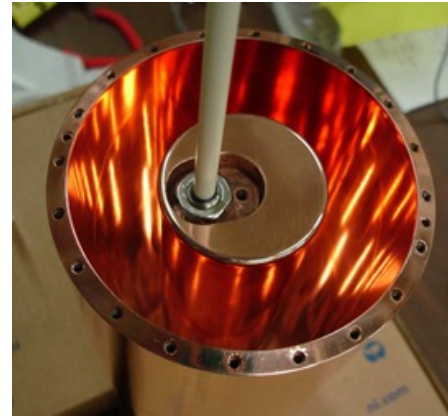
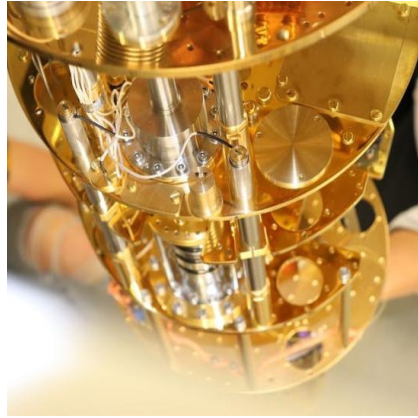
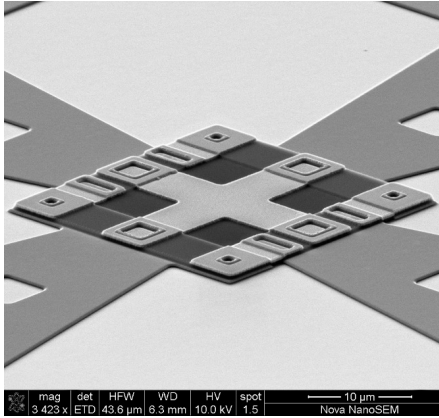


Quantum information for high-energy and nuclear particle physics



Konrad W. Lehnert
SLAC Summer institute 2026
Palo Alto, California

HAYSTAC 
The Haloscope At Yale Sensitive To Axion CDM



What can Quantum info do for high-energy and nuclear particle physics?

many things, but I will discuss the example I know best

quantum enhanced sensing of classical fields

hypothetical ultralight dark matter, especially the QCD axion (this lecture)

gravitational wave detection

Summary

quantum enhanced sensing: engineering design choice, not magic

reduces time or money needed to detect a signal

primary benefit is an increase in sensor bandwidth

useful if easier to lower noise than to increase signal

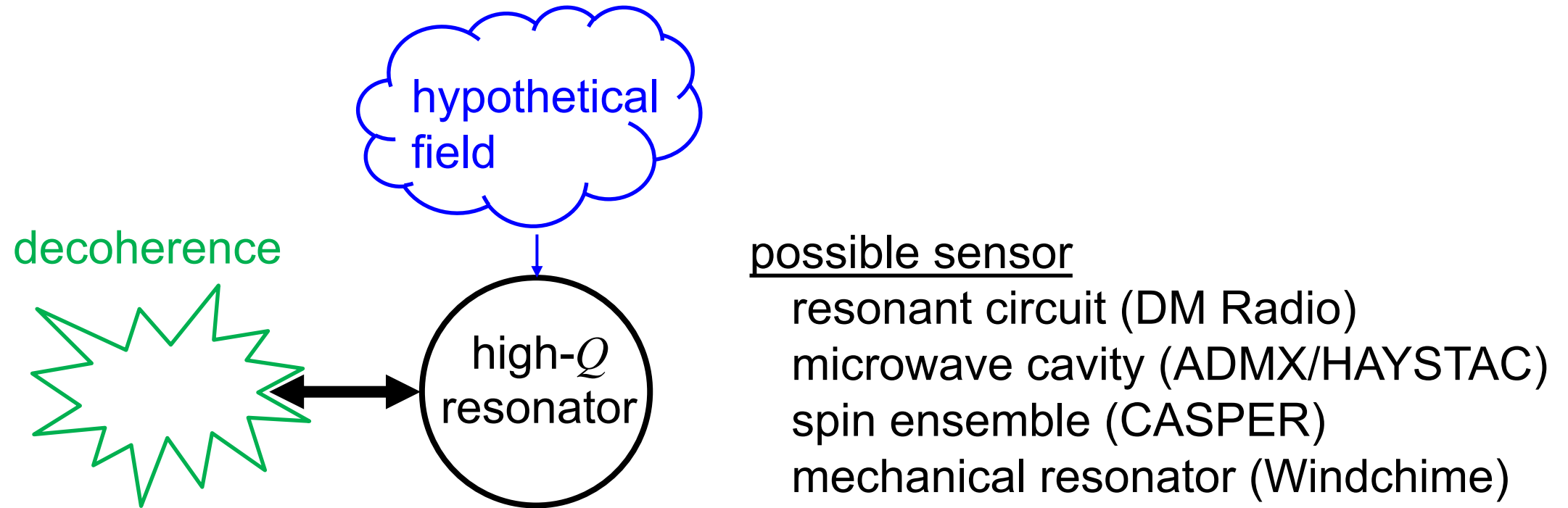
<https://doi.org/10.48550/arXiv.2110.04912>

theory of quantum squeezing to enhance classical field sensing

squeezing deployed in a search for axionic dark matter

strategies for more quantum enhancement

Classical fields: large amplitude but weak coupling to a sensor



distinguish evolution under

null hypothesis

$$\hat{H}_r = \frac{\hbar\omega_r}{2}(\hat{Q}^2 + \hat{P}^2)$$

field hypothesis

$$\hat{H}_r = \frac{\hbar\omega_r}{2}(\hat{Q}^2 + \hat{P}^2) + F(t)\hat{Q}$$

If signal is an oscillatory “force” of unknown frequency

$$F(t) = \alpha \cos(\omega_a t + \phi)$$

$$\omega_a = m_a c^2 / \hbar$$

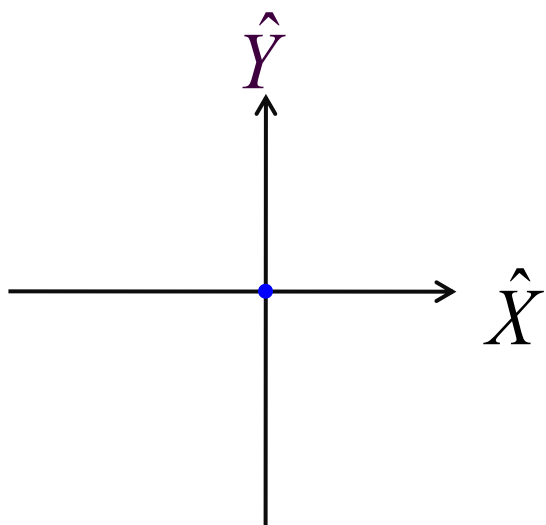
$$\hat{X} = \hat{Q} e^{-i\omega_r t} \quad \hat{Y} = \hat{P} e^{-i\omega_r t}$$

quadrature variables

$$\Delta_{ar} = \omega_a - \omega_r$$

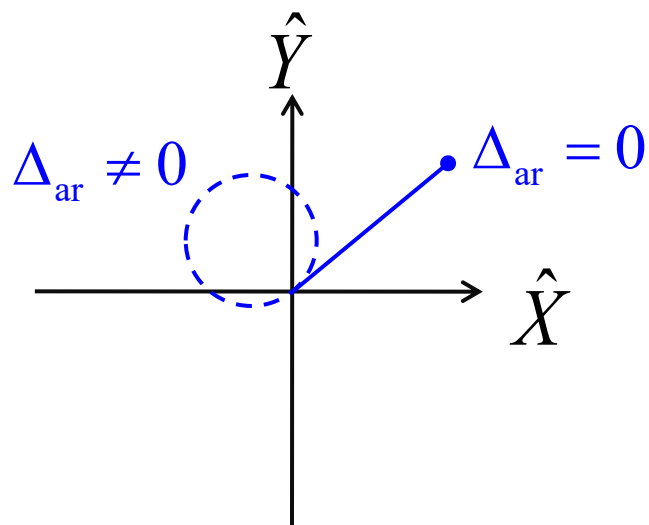
null hypothesis

$$\tilde{H}_r = 0$$



dark matter hypothesis

$$\tilde{H}_r \approx F_Y \sin(\Delta_{ar} t) \hat{X} + F_X \cos(\Delta_{ar} t) \hat{Y}$$



