

# Geometry II

Makoto Asai (SLAC) Geant4 Tutorial Course

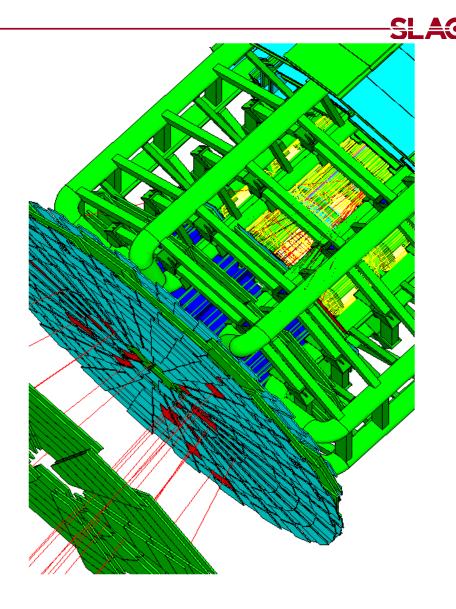






### Contents

- Various ways of placing volumes
  - Simple placement volume
  - Parameterized volume
  - Replicated volume
  - Divided volume
  - Nested parameterization
  - Reflected volume
  - Assembly volume
- Touchable







Physical volume



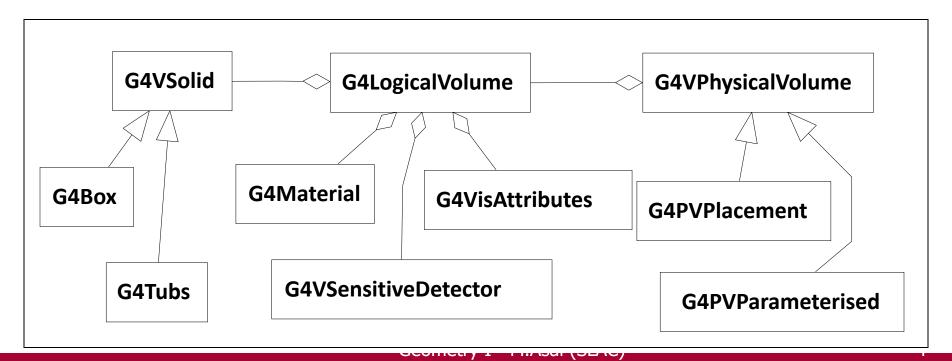




## **Detector geometry**



- Three conceptual layers
  - G4VSolid -- shape, size
  - G4LogicalVolume -- <u>daughter physical volumes</u>,
     material, sensitivity, user limits, etc.
  - G4VPhysicalVolume -- position, rotation

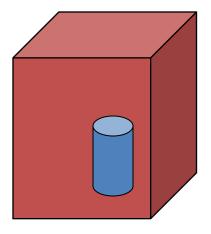




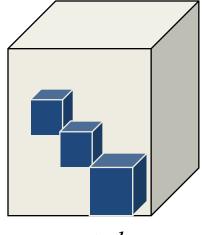
## Physical Volumes

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- Placement volume : it is one positioned volume
  - One physical volume object represents one "real" volume.
- Repeated volume : a volume placed many times
  - One physical volume object <u>represents</u> any number of "real" volumes.
  - reduces use of memory.
  - Parameterised
    - repetition w.r.t. copy number
  - Replica and Division
    - simple repetition along one axis
- A mother volume can contain either
  - many placement volumes
  - or, one repeated volume



placement



repeated



### Physical volume



- G4PVPlacement 1 Placement = One Placement Volume
  - A volume instance positioned once in its mother volume
- G4PVParameterised 1 Parameterized = Many Repeated Volumes
  - Parameterized by the copy number
    - Shape, size, material, sensitivity, vis attributes, position and rotation can be parameterized by the copy number.
    - You have to implement a concrete class of G4VPVParameterisation.
  - Reduction of memory consumption
  - Currently: parameterization can be used only for volumes that either
    - a) have no further daughters, or
    - b) are identical in size & shape (so that grand-daughters are safely fit inside).
  - By implementing G4PVNestedParameterisation instead of G4VPVParameterisation, material, sensitivity and vis attributes can be parameterized by the copy numbers of ancestors.



