CPV and Leptogenesis

1. mixing matrix phases +
   leptonic unitarity triangle

2. leptogenesis in the type 1 seesaw

U

leptonic mixing matrix (lives in generation space ; rotates from charged lepton α to neutrino i) with three angles (index order reversed wrt quarks) :

$$
\begin{aligned}
U_{\alpha i} &= \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} P \\
&= \begin{bmatrix} c_{12}c_{13} & c_{13}s_{12} & s_{13}e^{-i\delta} \\ -c_{23}s_{12} - c_{12}s_{13}s_{23}e^{i\delta} & c_{12}c_{23} - s_{12}s_{13}s_{23}e^{i\delta} & c_{13}s_{23} \\ s_{23}s_{12} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - c_{23}s_{12}s_{13}e^{i\delta} & c_{13}c_{23} \end{bmatrix} P
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$$

P = diag$\{e^{-i\phi_1/2}, e^{-i\phi_2/2}, 1\}$ for Majorana, identity for Dirac

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$$\theta_{23} \simeq \pi/4 \quad \theta_{12} \simeq \pi/6 \quad \theta_{13} \simeq 0.15, 8^o \quad \delta \sim 1.4\pi$$

(global fits of www.nu-fit.org)

for comparaison, in CKM :

$$\theta_{23} \simeq V_{cb} \simeq 0.04 \quad \theta_{12} \simeq V_{us} \simeq 0.225 \quad \theta_{13} \simeq V_{ub} \simeq 0.004$$

The drunken Unitarity triangle

Not hear much about "leptonic unitarity triangle"
1.not measure elements at tree in CC
2. Also, it drinks.

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Amplitude to oscillate from flavour α to β over distance L :

$$\mathcal{A}_{\alpha\beta}(L) = U_{\alpha 1} U^*_{\beta 1} + U_{\alpha 2} U^*_{\beta 2} e^{-i(m_2^2 - m_1^2)L/(2E)} + U_{\alpha 3} U^*_{\beta 3} e^{-i(m_3^2 - m_1^2)L/(2E)}$$

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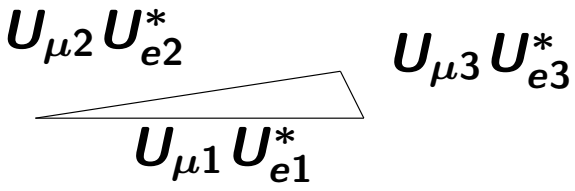
at $L = 0$ unitarity : $\Rightarrow \mathcal{A}_{\alpha\beta} = 1$ for $\alpha = \beta$
$\mathcal{A}_{\alpha\beta} = 0$ for $\alpha \neq \beta$

$\Leftrightarrow$ unitarity triangle(in complex plane)



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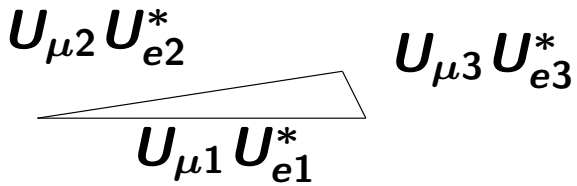

At $L = t \neq 0$, two of the vectors rotate in the complex plane, with frequencies $(m_j^2 - m_1^2)/2E$
oscillations $\leftrightarrow$ time-dependent non-unitarity
"drunken unitarity" $\Rightarrow$ intuition when can use 2-flavour approx

About two- flavour analyses : atm/LBL ν_μ disappearance

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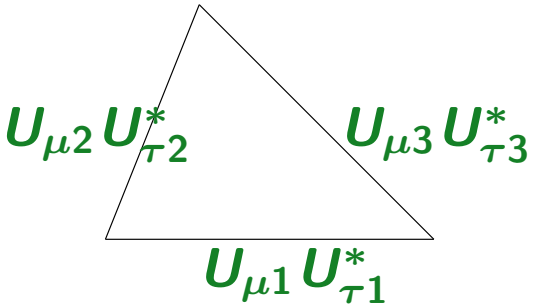

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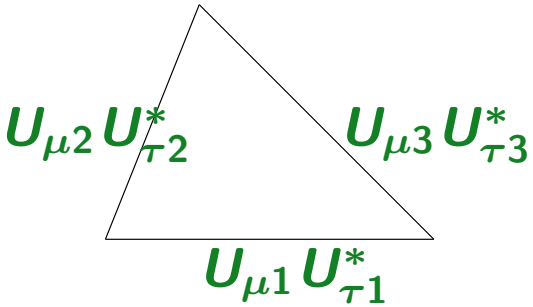


