}(t\bar{t})|$, N_{jet} , $M(t\bar{t})$



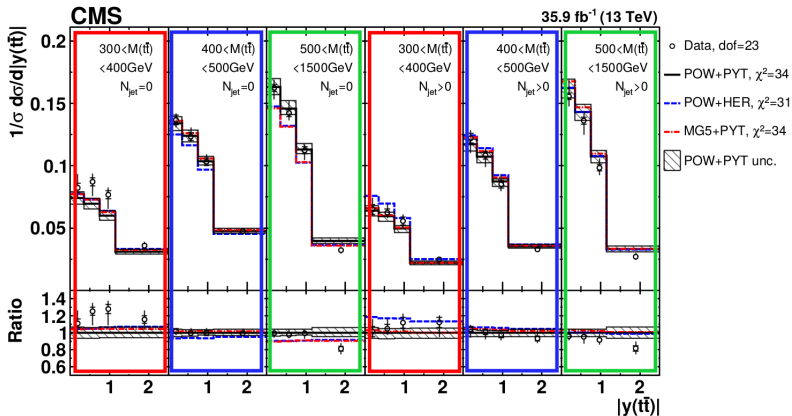
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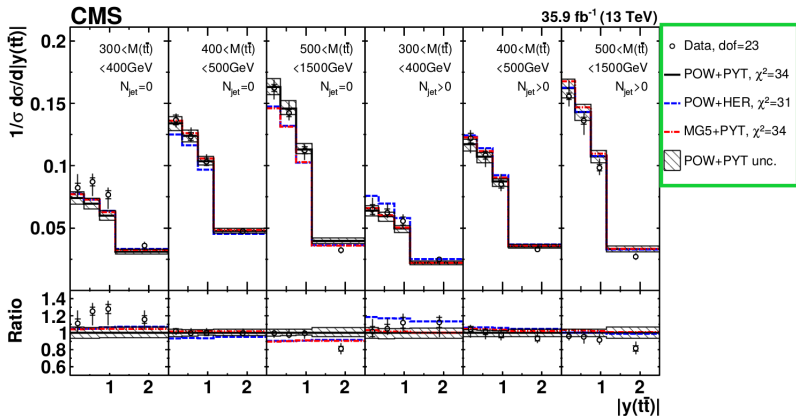
normalized triple-differential $t\bar{t}$ cross section

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normalized triple-differential $t\bar{t}$ cross section

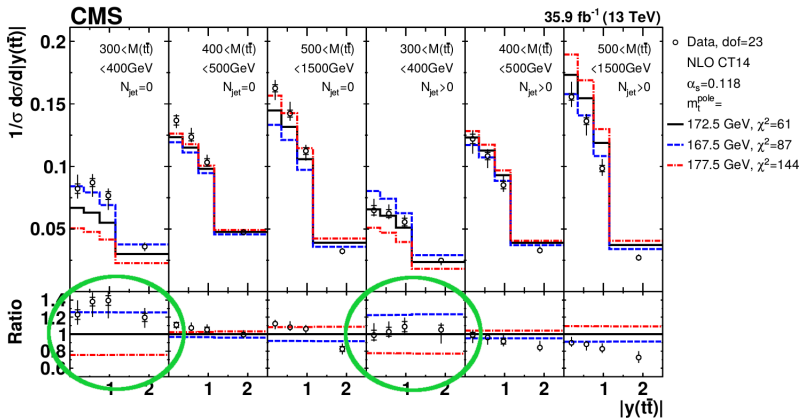
- measured as a function of $|y(t\bar{t})|$, N_{jet} , $M(t\bar{t})$
- particle-level result compared to different event generators