Quantum noise pollutes inference of classical force

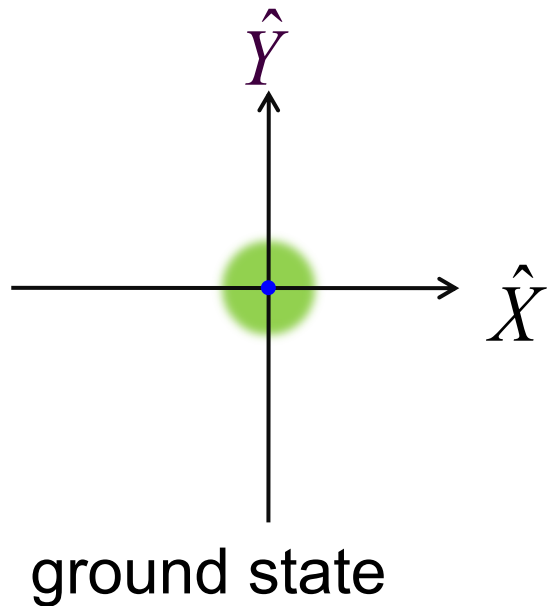
$$[\hat{X}, \hat{Y}] = i$$

coherent state limit (CSL) also “SQL”

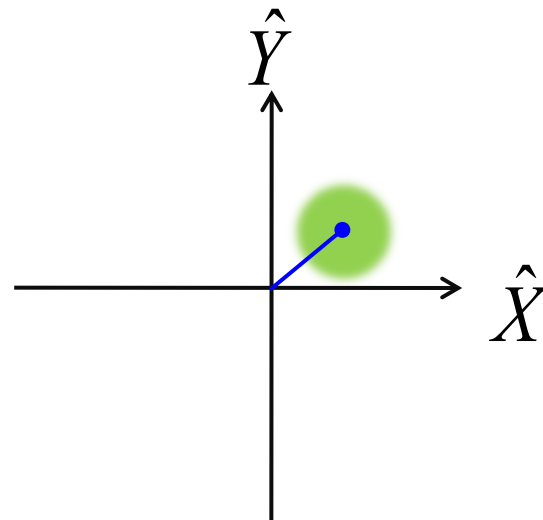
$$\delta\hat{X}\delta\hat{Y} \geq \frac{1}{2}$$

prepare in ground state, measure X or Y

null hypothesis



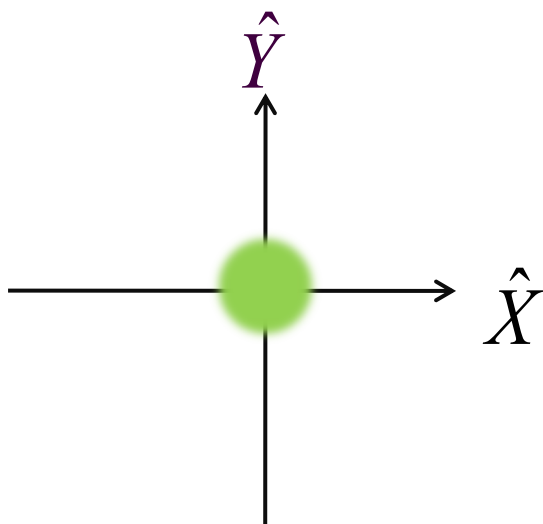
field hypothesis



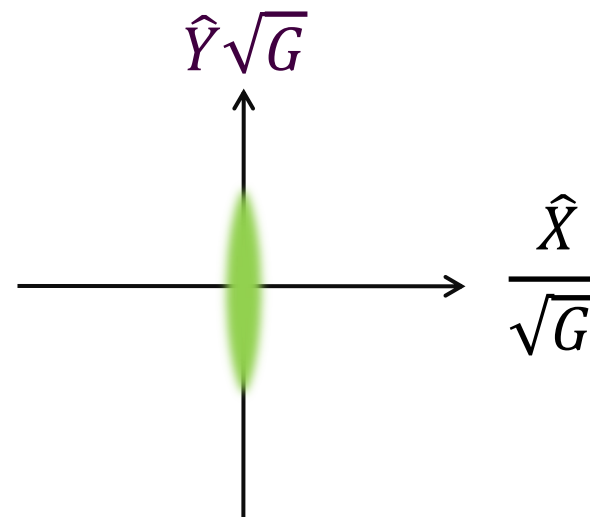
displaced ground state

Squeezed states approximate quadrature eigenstates

$$[\hat{X}, \hat{Y}] = i$$



$$[\hat{X}/\sqrt{G}, \hat{Y}\sqrt{G}] = i$$



phase space volume conserved
 commutator preserved
 no added noise

Squeezing and noiseless measurement circumvent quantum limit⁹

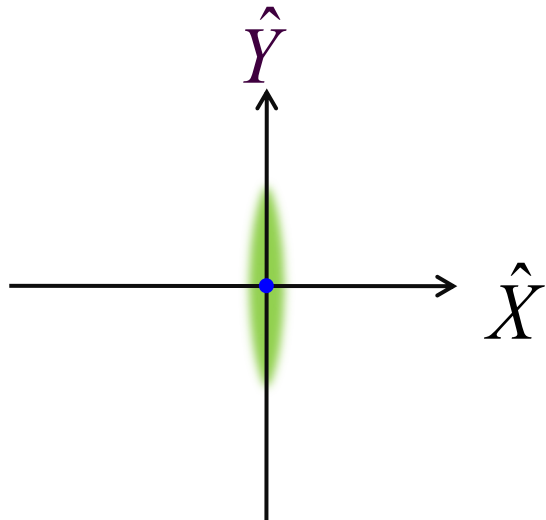
$$[\hat{X}, \hat{Y}] = i$$

$$\delta\hat{X}\delta\hat{Y} \geq \frac{1}{2}$$

‘beat’ the CSL:

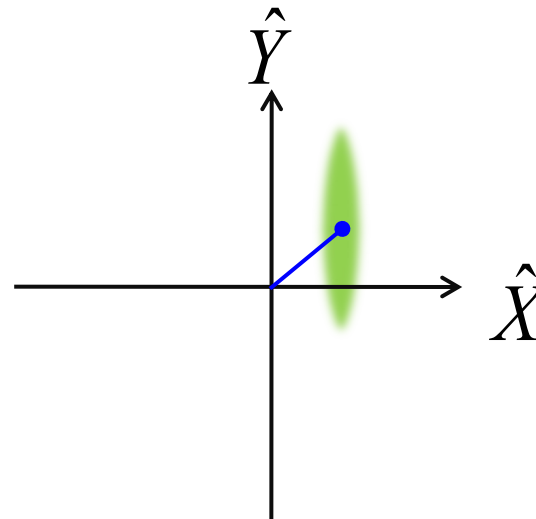
prepare in X squeezed state, measure X noiselessly