$\Rightarrow$ "Atmospheric" neutrinos, also LBL
(ν_μ disappearance via Δm^2_{31} oscillations) :

$$\mathcal{A}_{\mu\tau}(L) \simeq U_{\mu 1} U^*_{\tau 1} + U_{\mu 2} U^*_{\tau 2} + U_{\mu 3} U^*_{\tau 3} e^{-i(m_3^2 - m_1^2)L/(2E)}$$

$U_{\mu 3} U^*_{\tau 3}$ oscillates on timescale $t = L \sim (m_3^2 - m_1^2)/E$
$U_{\mu 2} U^*_{\tau 2} \sim$ stationary, measure θ_{23}

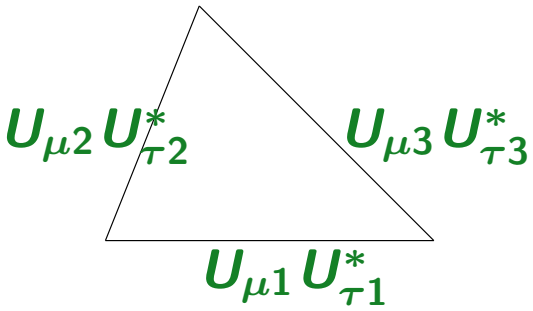
Three flavour probability required for CPV $\propto$ triangle area

$$\mathcal{P}_{\alpha\beta}(L) = \delta_{\alpha\beta} - 4\sum_{i<j} \mathrm{Re}\{U_{\alpha i}U^*_{\beta i}U^*_{\alpha j}U_{\beta j}\}\sin^2\frac{x_{ji}}{2}$$
$$+2\sum_{i<j} \mathrm{Im}\{U_{\alpha i}U^*_{\beta i}U^*_{\alpha j}U_{\beta j}\}\sin x_{ji}$$

Last term violates CP $\Leftrightarrow$ opposite sign for $\overline{\nu_\alpha} \to \overline{\nu_\beta}$.

(Also matter effect opposite sign for $\bar{\nu}$).

$\propto$ area of triangle $\propto \widetilde{J} = 8c_{13}^2 s_{13}c_{23}s_{23}c_{12}s_{12}$:



Suppose triangle base $\in \mathrm{Re} = U_{\mu 1}U^*_{\tau 1}$.
Then base*height $\propto \mathrm{Im}\{U_{\mu 1}U^*_{\tau 1}U^*_{\mu j}U_{\tau j}\}$
$\propto \widetilde{J}\sin\delta$

Leptogenesis

a class of recipes, that use (majorana) neutrino mass models to generate the matter excess

- what matter excess ?
- required ingredients ?
- a simple seesaw model
- how it works...

Preambule

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3. quantify as ($s_0 \simeq 7 n_{\gamma,0}$)

$$Y_B \equiv \left.\frac{n_B - n_{\bar{B}}}{s}\right|_0 = 3.86 \times 10^{-9} \Omega_B h^2 \simeq (8.53 \pm 0.11) \times 10^{-11}$$

PLANCK

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PLANCK

$\Rightarrow$ Question : where did that excess come from ?

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   X no ! After birth of U, there was "inflation"
   - (only theory explaining coherent temperature fluctuations in microwave background that arrive from causally disconnected regions today...)
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3. created/generated/cooked after inflation...

Three ingredients to prepare in the early U (old russian recipe)

Sakharov

1. B violation : if Universe starts in state of $n_B - n_{\bar{B}} = 0$, need $\not{B}$ to evolve to $n_B - n_{\bar{B}} \neq 0$

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   From end inflation $\rightarrow$ BBN, Universe is an expanding, cooling thermal bath, so non-equilibrium from :
   - slow interactions : $\tau_{int} \gg \tau_U$ = age of Universe ($\Gamma_{int} \ll H$)
   - phase transitions :

ingredient 1 : Does the SM conserve B ?