- 1 N_{jet} strongly dependent on value of α_S

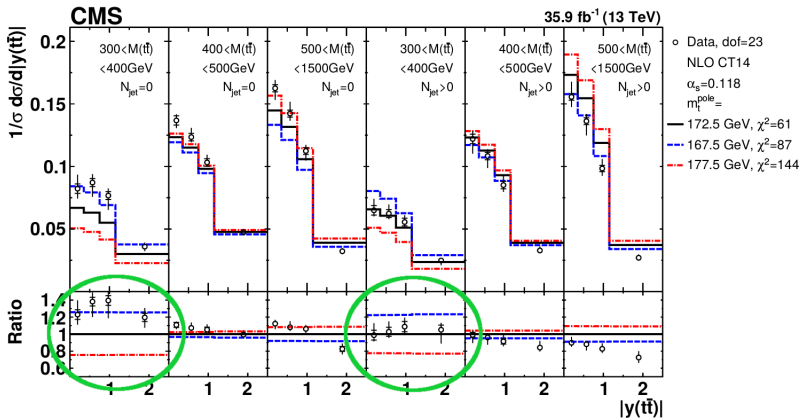
choice of variables

- 1 N_{jet} strongly dependent on value of α_S
- 2 threshold of $M(t\bar{t})$ sensitive to value of m_t



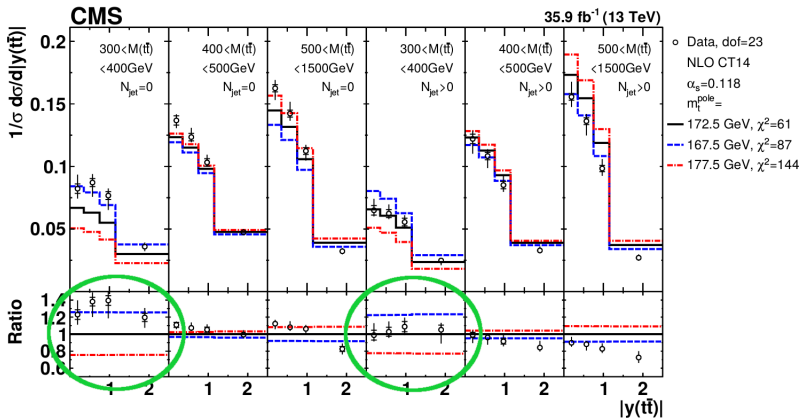
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- 3 at LO, $x_B = \frac{M(t\bar{t})}{\sqrt{s_{e^+e^-}(t\bar{t})}} \rightarrow$ (gluon) PDFs



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caveat: shape of threshold region affected by choice of m_t in kinematic reconstruction



loose kinematic reconstruction

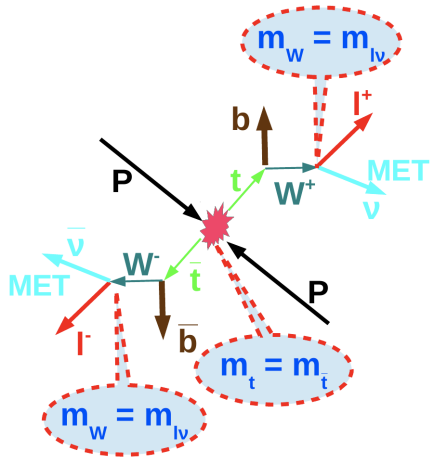
new kinematic reconstruction method developed for this analysis

full kinematic reconstruction

- separate reconstruction of t and \bar{t}
- m_t, m_W constraint

→ strong dependence on choice of m_t

however, chosen variables only depend on kinematic of $t\bar{t}$ system



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new kinematic reconstruction method developed for this analysis

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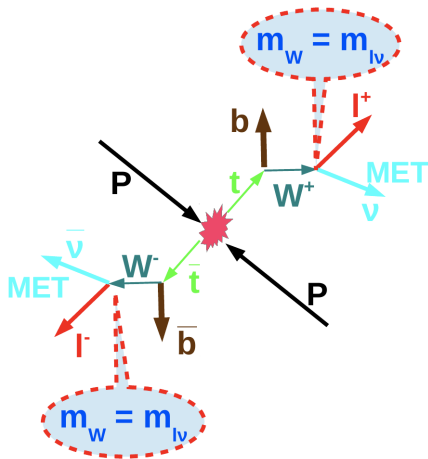
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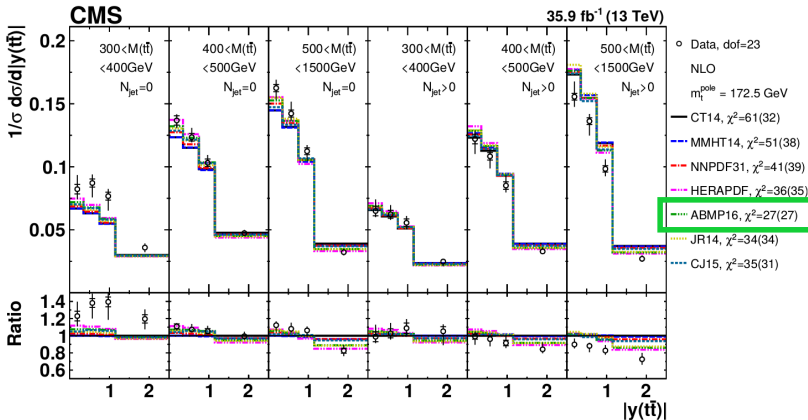
loose kinematic reconstruction