### Physical volume



G4PVReplica

- 1 Replica = Many Repeated Volumes
- Daughters of same shape are aligned along one axis
- Daughters fill the mother completely without gap in between.
- G4PVDivision

- 1 Division = Many Repeated Volumes
- Daughters of same shape are aligned along one axis and fill the mother.
- There can be gaps between mother wall and outmost daughters.
- No gap in between daughters.
- G4ReflectionFactory
   1 Placement = a pair of Placement volumes
  - generating placements of a volume and its reflected volume
  - Useful typically for end-cap calorimeter
- G4AssemblyVolume 1 Placement = a set of Placement volumes
  - Position a group of volumes



Parameterized volume



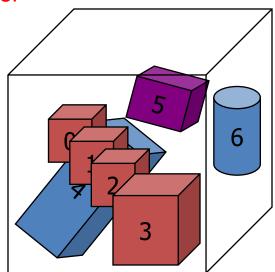




```
G4PVParameterised (const G4String& pName,
G4LogicalVolume* pLogical,
G4LogicalVolume* pMother,
const EAxis pAxis,
const G4int nReplicas,
G4VPVParameterisation* pParam
G4bool pSurfChk=false);
```

- Replicates the volume nReplicas times using the parameterization pParam, within the mother volume pMother
- paxis is a "suggestion" to the navigator along which Cartesian axis replication of parameterized volumes dominates.
  - kXAxis, kYAxis, kZAxis : one-dimensional optimization
  - kUndefined : three-dimensional optimization

- User should implement a class derived from G4VPVParameterisation abstract base class and define following as a function of copy number
  - where it is positioned (transformation, rotation)
- Optional:
  - the size of the solid (dimensions)
  - the type of the solid, material, sensitivity, vis attributes
- All daughters must be fully contained in the mother.
- Daughters should not overlap to each other.
- Limitations:
  - Applies to simple CSG solids only
  - Granddaughter volumes allowed only for special cases
  - Consider parameterised volumes as "leaf" volumes
- Typical use-cases
  - Complex detectors
    - with large repetition of volumes, regular or irregular
  - Medical applications
    - the material in animal tissue is measured as cubes with varying material



```
G4VSolid* solidChamber =
  new G4Box("chamber", 100*cm, 100*cm, 10*cm);
G4LogicalVolume* logicChamber =
  new G4LogicalVolume
   (solidChamber, ChamberMater, "Chamber", 0, 0, 0);
G4VPVParameterisation* chamberParam =
  new ChamberParameterisation();
G4VPhysicalVolume* physChamber =
  new G4PVParameterised("Chamber", logicChamber,
        logicMother, kZAxis, NbOfChambers, chamberParam);
```



```
class ChamberParameterisation : public G4VPVParameterisation
{
 public:
   ChamberParameterisation();
   virtual ~ChamberParameterisation();
  virtual void ComputeTransformation // position, rotation
     (const G4int copyNo, G4VPhysicalVolume* physVol) const;
  virtual void ComputeDimensions // size
     (G4Box& trackerLayer, const G4int copyNo,
         const G4VPhysicalVolume* physVol) const;
  virtual G4VSolid* ComputeSolid // shape
     (const G4int copyNo, G4VPhysicalVolume* physVol);
   virtual G4Material* ComputeMaterial // material, sensitivity, visAtt
     (const G4int copyNo, G4VPhysicalVolume* physVol,
         const G4VTouchable *parentTouch=0);
       // G4VTouchable should not be used for ordinary parameterization
};
```

## <u>G4VPVParameterisation: example</u>

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```
void ChamberParameterisation::ComputeTransformation
(const G4int copyNo, G4VPhysicalVolume* physVol) const
  G4double Xposition = ... // w.r.t. copyNo
  G4ThreeVector origin (Xposition, Yposition, Zposition);
  physVol->SetTranslation(origin);
  physVol->SetRotation(0);
void ChamberParameterisation::ComputeDimensions
(G4Box& trackerChamber, const G4int copyNo,
 const G4VPhysicalVolume* physVol) const
  G4double XhalfLength = ... // w.r.t. copyNo
  trackerChamber.SetXHalfLength(XhalfLength);
  trackerChamber.SetYHalfLength(YhalfLength);
  trackerChamber.SetZHalfLength(ZHalfLength);
```



## G4VPVParameterisation: example