B, L are global symmetries of the SM Lagrangian (q, ℓ doublets, e, u, d singlets)

$$\mathcal{L}_{SM} \supset \overline{q} \not{D}\, q \ , \ \overline{\ell} \not{D}\, \ell \ \ , \ \ \overline{\ell} H e \ \ , \ \ \overline{q} \widetilde{H} u \ \ , \ \ \overline{q} H d$$

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But the SM *does not* conserve $B + L$...
In QFT, there is the axial anomaly...
...anomalously, the fermion current associated to a classical symmetry is not conserved.

see Polyakov,
"Gauge Fields + Strings,"
6.3=qualitative effects of instantons

ingredient 1 : the SM *does not* conserve $B + L$

$B + L$ is anomalous. Formally, for one generation(α colour) :

$$\sum_{\frac{SU(\mathbf{2})}{singlets}} \partial^\mu(\overline{\psi}\gamma_\mu\psi) + \partial^\mu(\overline{\ell}\gamma_\mu\ell) + \partial^\mu(\overline{q}^\alpha\gamma_\mu q_\alpha) \propto \frac{1}{64\pi^2} W^A_{\mu\nu}\widetilde{W}^{\mu\nu A}.$$

where integrating the RHS over space-time counts "winding number" of the SU(2) gauge field configuration.
$\Rightarrow$ Field configurations of non-zero winding number are sources of a doublet lepton and three (for colour) doublet quarks for each generation.

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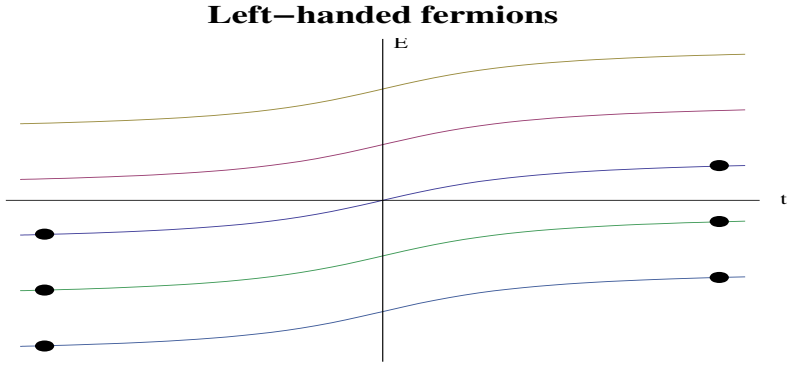

thanks to V Rubakov

SM B+L violation : rates

't Hooft
Kuzmin Rubakov+
Shaposhnikov

At $T = 0$ is tunneling process (from winding # to next, "instanton") : $\Gamma \propto e^{-8\pi/g^2}$

At $0 < T < m_W$, can climb over the barrier : $\Gamma_{\not{B+L}} \sim \begin{array}{ll} e^{-m_W/T} & T < m_W \\ \alpha^5 T & T > m_W \end{array}$

$$\Rightarrow \text{fast SM } \not{\mathrm{B+L}} \quad \text{at } T > m_W$$

$$\Gamma_{\not{\mathrm{B+L}}} > H \text{ for } m_W < T < 10^{12} \text{ GeV}$$

SM $\not{\mathrm{B+L}}$ called "sphalerons"
$\Rightarrow$ if produce a lepton asym, "sphalerons" partially transform to a baryon asym. ! !
$\star\star\star$ SM $\not{\mathrm{B+L}}$ is $\Delta B = \Delta L = 3$ $(= N_f)$. No proton decay ! $\star\star\star$

Summary of preliminaries : A Baryon excess today :

- Want to make a baryon excess $\equiv Y_B$ after inflation, that corresponds today to ~ 1 baryon per 10^{10} γs.
- Three required ingredients : $\not{B}$, $\not{CP}$, $\not{TE}$.

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One observation to fit, many new parameters...

$\Rightarrow$ *prefer BSM motivated by other data* $\Leftrightarrow m_\nu \Leftrightarrow$ *seesaw !* (uses non-pert. SM $\not{B+L}$)

The type I seesaw

Minkowski, Yanagida
Gell-Mann Ramond Slansky

- add 3 singlet N to the SM in charged lepton and N mass bases, at scale $> M_i$:

$$\mathcal{L} = \mathcal{L}_{SM} + \boldsymbol{\lambda}_{\alpha J} \overline{N}_J \ell_\alpha \cdot \phi - \tfrac{1}{2} \overline{N_J} M_J N_J^c$$

add 18 parameters :
M_1, M_2, M_3
18 - 3 (ℓ phases) in λ

M_I unknown ($\not{\propto} v = \langle \phi^0 \rangle$), and Majorana ($\not{L}$). $\not{CP}$ in $\boldsymbol{\lambda}_{\alpha J} \in \boldsymbol{C}$.