- reconstruction of $t\bar{t}$ system
- m_W constraint only

→ negligible dependence on m_t

→ similar performance as full kin. reco.





trends observed in all cases \Rightarrow $t\bar{t}$ data can bring significant improvements

NB: values of α_S , m_t often assumed in PDFs \Rightarrow important correlations neglected

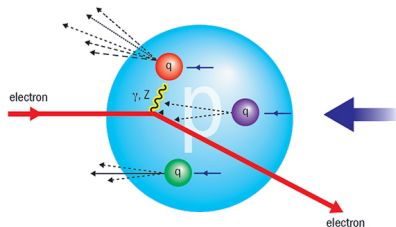
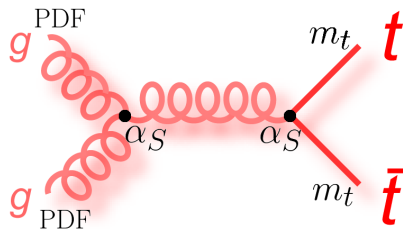
- simultaneous determination of $\alpha_S(m_Z)$, m_t^{pole} , proton PDFs
- fit to HERA + CMS $t\bar{t}$ data

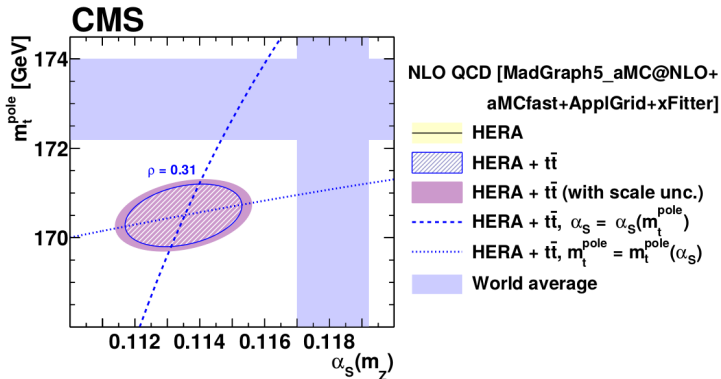
$t\bar{t}$ data

- mainly sensitive to gluon PDF
- sensitive to quark PDFs at large $M(t\bar{t})$

DIS data

- precise determination of quark PDFs
- gluon PDF mainly from scaling violation \rightarrow significant improvement expected with $t\bar{t}$ data

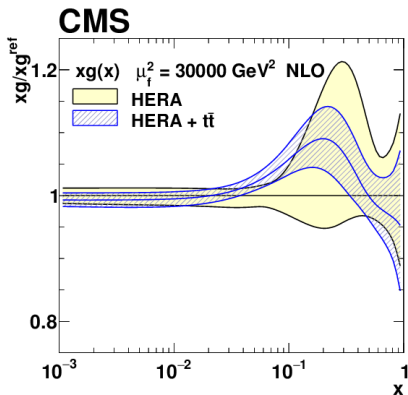




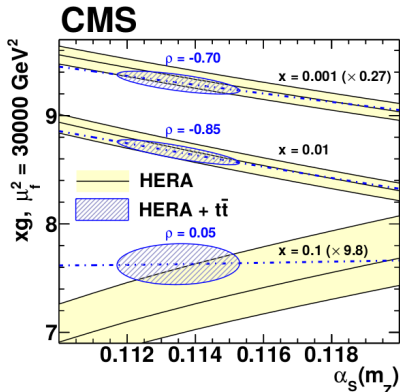
- results consistent with those from inclusive $\sigma_{t\bar{t}}$ (ABMP16)
- $m_t^{\text{pole}} = 170.5 \pm 0.8 \text{ GeV} \Rightarrow$ **most precise determination to date**