```
G4VSolid* ChamberParameterisation::ComputeSolid
     (const G4int copyNo, G4VPhysicalVolume* physVol)
  G4VSolid* solid;
  if(copyNo == ...) solid = myBox;
  else if(copyNo == ...) solid = myTubs;
  return solid;
G4Material* ComputeMaterial // material, sensitivity, visAtt
     (const G4int copyNo, G4VPhysicalVolume* physVol,
         const G4VTouchable *parentTouch=0);
  G4Material* mat:
  if(copyNo == ...)
    mat = material1;
    physVol->GetLogicalVolume()->SetVisAttributes( att1 );
  return mat;
```





Replicated volume







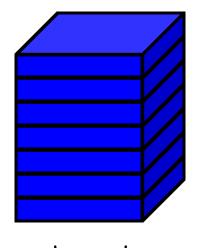
### Replicated Volumes



- The mother volume is completely filled with replicas, all of which are the same size (width) and shape.
- Replication may occur along:
  - Cartesian axes (X, Y, Z) slices are considered perpendicular to the axis of replication
    - Coordinate system at the center of each replica
  - Radial axis (Rho) cons/tubs sections centered on the origin and un-rotated
    - Coordinate system same as the mother
  - Phi axis (Phi) phi sections or wedges, of cons/tubs
     form
    - Coordinate system rotated such as that the X axis bisects the angle made by each wedge



a daughter logical volume to be replicated



mother volume



```
G4PVReplica(const G4String &pName,
G4LogicalVolume *pLogical,
G4LogicalVolume *pMother,
const EAxis pAxis,
const G4int nReplicas,
const G4double width,
const G4double offset=0.);
```

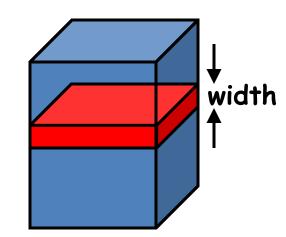
- offset may be used only for tube/cone segment
- Features and restrictions:
  - Replicas can be placed inside other replicas
  - Normal placement volumes can be placed inside replicas, assuming no intersection/overlaps with the mother volume or with other replicas
  - No volume can be placed inside a radial replication
  - Parameterised volumes cannot be placed inside a replica

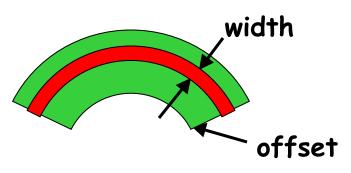


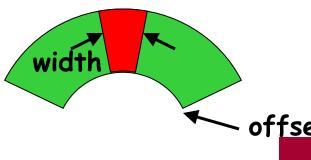
### Replica - axis, width, offset

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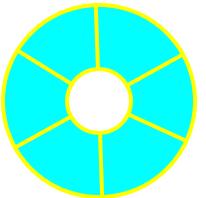
- Cartesian axes kXaxis, kYaxis, kZaxis
  - Center of n-th daughter is given as-width\*(nReplicas-1)\*0.5+n\*width
  - Offset shall not be used
- Radial axis kRaxis
  - Center of n-th daughter is given aswidth\* (n+0.5) +offset
  - Offset must be the inner radius of the mother
- Phi axis kPhi
  - Center of n-th daughter is given aswidth\* (n+0.5) +offset
  - Offset must be the starting angle of the mother