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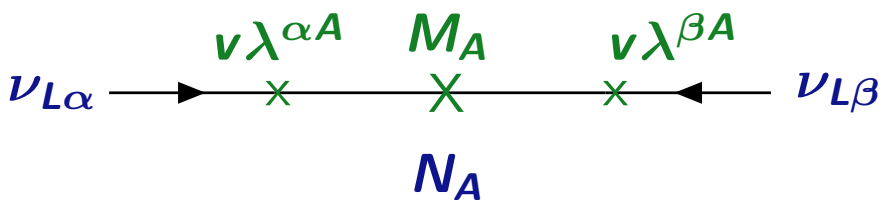
- at low scale, for $M \gg m_D = \lambda v$, light ν mass matrix



9 parameters :
m_1, m_2, m_3
6 in U_{MNS}

$$[m_\nu] = \boldsymbol{\lambda} M^{-1} \boldsymbol{\lambda}^T v^2$$

for $\lambda \sim h_t$, $M \sim 10^{15}$ GeV
$\lambda \sim 10^{-7}$, $M \sim 10$ GeV

$$\sim .05 \text{ eV}$$

"natural" $m_\nu \ll m_f$: $m_\nu \propto \lambda^2$, and $M > v$ allowed.

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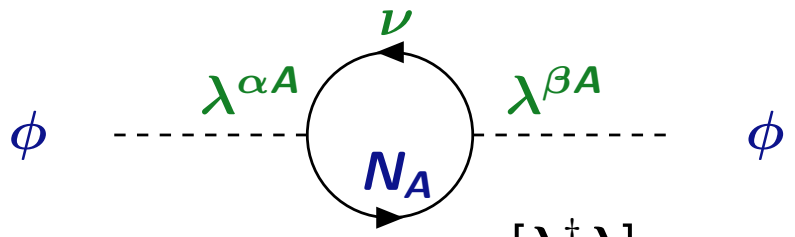
- at low scale, Higgs mass contribution



$$\delta m_\phi^2 \simeq -\sum_I \frac{[\lambda^\dagger \lambda]_{II}}{8\pi^2} M_I^2 \sim \frac{m_\nu M_I^3}{8\pi^2 v^4} v^2$$

for $M \gtrsim 10^7$ GeV $\quad > \quad v^2$ tuning problem

(? adding particles to cancel 1 loop...but higher loop ? Need symmetry to cancel ≥ 2 loop ?)
$\Rightarrow$ do seesaw with $M_I \lesssim 10^8$ GeV ?
(NB, in this talk, ϕ = Higgs, H = Hubble)

Leptogenesis in the type 1 seesaw : usually a Fairy Tale

Fukugita Yanagida
Buchmuller et al
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The adventure begins after inflationary expansion of the Universe :

1 Assuming its hot enough, a population of Ns appear—they like the heat.

2 As the temperature drops below M, the N population decays away.

3 In the $\not{CP}$,$\not{L}$ interactions of the N, an asym. in SM leptons is created.

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...

If this asymmetry can escape the big bad wolf of thermal equilibrium...

Leptogenesis in the type 1 seesaw : usually a Fairy Tale

Fukugita Yanagida
Buchmuller et al
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Once upon a time, a Universe was born.
At the christening of the Universe,the fairies give the Standard Model and the Seesaw (heavy sterile N_j with $\not{L}$ masses and $\not{CP}$ interactions) to the Universe.
The adventure begins after inflationary expansion of the Universe :

1 Assuming its hot enough, a population of Ns appear—they like the heat.

2 As the temperature drops below M, the N population decays away.

3 In the $\not{CP}$,$\not{L}$ interactions of the N, an asym. in SM leptons is created.

4 If this asymmetry can escape the big bad wolf of thermal equilibrium...

5 the lepton asym gets partially reprocessed to a baryon asym by non-perturbative $B + L$ -violating SM processes ("sphalerons")

And the Universe lived happily ever after, containing many photons. And for every 10^{10} photons, there were 6 extra baryons (wrt anti-baryons).

Estimate something : $\not{T}\not{E}$ + dynamics

Suppose $M_1 \ll M_{2,3}$, $T_{reheat} > M_1 \sim 10^9$GeV

Recipe : calculate suppression factor for each Sakharov condition, multiply together to get Y_B :

$$\frac{n_B - n_{\bar{B}}}{s} \sim \frac{1}{3g_*}\epsilon_{L,CP}\eta_{TE} \sim 10^{-3}\epsilon\eta \qquad (\text{want } 10^{-10})$$

$s \sim g_* n_\gamma$, $\epsilon =$ lepton asym in decay, $\eta \sim \not{T}\not{E}$ process

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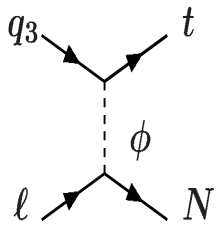

1 produce a population of N_1s, via *e.g.* $(q\ell_\alpha \to N t_R)$

Get thermal density $n_N \simeq n_\gamma$ if $M_1 \lesssim T$, and $\tau_{prod} < \tau_U$:

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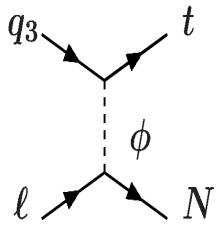

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Suppose satisfied...