caveats

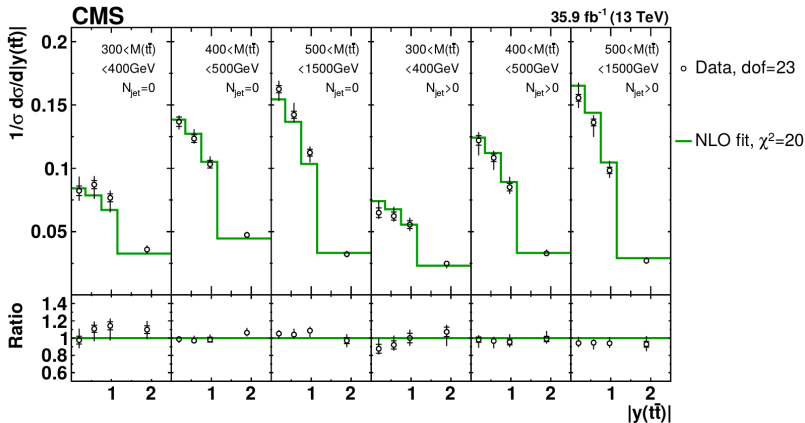
- results are obtained at NLO
- missing threshold corrections can have large effect on m_t^{pole} (order 1 GeV)



- uncertainty on gluon PDF significantly reduced in sensitive range ($x_B \simeq 0.1$)



- correlation between α_S and gluon PDF significantly mitigated



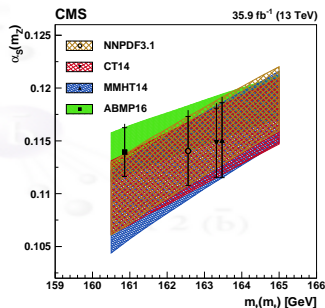
- remarkable agreement after the fit
→ improved wrt external PDFs
- benefits from proper account for correlation between QCD parameters

most recent CMS measurements of $t\bar{t}$ data used to probe pQCD

- simultaneous measurement of $\sigma_{t\bar{t}}$ and m_t^{MC}
 - determination of α_S and m_t at NNLO
- } → EPJC 79 (2019) 368
- ① most precise NNLO measurement of α_S at hadron collider
 - ② first consistent determination of $m_t(m_t)$ → 1.2% precision

possible improvements

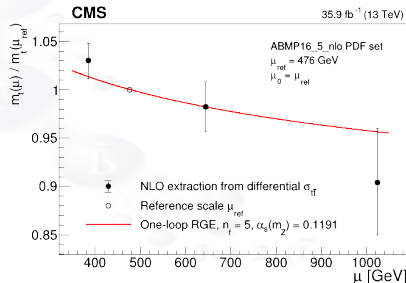
- luminosity and lepton ID uncertainties
- threshold resummation in $\overline{\text{MS}}$ scheme



- **first measurement of running of the top quark mass**
→ [PLB 803 \(2020\) 135263](#)
- investigated up to the TeV scale

possible improvements

- same as for inclusive analysis
- higher order calculations in $\overline{\text{MS}}$ scheme
- dynamic scales in calculation

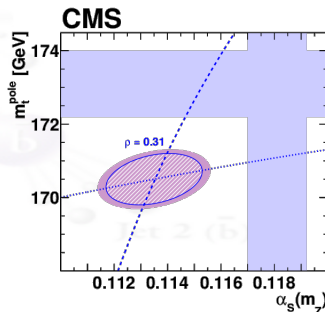


- global QCD analysis of CMS triple-differential $t\bar{t}$ cross section and HERA data → [arXiv:1904.05237](https://arxiv.org/abs/1904.05237) (accepted by EPJC)
- simultaneous determination of α_S , m_t , PDF