null hypothesis



squeezed state

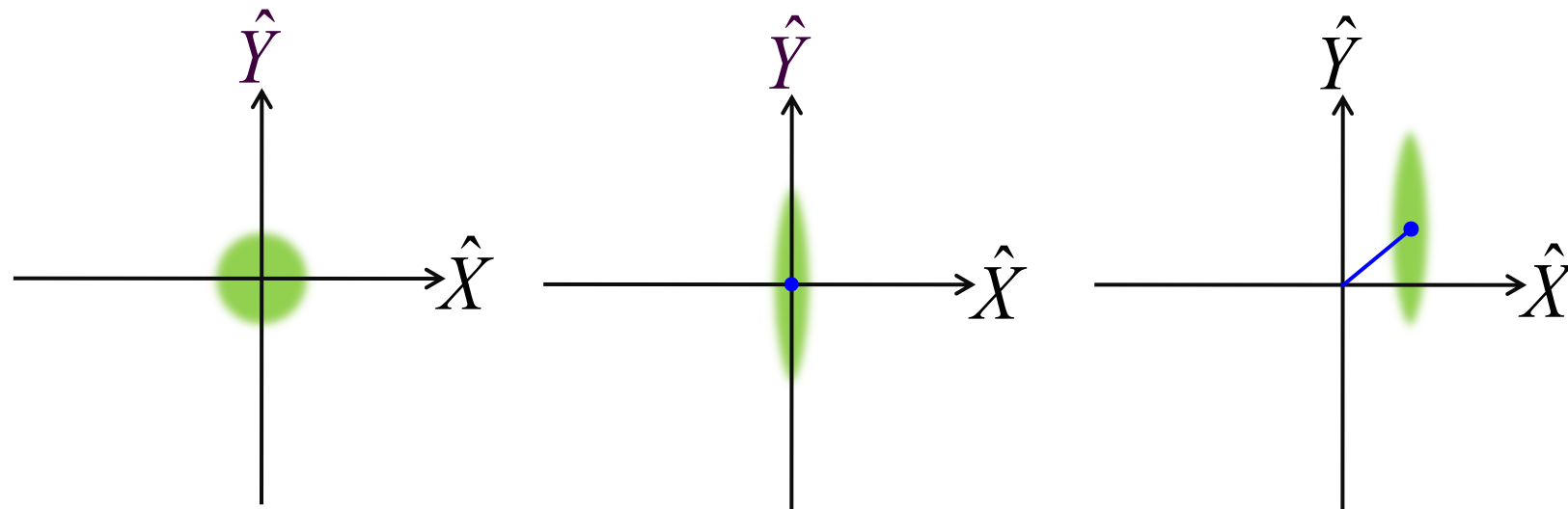
field hypothesis



displaced squeezed state

Quantum state preparation and measurement access quantum metrology

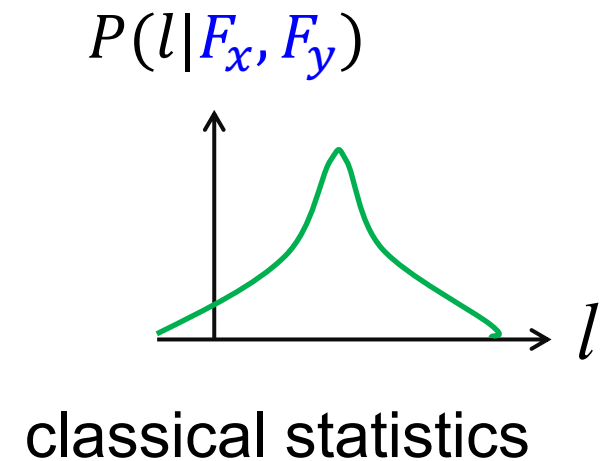
$|\psi_0\rangle$ prepare $|\psi_{\text{in}}\rangle$ evolve $|\psi_{\text{out}}(F_x, F_y)\rangle$ measure $P_l = \langle \psi_{\text{out}} | \mathbf{M}_l | \psi_{\text{out}} \rangle$



optimize estimation of parameters over:

initial state preparation $|\psi_{\text{in}}\rangle$

measured quantity $\mathbf{M}_l$



Frequently asked questions

Does the quantum advantage disappear when considering decoherence?

Do you need to know the phase of the signal to benefit from squeezing?

Can you measure both quadratures of the *signal* better than the CSL?