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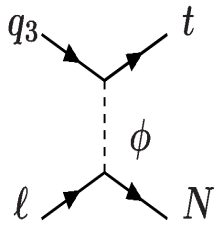

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$$\Gamma_{ID}(\phi\ell \to N) \simeq \Gamma_{decay}\, e^{-M_1/T} = \frac{[\lambda\lambda^\dagger]_{11} M_1}{8\pi} e^{-M_1/T} < \frac{10\,T^2}{m_{pl}}$$

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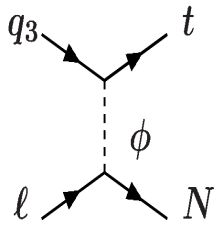

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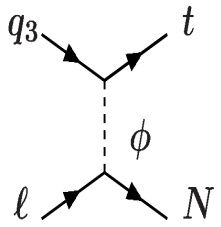

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so (1/3 is from SM $\not{B}+\not{L}$, $s \sim g_* n_\gamma$, ϵ_α is lepton asym in decay)

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Estimate ϵ, the CP and L asymmetry in decays

Recall (in **S**-matrix) $CP : \langle \phi \ell | \boldsymbol{S} | N \rangle \to \langle \overline{\phi \ell} | \boldsymbol{S} | \overline{N} \rangle = \langle \overline{\phi \ell} | \boldsymbol{S} | N \rangle$, ($\overline{\eta}$ =anti-η)

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finite temp :Beneke etal 10

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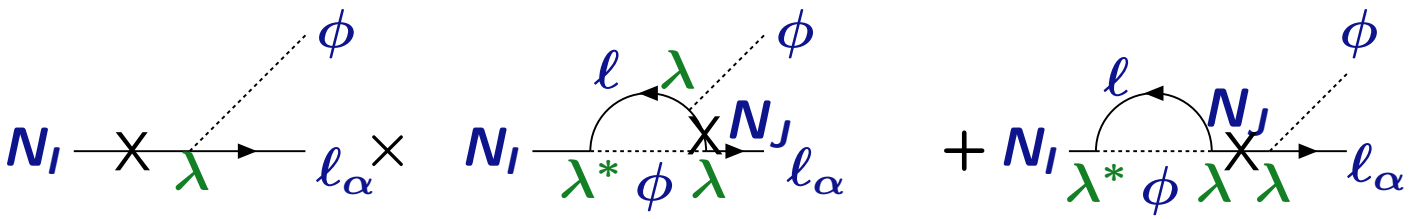

Just try to calculate ϵ_1 ?

- no asym at tree
- asym at tree $\times$ loop, *if* $\not{CP}$ from complex cpling *and* on-shell particles in the loop (divergences cancel in diff, need Im part of Feynman param integrtn)

$\not{C}\not{P}$, complex couplings, loops unitarity and all that...(estimate ϵ, no loop caln)

Kolb+Wolfram, NPB '80, Appendix

1 the S-matrix $\boldsymbol{S} \equiv \mathbf{1} + i\,\boldsymbol{T}$ is CPT invariant

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2 We are interested in a $\not{C}\not{P}$ asymmetry :

$$\epsilon \propto \int d\Pi \Big(|\langle \phi\ell | \boldsymbol{T} | N \rangle|^2 - |\langle \overline{\phi\ell} | \boldsymbol{T} | N \rangle|^2 \Big)$$

so (this formula exact, if I kept 2s and sums ; $\int d\Pi =$ phase space)

$$\epsilon \propto \int d\Pi \, \boldsymbol{Im} \Big\{ \langle \phi\ell | \boldsymbol{T}^\dagger | N \rangle \langle N | \boldsymbol{T}\boldsymbol{T}^\dagger | \phi\ell \rangle \Big\}$$

$\Rightarrow$ need complex cplings, and on-shell particles in a loop

Estimating ϵ for hierarchical N_I

Consider simple case : $M_1 \ll M_{2,3}$. Suppose lepton asym generated in $\not{CP}$, $\not{L}$ decays of N_1 :