→ among most precise determination of QCD parameters are obtained
 → method takes all correlations into account

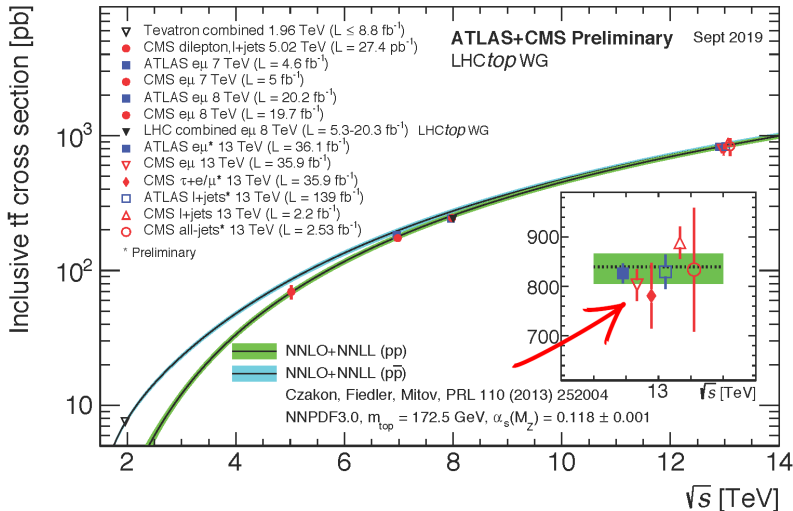
possible improvements

- theory predictions beyond NLO
 - will benefit from additional statistics collected during Run2 (x4) and upcoming Run3 (x10)
- better understanding of $t\bar{t}$ production near threshold needed

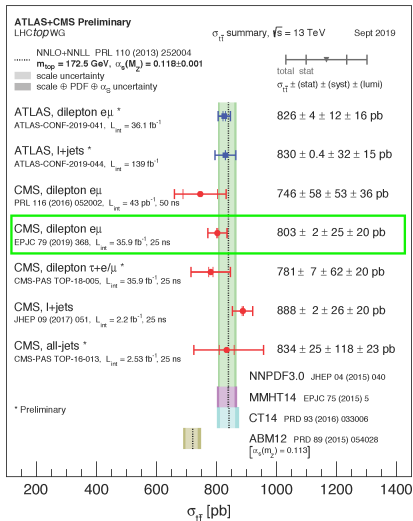


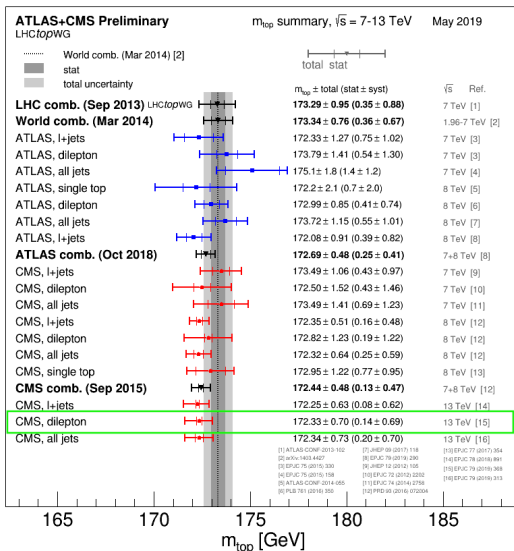
Thank you for your attention!