Impact of loss and decoherence on squeezing and signal

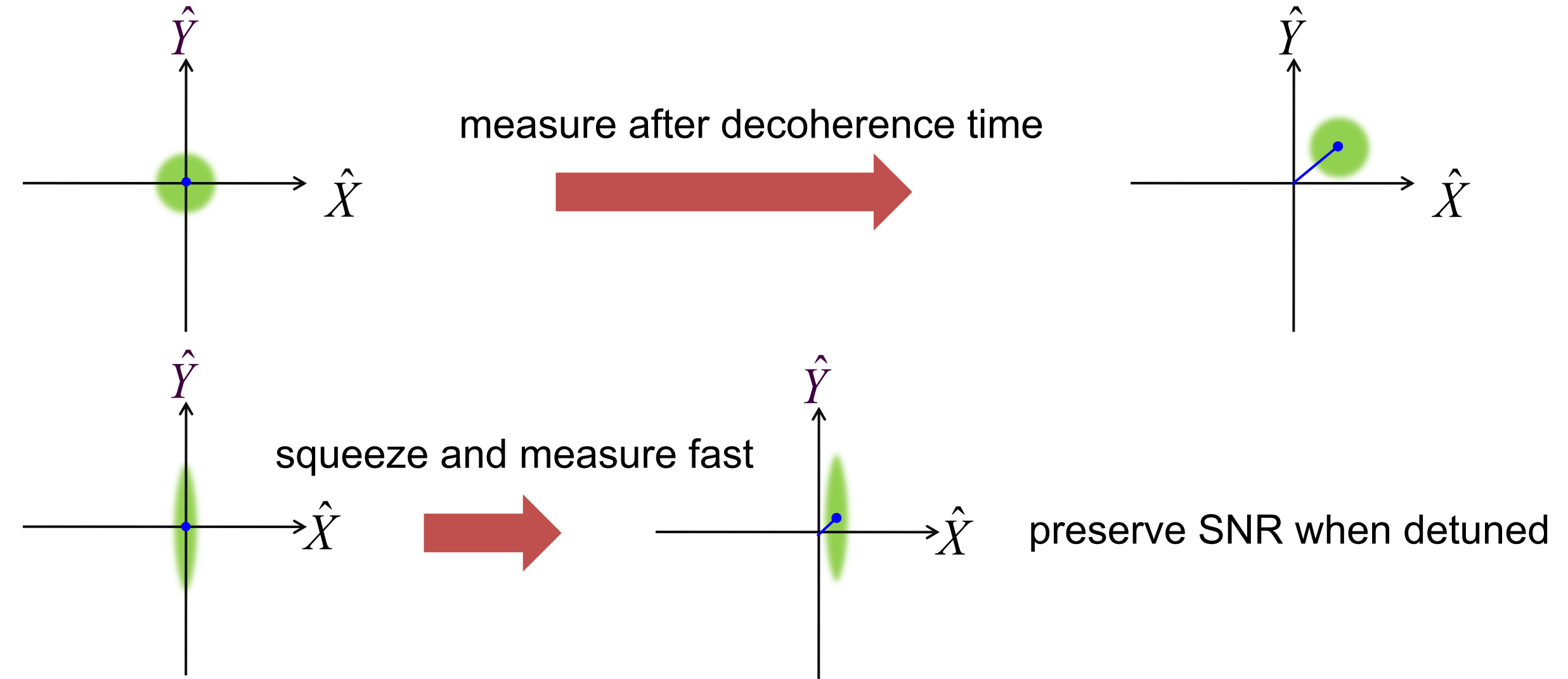


in a characteristic decoherence time

squeezing is lost

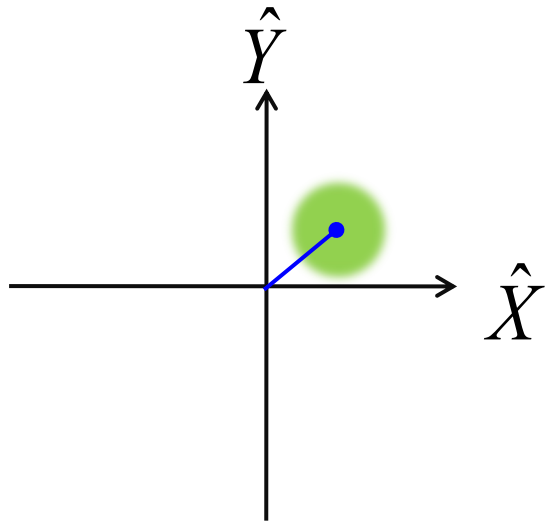
displacement reaches steady-state value

Squeezing improves sensor bandwidth



Measuring both quadratures doubles the signal and noise power

Wigner function

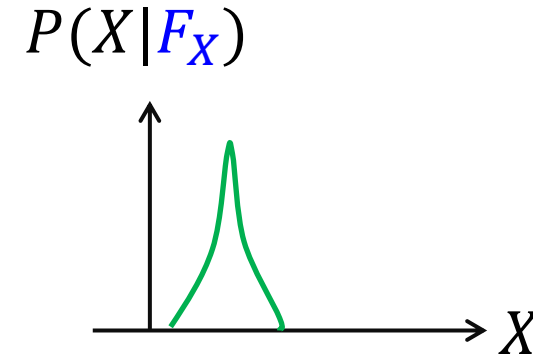


measure X only

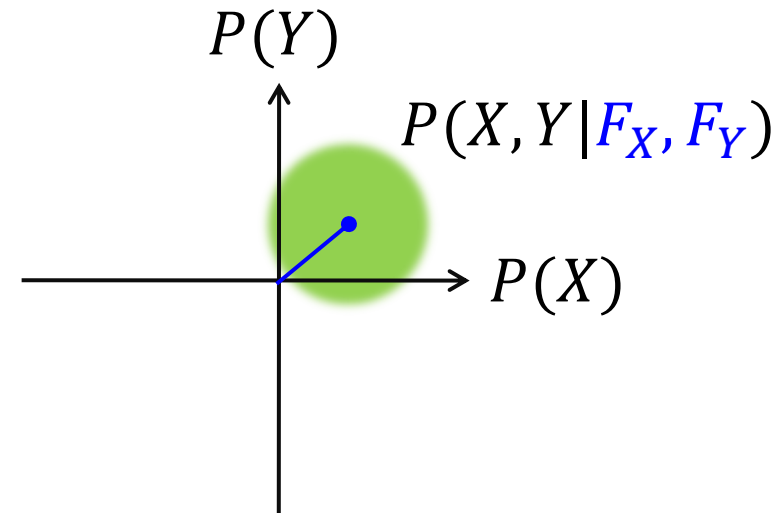
$$[\hat{X}, \hat{Y}] = i$$

measure X and Y

marginal of Wigner function

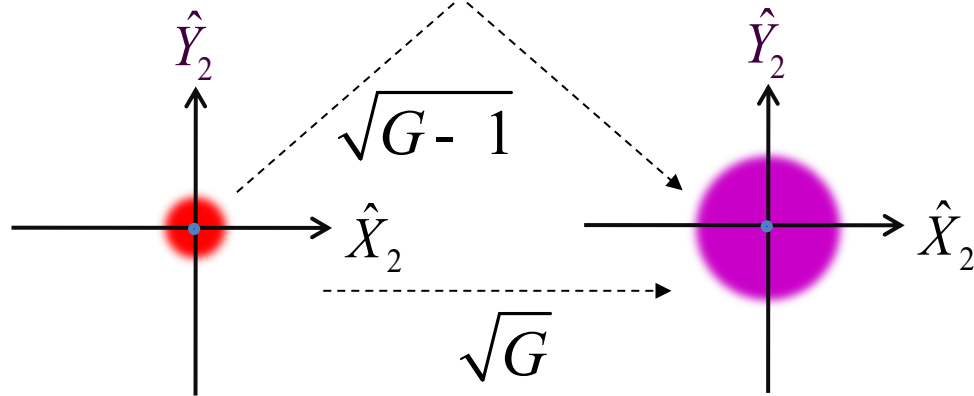
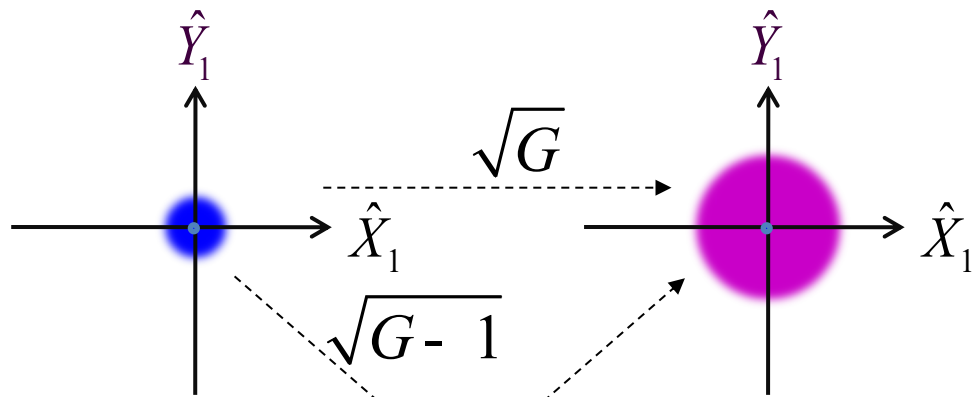


Huisimi – Q function



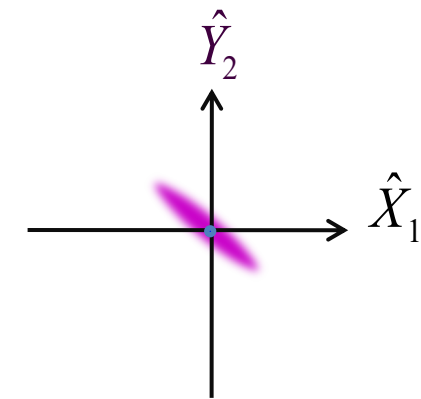
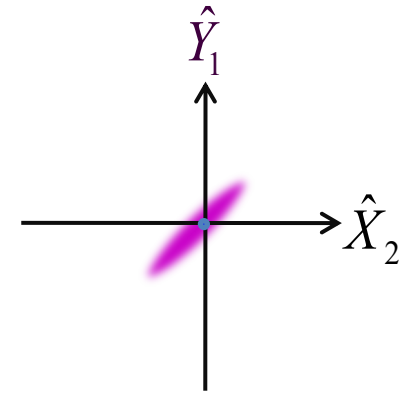
Two-mode squeezing operation is unitary

resonator 1



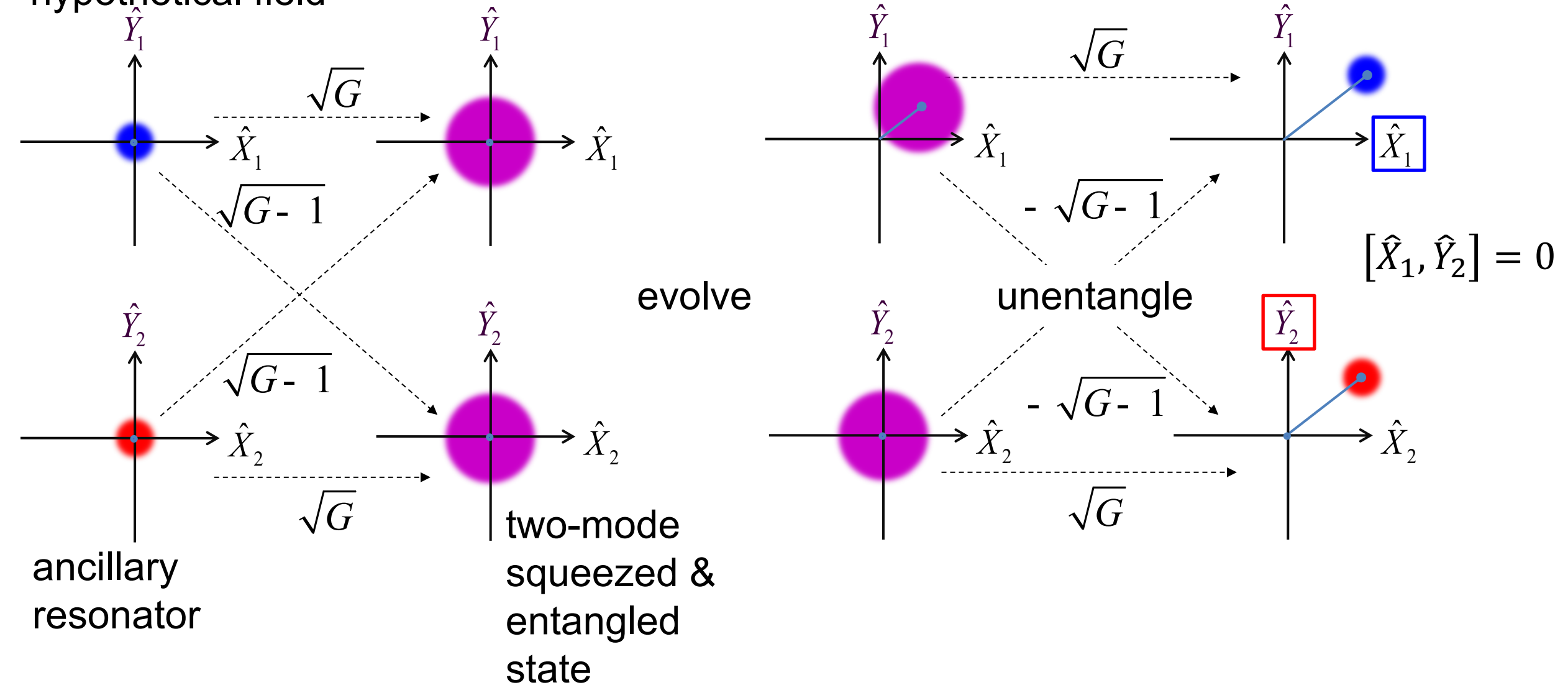
resonator 2

correlations reveal entanglement



Quantum enhanced measurement of both quadratures

resonator coupled to
hypothetical field



Squeezing in an axion dark matter search

Ultralight dark matter must be bosonic

dark matter (Λ CDM)