```
G4double tube dPhi = 2.* M PI * rad;
G4VSolid* tube =
   new G4Tubs("tube",20*cm,50*cm,30*cm,0.,tube dPhi);
G4LogicalVolume * tube log =
   new G4LogicalVolume(tube, Air, "tubeL", 0, 0, 0);
G4VPhysicalVolume* tube phys =
   new G4PVPlacement(0,G4ThreeVector(-200.*cm,0.,0.),
            "tubeP", tube log, world phys, false, 0);
G4double divided tube dPhi = tube dPhi/6.;
G4VSolid* div tube =
   new G4Tubs ("div tube", 20*cm, 50*cm, 30*cm,
        -divided tube dPhi/2., divided tube dPhi);
G4LogicalVolume* div tube log =
   new G4LogicalVolume(div tube, Pb, "div tubeL", 0, 0, 0);
G4VPhysicalVolume* div tube phys =
   new G4PVReplica ("div tube phys", div tube log,
   tube log, kPhi, 6, divided tube dPhi);
```







Divided volume



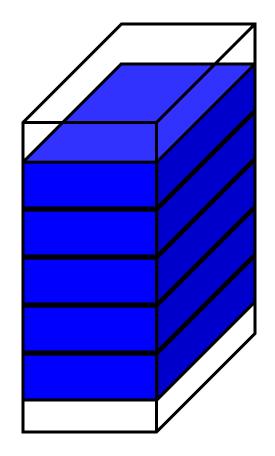




#### **G4PVDivision**



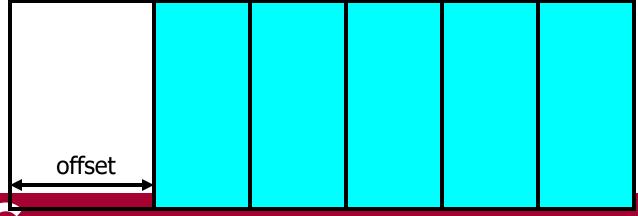
- G4PVDivision is a special kind of G4PVParameterised.
  - G4VPVParameterisation is automatically generated according to the parameters given in G4PVDivision.
- G4PVDivision is similar to G4PVReplica but
  - It currently allows gaps in between mother and daughter volumes
  - We are extending G4PVDivision to allow gaps between daughters, and also gaps on side walls. We plan to release this extension in near future.
- Shape of all daughter volumes must be same shape as the mother volume.
  - G4VSolid (to be assigned to the daughter logical volume)
     must be the same type, but different object.
- Replication must be aligned along one axis.
- If your geometry does not have gaps, use G4Replica.
  - For identical geometry, navigation of G4Replica is faster.



mother volume

```
G4PVDivision(const G4String& pName,
G4LogicalVolume* pDaughterLogical,
G4LogicalVolume* pMotherLogical,
const EAxis pAxis,
const G4int nDivisions, // number of division is given
const G4double offset);
```

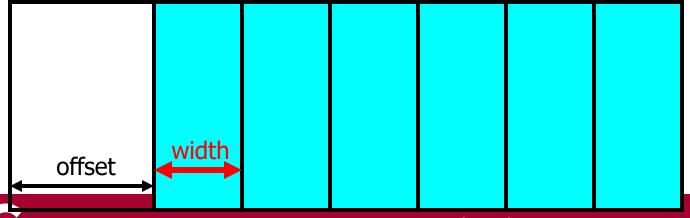
The size (width) of the daughter volume is calculated as
 (size of mother) - offset ) / nDivisions





```
G4PVDivision(const G4String& pName,
G4LogicalVolume* pDaughterLogical,
G4LogicalVolume* pMotherLogical,
const EAxis pAxis,
const G4double width, // width of daughter volume is given const G4double offset);
```

- The number of daughter volumes is calculated as
   int( (size of mother) offset ) / width )
  - As many daughters as width and offset allow

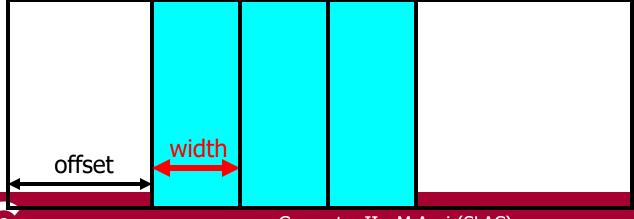


#### G4PVDivision - 3