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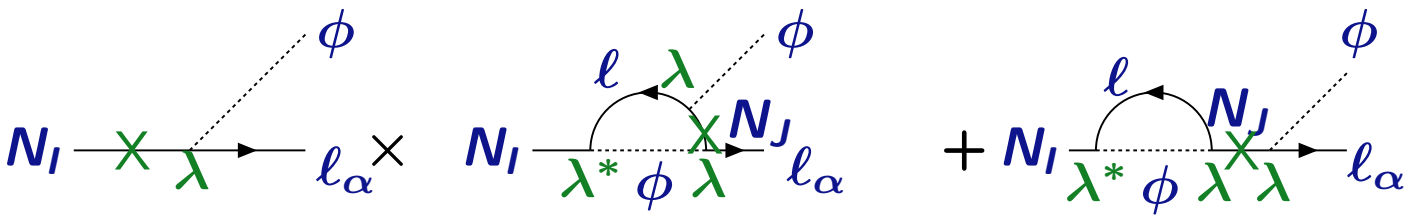
(NB, no intermediate N_1 because cplg combo real)



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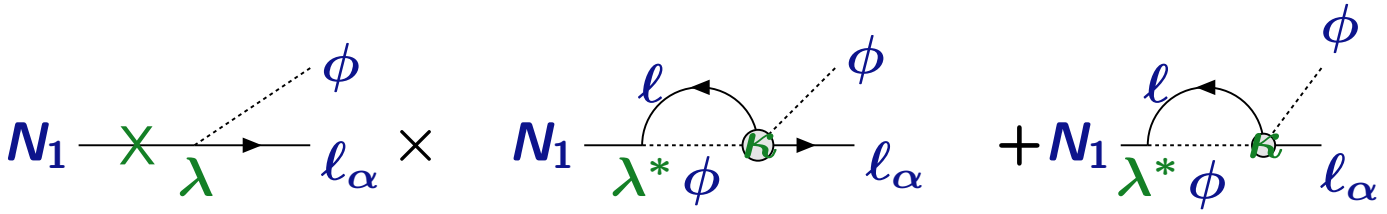

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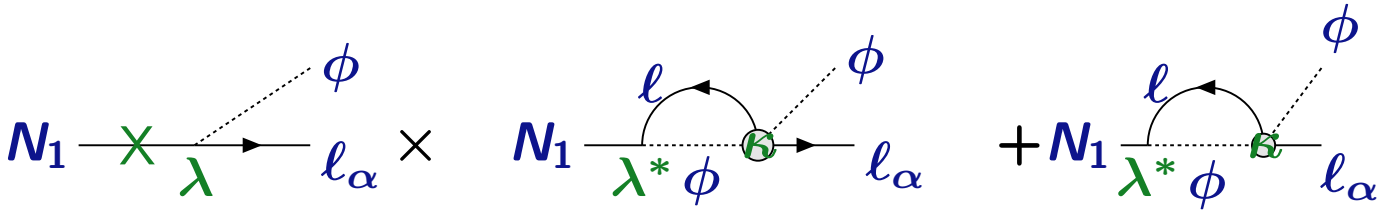

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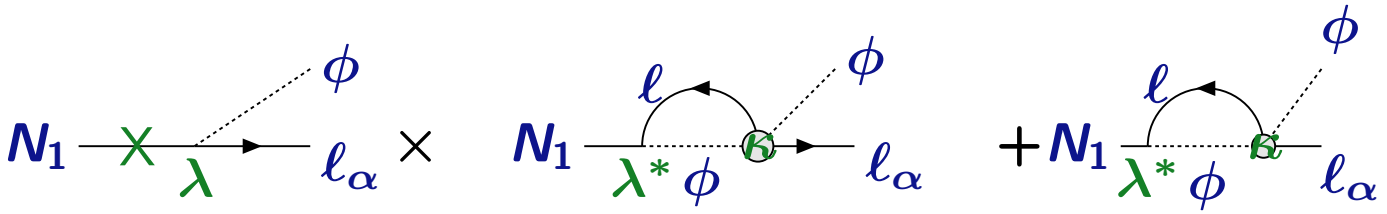