“cold:” gravitationally bound to us

mean density: $\sim 0.4 \text{ GeV/cm}^3$

weakly interacting

implications for particles with rest mass $m_a < 1 \text{ eV}$

quantum degenerate Bose gas

more “field-like” than “particle-like”

persistent, large amplitude, weakly coupled field



Hypothetical QCD axion: a light particle that is cold and dense enough to contribute to dark matter

mechanism to resolve strong-CP problem (Peccei and Quinn)

associated particle (axion) is dark matter candidate

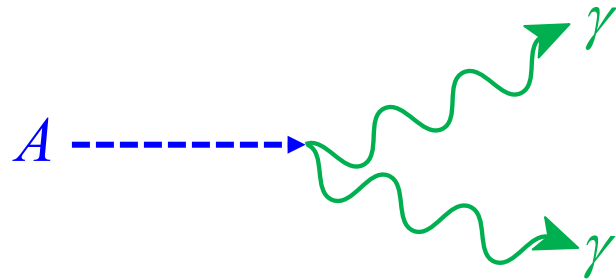
mass range $2 \mu\text{eV} < m_a c^2 < 2000 \mu\text{eV}$

as a frequency $500 \text{ MHz}^* < m_a c^2 / h < 500 \text{ GHz}$

*post-inflation scenario

Axion field couples (weakly) to electromagnetism

modified QCD Lagrangian $\Rightarrow g_{A\gamma\gamma} A (\vec{E} \cdot \vec{B})$

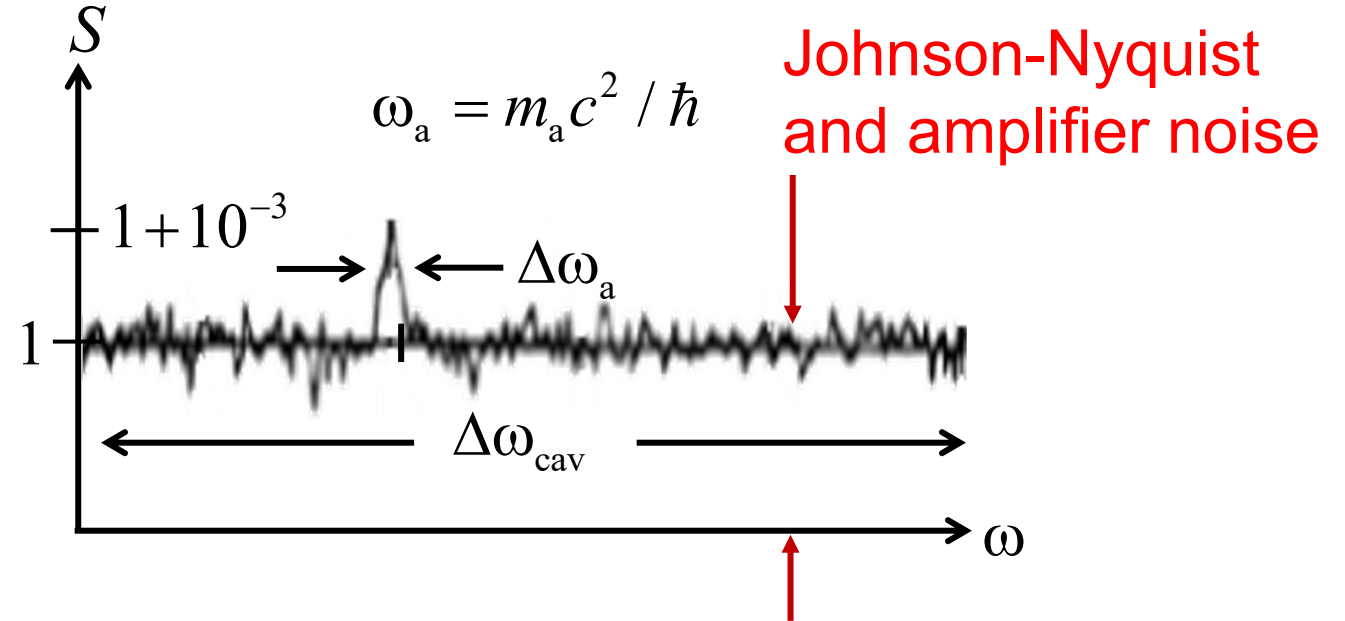
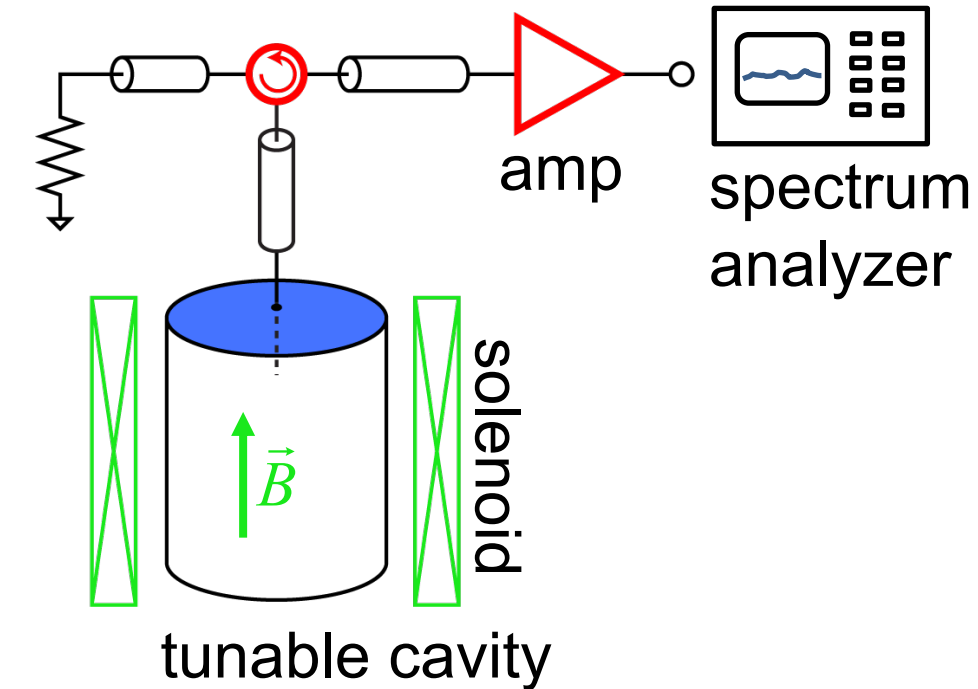


linearize coupling around static $\vec{B}$ -field



dark matter axions create microwave photons

Scan narrowband cavity to search for resonant axion to photon conversion: haloscope (Sikivie 1983)



axion field more coherent than cavity

tune $\rightarrow$ wait and integrate $\rightarrow$ tune

resolve variance with 10^{-3} precision
 $\Rightarrow 10^6$ realizations of random process

$$\frac{\omega_a}{\Delta \omega_a} \approx 10^6 \quad \frac{\omega_{\text{cav}}}{\Delta \omega_{\text{cav}}} \approx 10^4$$

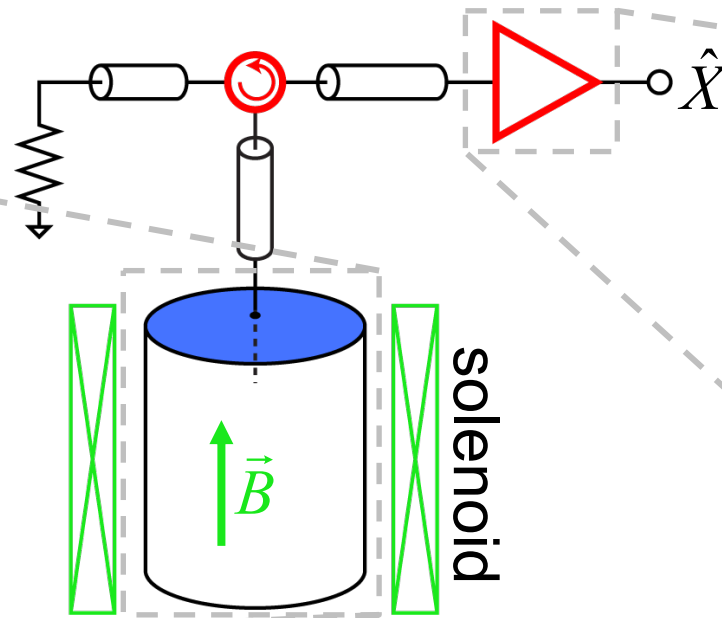
Cool cavity and measure with noiseless amplifier to reach CSL