```
G4PVDivision(const G4String& pName,
G4LogicalVolume* pDaughterLogical,
G4LogicalVolume* pMotherLogical,
const EAxis pAxis,
const G4int nDivisions,
const G4double width, // both number of division and width are given const G4double offset);
```

nDivisions daughters of width thickness



#### **G4PVDivision**



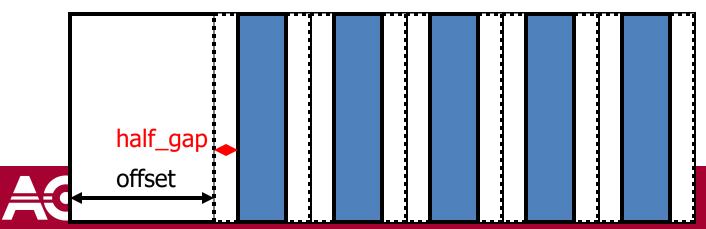
- G4PVDivision currently supports following shapes / axes.
  - G4Box: kXAxis, kYAxis, kZAxis
  - G4Tubs : kRho, kPhi, kZAxis
  - G4Cons : kRho, kPhi, kZAxis
  - G4Trd: kXAxis, kYAxis, kZAxis
  - G4Para: kXAxis, kYAxis, kZAxis
  - G4Polycone : kRho, kPhi, kZAxis
    - kZAxis the number of divisions has to be the same as solid sections,
       (i.e. numZPlanes-1), the width will not be taken into account.
  - G4Polyhedra : kRho, kPhi, kZAxis
    - kPhi the number of divisions has to be the same as solid sides, (i.e. numSides), the width will not be taken into account.
    - kZAxis the number of divisions has to be the same as solid sections,
       (i.e. numZPlanes-1), the width will not be taken into account.
- In the case of division along kRho of G4Cons, G4Polycone, G4Polyhedra, if width is provided, it is taken as the width at the -Z radius; the width at other radii will be scaled to this one.



### G4ReplicatedSlice



- New extension of G4Division introduced with version 9.4.
- It allows gaps in between divided volumes.
  - G4PVDivision(const G4String& pName, G4LogicalVolume\* pDaughterLogical, G4LogicalVolume\* pMotherLogical, const EAxis pAxis,
    - const G4int nDivisions, const G4double half\_gap, const G4double offset);
  - G4PVDivision(const G4String& pName, G4LogicalVolume\* pDaughterLogical, G4LogicalVolume\* pMotherLogical, const EAxis pAxis,
    - const G4double width, const G4double half\_gap, const G4double offset);
  - G4PVDivision(const G4String& pName, G4LogicalVolume\* pDaughterLogical,
    - G4LogicalVolume\* pMotherLogical, const EAxis pAxis,
    - const G4int nDivisions, const G4double width,
    - const G4double half\_gap, const G4double offset);





Nested parameterization



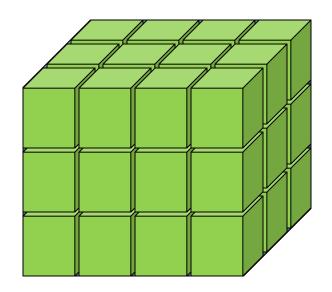


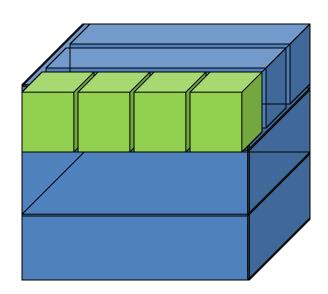


### Nested parameterization



- Suppose your geometry has three-dimensional regular reputation of same shape and size of volumes without gap between volumes. And material of such volumes are changing according to the position.
  - ▶ E.g. voxels made by CT Scan data (DICOM)
- Instead of direct three-dimensional parameterized volume,
   use replicas for the first and second axes sequentially, and then use one-dimensional parameterization along the third axis.



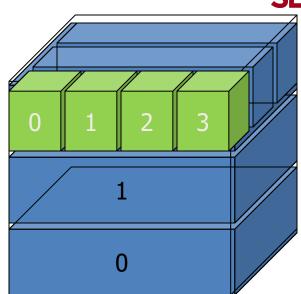


It requires much less memory for geometry optimization and gives much faster navigation for ultra-large number of voxels.

## Nested parameterization

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- Given geometry is defined as two sequential replicas and then one-dimensional parameterization,
  - Material of a voxel must be parameterized not only by the copy number of the voxel, but also by the copy numbers of ancestors.
  - Material is indexed by three indices.