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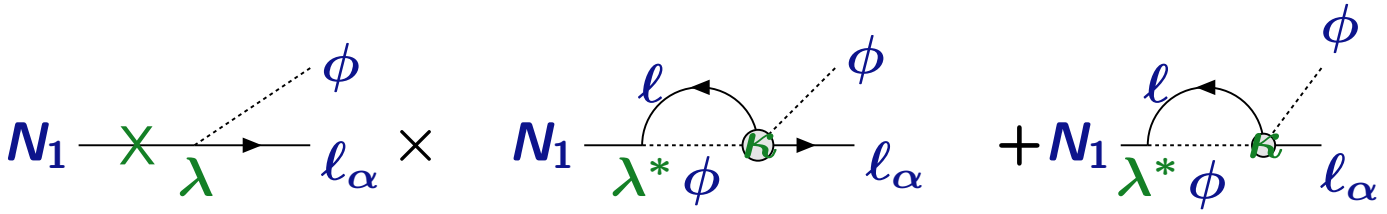

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$$\epsilon_1 \sim M\frac{\boldsymbol{Im}\{\lambda\lambda\kappa^*\}}{8\pi|\lambda|^2} < \frac{3}{8\pi}\frac{m_\nu^{max} M_1}{v^2} \sim 10^{-6}\ \frac{M_1}{10^9\text{GeV}} \gtrsim 10^{-6}$$

so for $M_1 \ll M_{2,3}$, need $M_1 \gtrsim 10^9$ GeV to obtain sufficient ϵ

Maybe want $M_K < 10^9$ GeV ? Leptogenesis with lighter N_I...

1. $M_I \sim M_J \Leftrightarrow$ resonantly enhance ϵ ... up to $\epsilon \lesssim 1$.
2. at lower T, age of Universe is longer, takes more care to get out-of-equilibrium...
3. need to generate L asym before Electroweak PT (to profit from sphalerons)...

$\Rightarrow$ leptogenesis via N_I decay/scattering works for degen N_I down to $M_I \sim$ TeV

For even lighter M_I, can make asym by coherent oscillations and scatterings of N_I...

νMSM : type 1 seesaw below 100 GeV gives BAU and DM

Asaka + Shaposhnikov
...
thesis Canetti

ingredients : SM +

$N_{2,3}$: 100 MeV $\lesssim M_{2,3} \lesssim$ 10 GeV, $\Delta M \lesssim \begin{cases} 10^{-6}\ \mathrm{eV} & Y_B, \Omega_{DM} \\ \mathrm{keV} & Y_B, NOT\ \Omega_{DM} \end{cases}$

Yukawas $\ni$ give 2 light SM neutrinos via seesaw

N_1 : $M_1 \sim$ keV. WDM candidate.

feebly coupled (negligeable contribution $m_{\nu,SM}$)

scenario :

Population of $N_{2,3}$ produced via Yukawas before EPT

Produce $\Delta L \to Y_B$, before EPT, via oscillations of $N_{2,3}$ coherent with Yukawa scattering to ν_{SM}

Produce $\Delta L \gtrsim 10^{-5}$ via osc. and decay of $N_{2,3}$ after EPT

Can produce sufficient distribution of N_1 via osc.

tests :

$N_{2,3}$: beam dump, SHIP

N_1 as DM : X-rays from DM decay, WDM bounds (depend on momentum distribution)

How does asym generation work ? (very simplified !)