1 L volume

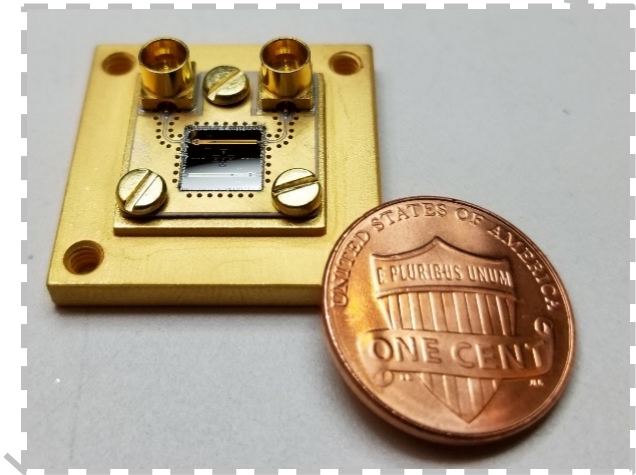
$$Q = 10^4$$

$$\omega_{\text{cav}} \sim 2\pi \times 5 \text{ GHz}$$



tunable cavity

$$T \ll \frac{\hbar \omega_{\text{cav}}}{k_B}$$

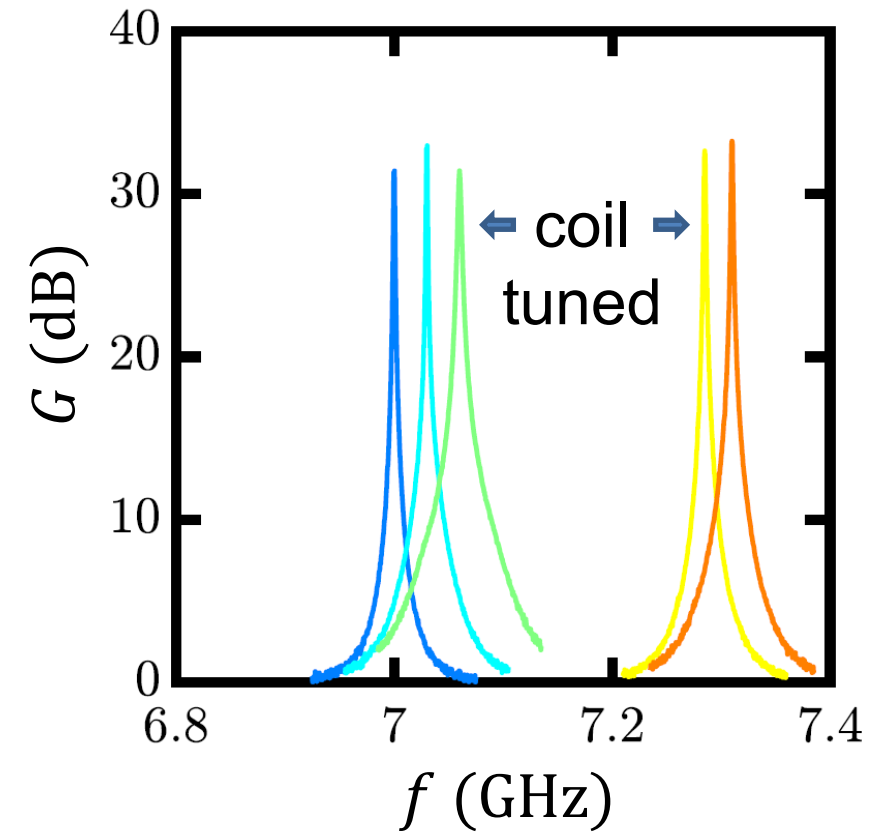
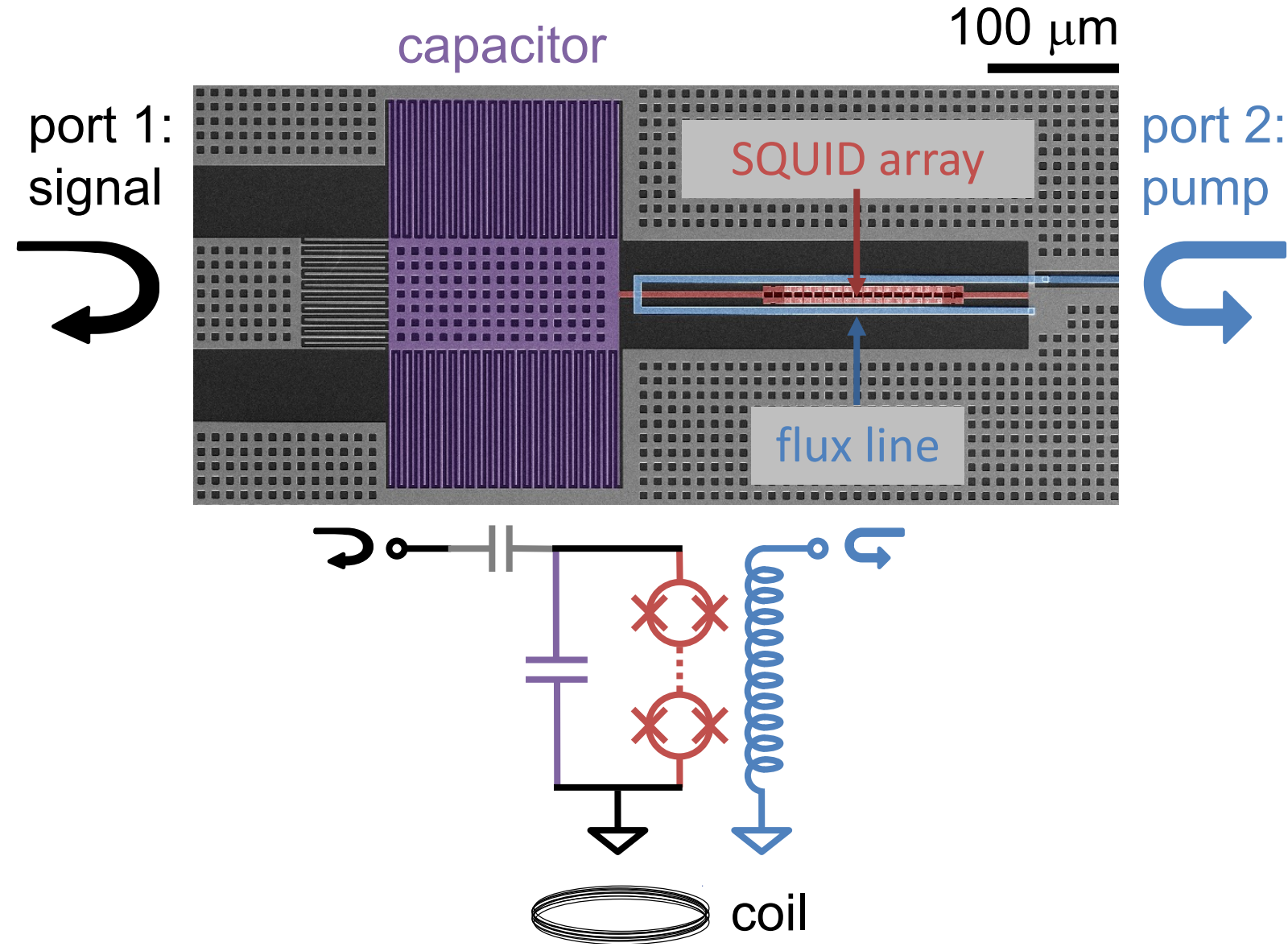


Josephson parametric
amplifier (JPA)

measure $\hat{X}$ noiselessly

haloscope near the CSL (HAYSTAC 2017)