- G4VNestedParameterisation is a special parameterization class derived from G4VPVParameterisation base class.
  - ComputeMaterial() method of G4VNestedParameterisation has a touchable object of the parent physical volume, in addition to the copy number of the voxel.
    - Index of first axis = theTouchable->GetCopyNumber(1);
    - Index of second axis = theTouchable->GetCopyNumber(0);
    - Index of third axis = copy number

#### G4VNestedParameterisation



- G4VNestedParameterisation is derived from G4VPVParameterization.
- G4VNestedParameterisation class has three pure virtual methods you have to implement,
  - in addition to ComputeTransformation() method, which is mandatory for all G4VPVParameterization classes.

virtual G4Material\* ComputeMaterial(G4VPhysicalVolume \*currentVol, const G4int repNo, const G4VTouchable \*parentTouch=0)=0;

- Return a material pointer w.r.t. copy numbers of itself and ancestors.
- Must cope with parentTouch=0 for navigator's sake. Typically, return a default material if parentTouch=0.

#### virtual G4int GetNumberOfMaterials() const=0;

 Return total number of materials which may appear as the return value of ComputeMaterial() method.

#### virtual G4Material\* GetMaterial(G4int idx) const=0;

- Return idx-th material.
- "idx" is not a copy number. idx = [0, nMaterial-1]



#### G4VNestedParameterisation



- G4VNestedParameterisation is a kind of G4VPVParameterization.
  - It can be used as an argument of G4PVParameterised.
  - All other arguments of G4PVParameterised are unaffected.
- Nested parameterization of placement volume is not supported.
  - All levels used as indices of material must be repeated volume.
     There cannot be a level of placement volume in between.





Assembly volume



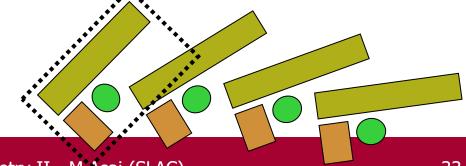




### **Grouping volumes**



- To represent a regular pattern of positioned volumes, composing a more or less complex structure
  - structures which are hard to describe with simple replicas or parameterised volumes
  - structures which may consist of different shapes
  - Too densely positioned to utilize a mother volume
- Assembly volume
  - acts as an envelope for its daughter volumes
  - its role is over once its logical volume has been placed
  - daughter physical volumes become independent copies in the final structure
- Participating daughter logical volumes are treated as triplets
  - logical volume
  - translation w.r.t. envelop
  - rotation w.r.t. envelop





- Helper class to combine daughter logical volumes in arbitrary way
  - Imprints of the assembly volume are made inside a mother logical volume through G4AssemblyVolume::MakeImprint(...)
  - Each physical volume name is generated automatically
    - Format: av\_WWW\_impr\_XXX\_YYY\_ZZZ
      - www assembly volume instance number
      - xxx assembly volume imprint number
      - YYY name of the placed logical volume in the assembly
      - zzz index of the associated logical volume
  - Generated physical volumes (and related transformations) are automatically managed (creation and destruction)



## G4AssemblyVolume : example