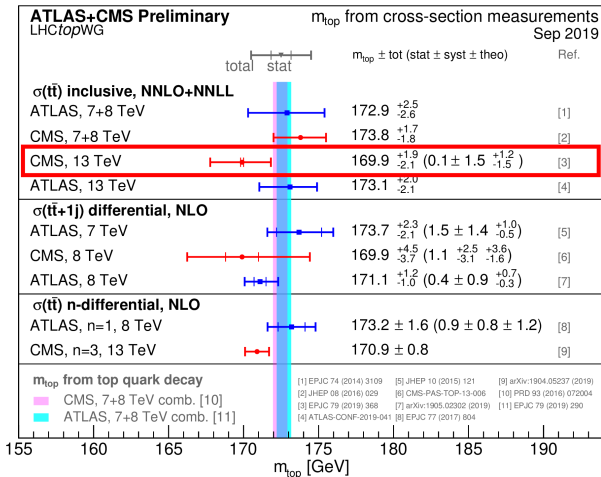


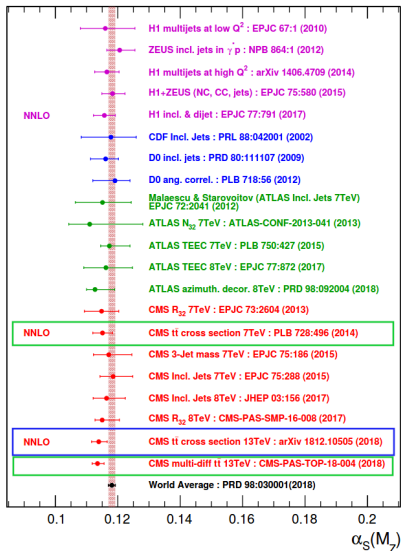


summary plot: $\sigma_{t\bar{t}}$ at 13 TeV









	ABMP16	NNPDF3.1	CT14	MMHT14
m_t^{pole} [GeV]	170.37	172.5	173.3	174.2
RUNDEC loops	3	2	2	3
$m_t(m_t)$ [GeV]	160.86	162.56	163.30	163.47
$\alpha_S(m_Z)$	0.116	0.118	0.118	0.118
α_S range	0.112–0.120	0.108–0.124	0.111–0.123	0.108–0.128

- CT14 does not use $t\bar{t}$ data
- CT14 and MMHT14: uncertainties provided only for nominal PDF

PDF set	$\alpha_S(m_Z)$
ABMP16	0.1139 ± 0.0023 (fit + PDF) $^{+0.0014}_{-0.0001}$ (scale)
NNPDF3.1	0.1140 ± 0.0033 (fit + PDF) $^{+0.0021}_{-0.0002}$ (scale)
CT14	0.1148 ± 0.0032 (fit + PDF) $^{+0.0018}_{-0.0002}$ (scale)
MMHT14	0.1151 ± 0.0035 (fit + PDF) $^{+0.0020}_{-0.0002}$ (scale)

PDF set	$m_t(m_t)$ [GeV]
ABMP16	161.6 ± 1.6 (fit + PDF + α_S) $^{+0.1}_{-1.0}$ (scale)
NNPDF3.1	164.5 ± 1.6 (fit + PDF + α_S) $^{+0.1}_{-1.0}$ (scale)
CT14	165.0 ± 1.8 (fit + PDF + α_S) $^{+0.1}_{-1.0}$ (scale)
MMHT14	164.9 ± 1.8 (fit + PDF + α_S) $^{+0.1}_{-1.1}$ (scale)

PDF set	m_t^{pole} [GeV]
ABMP16	169.9 ± 1.8 (fit + PDF + α_S) $^{+0.8}_{-1.2}$ (scale)
NNPDF3.1	173.2 ± 1.9 (fit + PDF + α_S) $^{+0.9}_{-1.3}$ (scale)
CT14	173.7 ± 2.0 (fit + PDF + α_S) $^{+0.9}_{-1.4}$ (scale)
MMHT14	173.6 ± 1.9 (fit + PDF + α_S) $^{+0.9}_{-1.4}$ (scale)

$t\bar{t}$ topology exploited to derive precise parametrization of normalization and shape uncertainties

$$S_{1b} = \mathcal{L} A_{\ell\ell} \sigma_{t\bar{t}} \epsilon_{\ell\ell} 2\epsilon_b (1 - C_b \epsilon_b)$$

$$S_{2b} = \mathcal{L} A_{\ell\ell} \sigma_{t\bar{t}} \epsilon_{\ell\ell} \epsilon_b^2 C_b$$

$$S_{\text{other}} = \mathcal{L} A_{\ell\ell} \sigma_{t\bar{t}} \epsilon_{\ell\ell} [1 - 2\epsilon_b (1 - C_b \epsilon_b) - \epsilon_b^2 C_b]$$