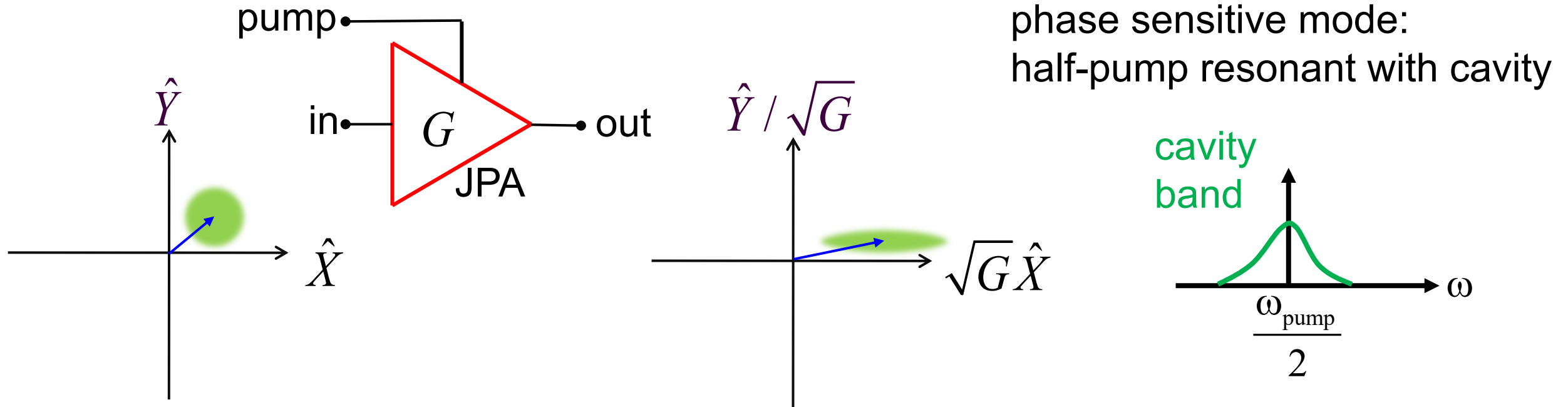
Low noise amplification with Josephson parametric amplifiers



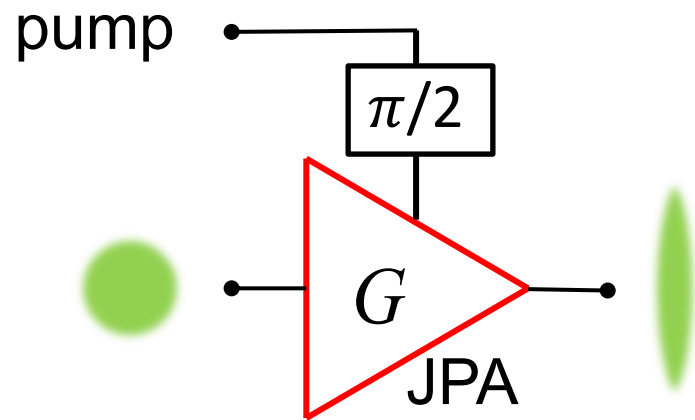
tunable over 1.5 GHz
gain > 30 dB

Phase sensitive amplifier measures one quadrature noiselessly

24



JPA noiselessly transforms ground state into squeezed state



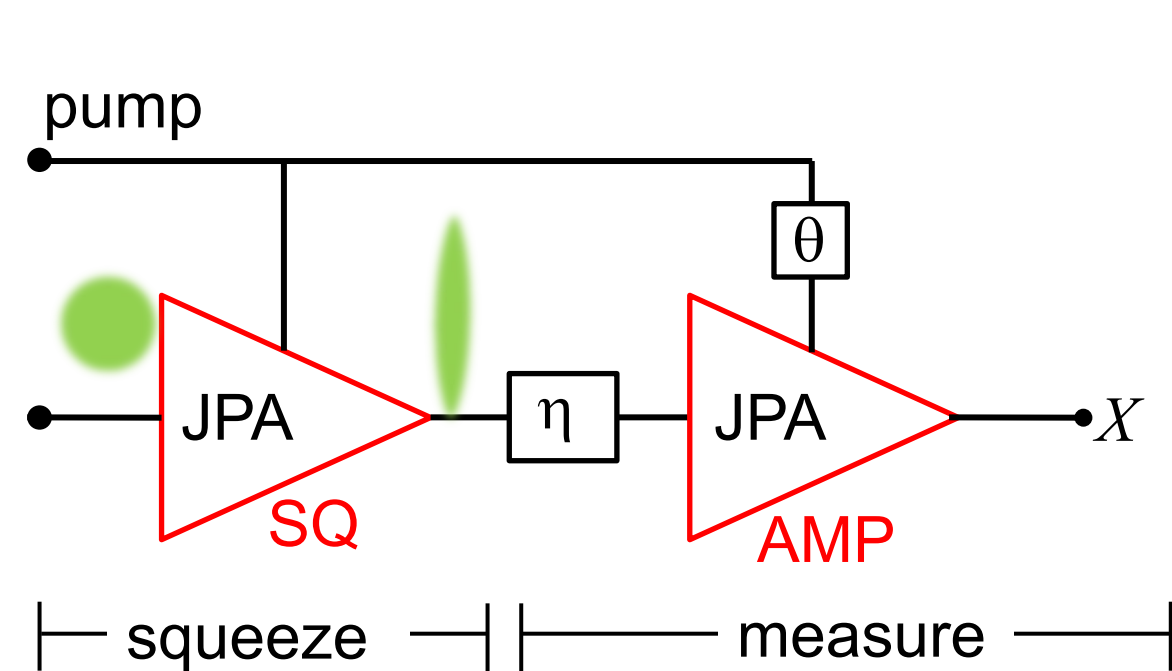
$$\delta^2 \hat{Y} = \frac{G}{2}$$

$$\delta^2 \hat{X} = \frac{1}{2G}$$

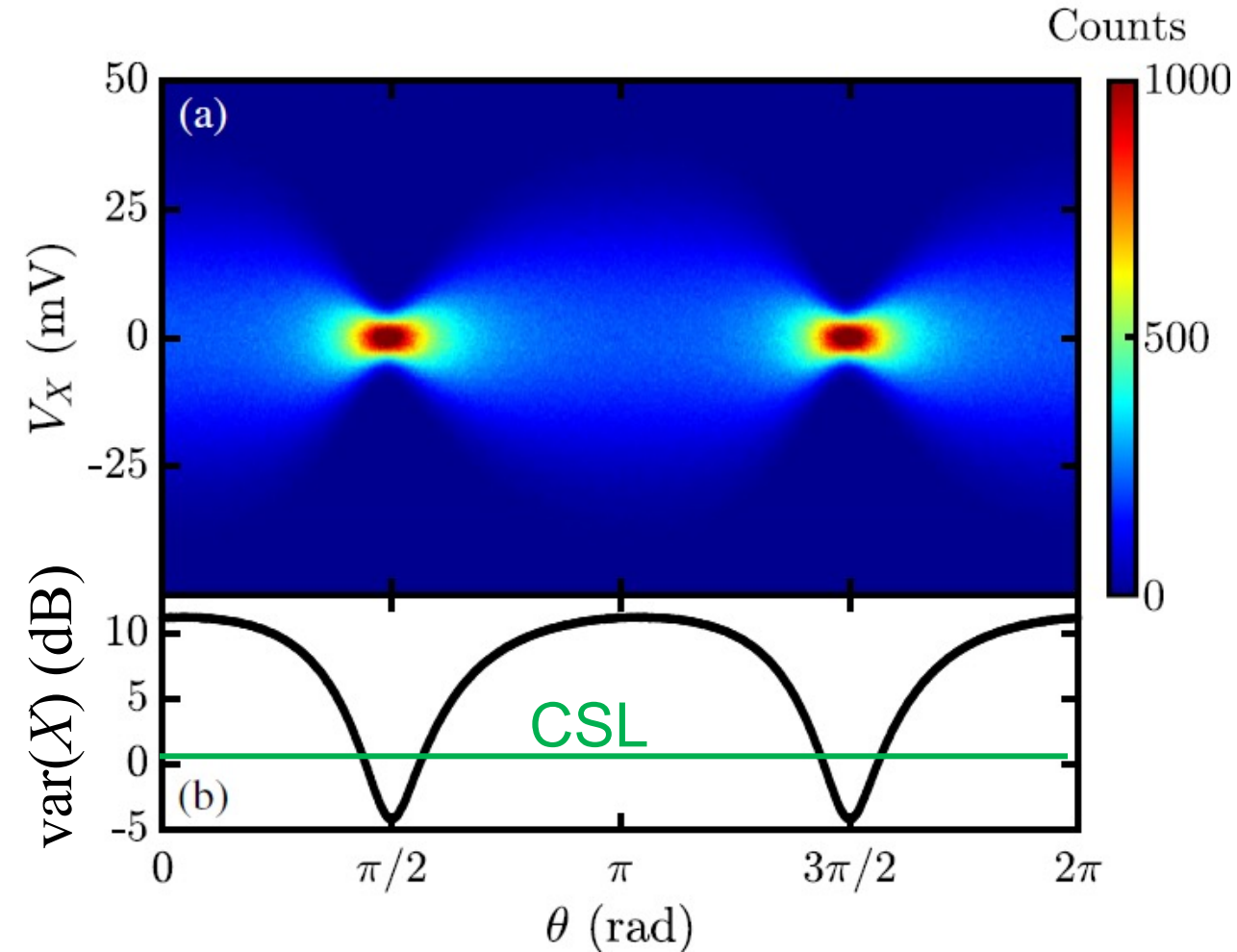
squeezed quadrature: quantum noise suppressed

use JPA to prepare cavity in squeezed state

Demonstration of squeezing and determination of loss: second JPA analyzes squeezed state created by first