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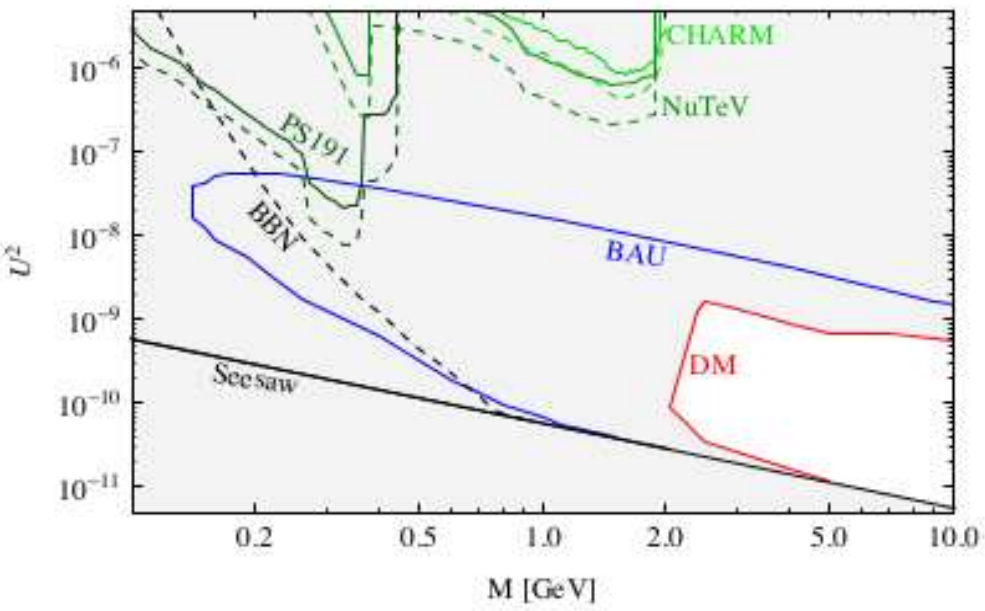
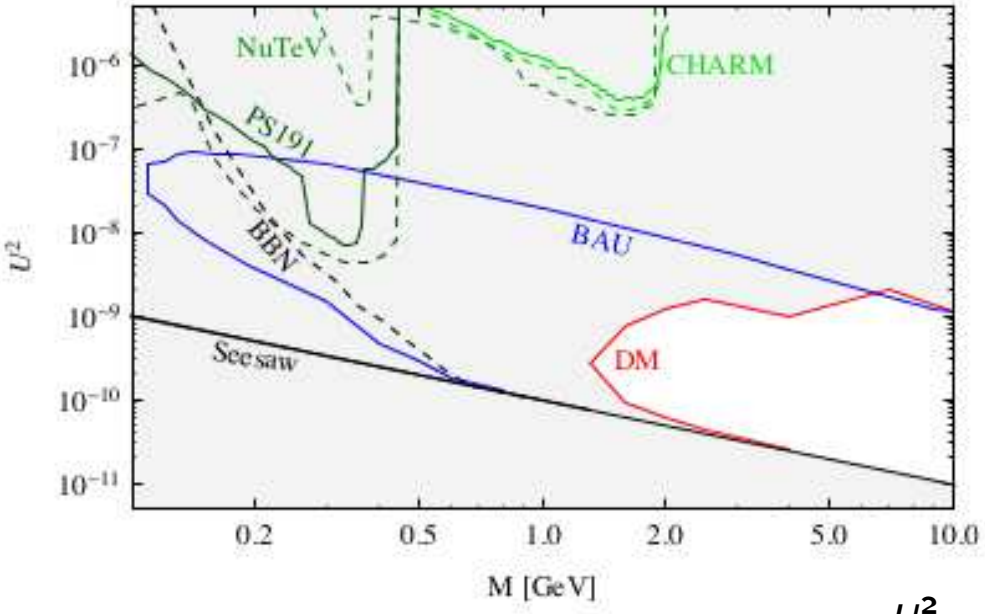
at $\tau_U \sim \tau_{osc}$, 1,2,3 are *coherent*, so CPV from λ-ΔM^2-λ gives flavour asyms in $\nu_{L\alpha}$ (to small)
lepton number in $\ell_L + N_R$ is conserved (actually, $L_{SM}+$ helicity of N_I)
from $\tau_{osc} \to \tau_{EWPT}$, asyms in $\nu_{L\alpha}$ seed asyms in $N \longrightarrow$ asyms in $\nu_{L\alpha}$ (enough asym)
...works also in detailed calculations with all available technology...
(eg also include lepton number violating interactions)

Teresi Hambye
Eijima + Shaposhnikov
Ghiglieri+ Laine





$$U^2 = \mathrm{Tr}[\lambda M^{-2} \lambda^\dagger]$$

arXiv :1208.4607

Summary

Leptogenesis is a class of recipes, that use (majorana) neutrino mass models to generate the matter excess. The model generates a lepton asymmetry (before the Electroweak Phase Transition), and the non-perturbative SM B+L violn reprocesses it to a baryon excess.

⋆ efficient, to use the BSM for m_ν to generate the Baryon Asym.

⋆ using SM B+L violn ($\Delta B = \Delta L = 3$) avoids proton lifetime bound

⋆ *it works* ...rather well, for a wide range of parameters

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- suppose that all parameters in $\mathcal{L}$ that can be complex (U and $m_{\nu i}$), are complex
- 3 angles and 6 phases in generic unitary matrix U (18 real parameters in arbitrary 3×3 complex matrix. Unitarity $UU^\dagger = 1$ reduces this to 9.)

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- now check if can make the masses real : if dirac masses, absorb phase of mass with ν_{Rl}. If ν_{L3} has Majorana mass, between self and anti-self, choose absolute phase of ν_{L3} to make the mass real. Now all LH fermion phases are fixed, and cannot remove phases from $m_{\nu 1}, m_{\nu 2}$.

$\Rightarrow$ extra CPV in processes where Majorana mass appears linearly (not as mm^*, not in kinematics = not in oscillations)