- $\epsilon_{\ell\ell}$ is the selection efficiency
 - ϵ_b is the b-tagging efficiency
 - C_b represents the residual correlation of tagging the two b-jets
-
- $A_{\ell\ell}$, $\epsilon_{\ell\ell}$, C_b , s_i , and b_i^j determined from simulation
 - they depend on $\vec{\lambda}$
 - b_i^j depends on ω_j
-
- S_b : normalization
 - s_i/S_b shape

$$\text{extrapol: } \frac{\Delta_i^\pm}{\sigma_{t\bar{t}}} = \left| 1 - \frac{A_i^{\text{fit}}}{A_i^\pm} \right|$$

$$\begin{aligned}
 S_{1b}^k &= \mathcal{L}\sigma_{t\bar{t}}^{(\mu_k)} A_{\text{sel}}^k \epsilon_{\text{sel}}^k 2\epsilon_b^k (1 - C_b^k \epsilon_b^k) \\
 S_{2b}^k &= \mathcal{L}\sigma_{t\bar{t}}^{(\mu_k)} A_{\text{sel}}^k \epsilon_{\text{sel}}^k C_b^k (\epsilon_b^k)^2 \\
 S_{\text{other}}^k &= \mathcal{L}\sigma_{t\bar{t}}^{(\mu_k)} A_{\text{sel}}^k \epsilon_{\text{sel}}^k [1 - 2\epsilon_b^k (1 - C_b^k \epsilon_b^k) - C_b^k (\epsilon_b^k)^2]
 \end{aligned}$$

same as in inclusive analysis, but for each bin of $m_{t\bar{t}}$ separately

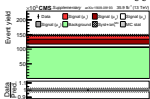
$$L = \prod_i \frac{e^{-\nu_i} \nu_i^{n_i}}{n_i!} \prod_j \pi(\omega_j) \prod_m \pi(\lambda_m)$$
$$\nu_i = \sum_{k=1}^4 s_i^k(\sigma_{t\bar{t}}^{(\mu_k)}, \vec{\lambda}, m_t^{\text{MC}}) + \sum_j b_i^j(\omega_j, \vec{\lambda})$$

ν_i incorporates the response matrix and its dependence on the nuisance parameters and m_t^{MC}

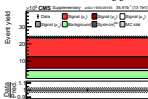
fit performed in categories of

- 1 b-tagged jet multiplicity
 - 2 m_{tt}^{reco} , including events with $N_{jets} \leq 2$
- $m_{\ell b}^{min} \rightarrow m_t^{MC}$ and m_t^{kin} (kin. reco)
 - jet $p_T \rightarrow JES$

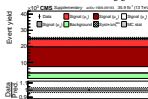
0 b-tags, no m_{tt}^{reco}



0 b-tags, m_{tt}^{reco} 1



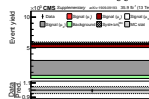
0 b-tags, m_{tt}^{reco} 2



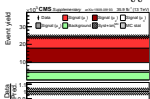
0 b-tags, m_{tt}^{reco} 3



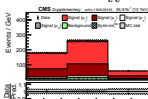
0 b-tags, m_{tt}^{reco} 4



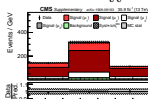
1 b-tag, no m_{tt}^{reco}



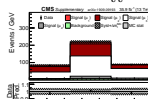
1 b-tag, m_{tt}^{reco} 1



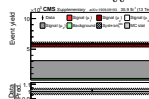
1 b-tag, m_{tt}^{reco} 2



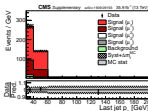
1 b-tag, m_{tt}^{reco} 3



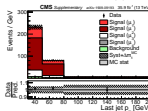
1 b-tag, m_{tt}^{reco} 4



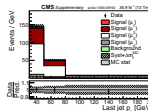
2 b-tags, m_{tt}^{reco} 1



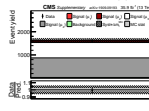
2 b-tags, m_{tt}^{reco} 2



2 b-tags, m_{tt}^{reco} 3



2 b-tags, m_{tt}^{reco} 4



“no m_{tt}^{reco} ” =
events with less
than 2 jets