```
G4AssemblyVolume* assembly = new G4AssemblyVolume();
G4RotationMatrix Ra;
G4ThreeVector Ta;
Ta.setX(...); Ta.setY(...); Ta.setZ(...);
assembly->AddPlacedVolume( plateLV, Ta, Ra );
  ... // repeat placement for each daughter
for( unsigned int i = 0; i < layers; i++ ) {</pre>
  G4RotationMatrix Rm(...);
  G4ThreeVector Tm(...);
  assembly->MakeImprint( worldLV, Tm, Rm );
```





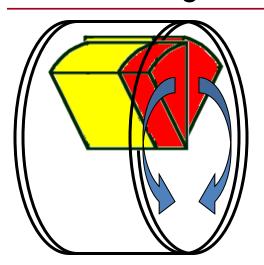
Reflected volume



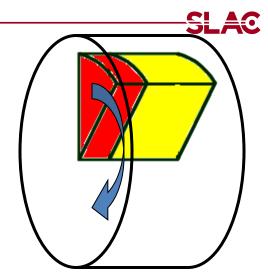




## Reflecting solids



- Let's take an example of a pair of mirror symmetric volumes.
- Such geometry cannot be made by parallel transformation or 180 degree rotation.



- G4ReflectedSolid (derived from G4VSolid)
  - Utility class representing a solid shifted from its original reference frame to a new mirror symmetric one
  - The reflection (G4Reflect[X/Y/Z]3D) is applied as a decomposition into rotation and translation
- G4ReflectionFactory
  - Singleton object using G4ReflectedSolid for generating placements of reflected volumes
- Reflections are currently limited to simple CSG solids.
  - will be extended soon to all solids



## Reflecting hierarchies of volumes - 1

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#### G4PhysicalVolumesPair G4ReflectionFactory::Place

- Used for normal placements:
  - i. Performs the transformation decomposition
  - ii. Generates a new reflected solid and logical volume
    - Retrieves it from a map if the reflected object is already created
  - iii. Transforms any daughter and places them in the given mother
  - iv. Returns a pair of physical volumes, the second being a placement in the reflected mother
- G4PhysicalVolumesPair is
  std::map<G4VPhysicalVolume\*,G4VPhysicalVolume\*>



# Reflecting hierarchies of volumes - 2



#### G4PhysicalVolumesPair G4ReflectionFactory::Replicate

- Creates replicas in the given mother volume
- Returns a pair of physical volumes, the second being a replica in the reflected mother





Touchable







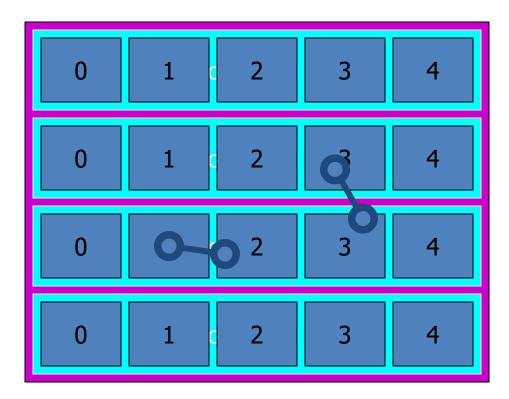
### Step point and touchable



- As mentioned already, G4Step has two G4StepPoint objects as its starting and ending points. All the geometrical information of the particular step should be taken from "PreStepPoint".
  - Geometrical information associated with G4Track is identical to "PostStepPoint".
- Each G4StepPoint object has
  - Position in world coordinate system
  - Global and local time
  - Material
  - G4TouchableHistory for geometrical information
- G4TouchableHistory object is a vector of information for each geometrical hierarchy.
  - copy number
  - transformation / rotation to its mother
- Since release 4.0, handles (or smart-pointers) to touchables are intrinsically used.
   Touchables are reference counted.



- Suppose a calorimeter is made of 4x5 cells.
  - and it is implemented by two levels of replica.
- In reality, there is only one physical volume object for each level. Its position is parameterized by its copy number.
- To get the copy number of each level, suppose what happens if a step belongs to two cells.



- Remember geometrical information in G4Track is identical to "PostStepPoint".
- You cannot get the correct copy number for "PreStepPoint" if you directly access to the physical volume.
- Use touchable to get the proper copy number, transform matrix, etc.

G4TouchableHistory has information of geometrical hierarchy of the point.

```
G4Step* aStep;
G4StepPoint* preStepPoint = aStep->GetPreStepPoint();
G4TouchableHistory* theTouchable =
    (G4TouchableHistory*) (preStepPoint->GetTouchable());
G4int copyNo = theTouchable->GetVolume()->GetCopyNo();
G4int motherCopyNo
            = theTouchable->GetVolume(1)->GetCopyNo();
G4int grandMotherCopyNo
            = theTouchable->GetVolume(2)->GetCopyNo();
G4ThreeVector worldPos = preStepPoint->GetPosition();
G4ThreeVector localPos = theTouchable->GetHistory()
    ->GetTopTransform().TransformPoint(worldPos);
```