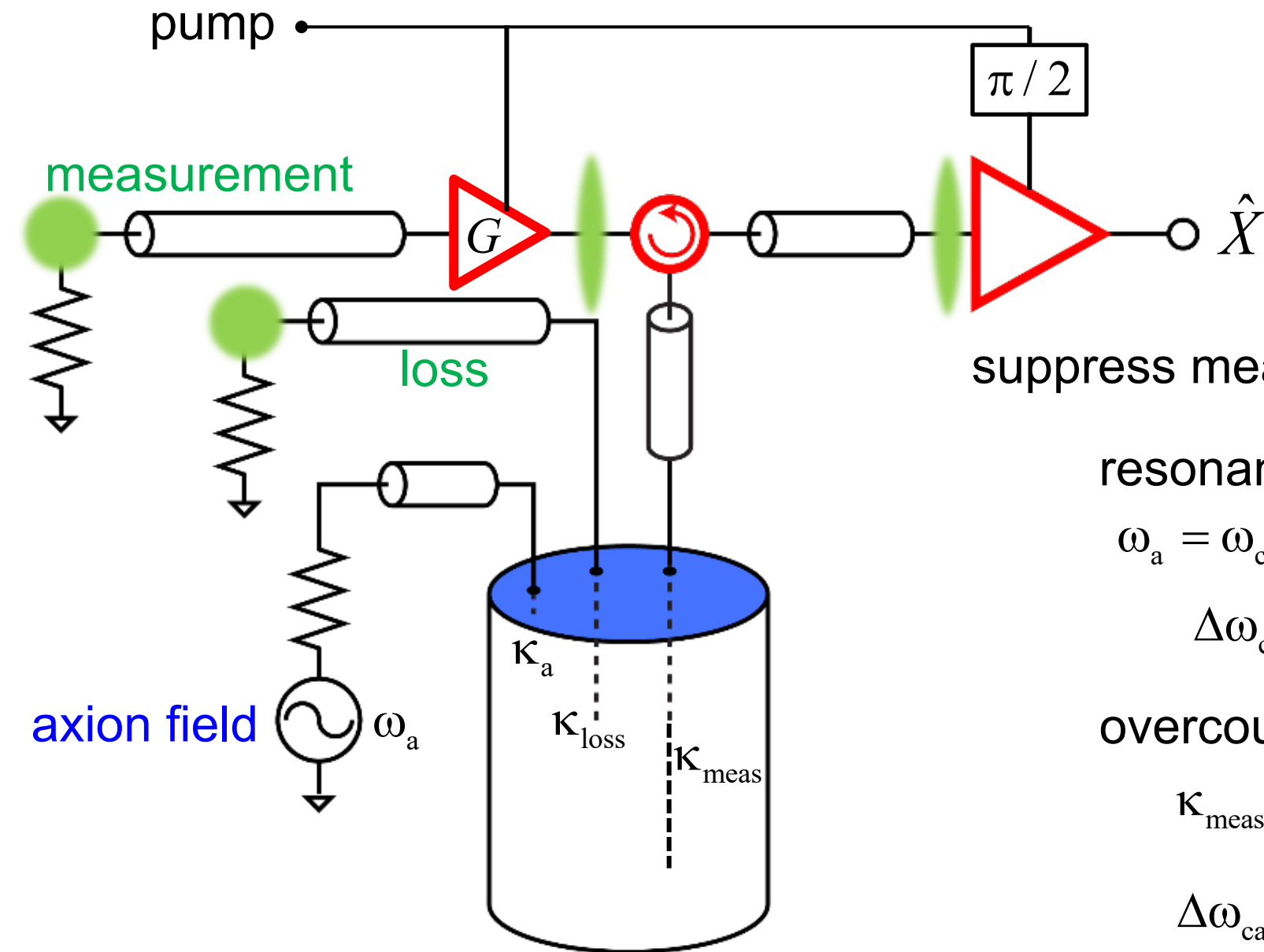


phase θ chooses measured quadrature relative to squeezed quadrature



loss η : 1.63 dB

Squeezing achieves best sensitivity over a wider bandwidth



suppress measurement port noise

resonant signal and critically coupled

$$\omega_a = \omega_{\text{cav}} \quad \kappa_{\text{meas}} = \kappa_{\text{loss}}$$

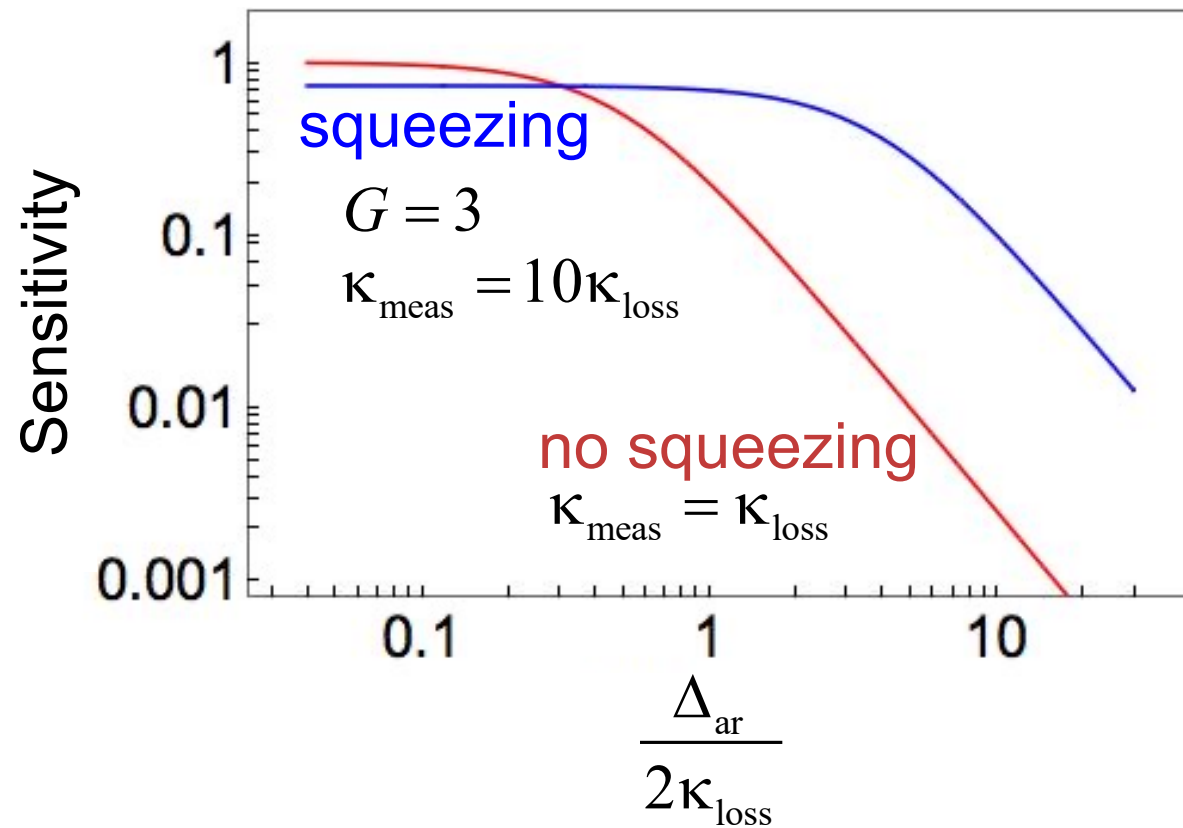
$$\Delta\omega_{\text{cav}} = 2\kappa_{\text{loss}} \quad G = 1$$

overcoupled cavity with squeezing

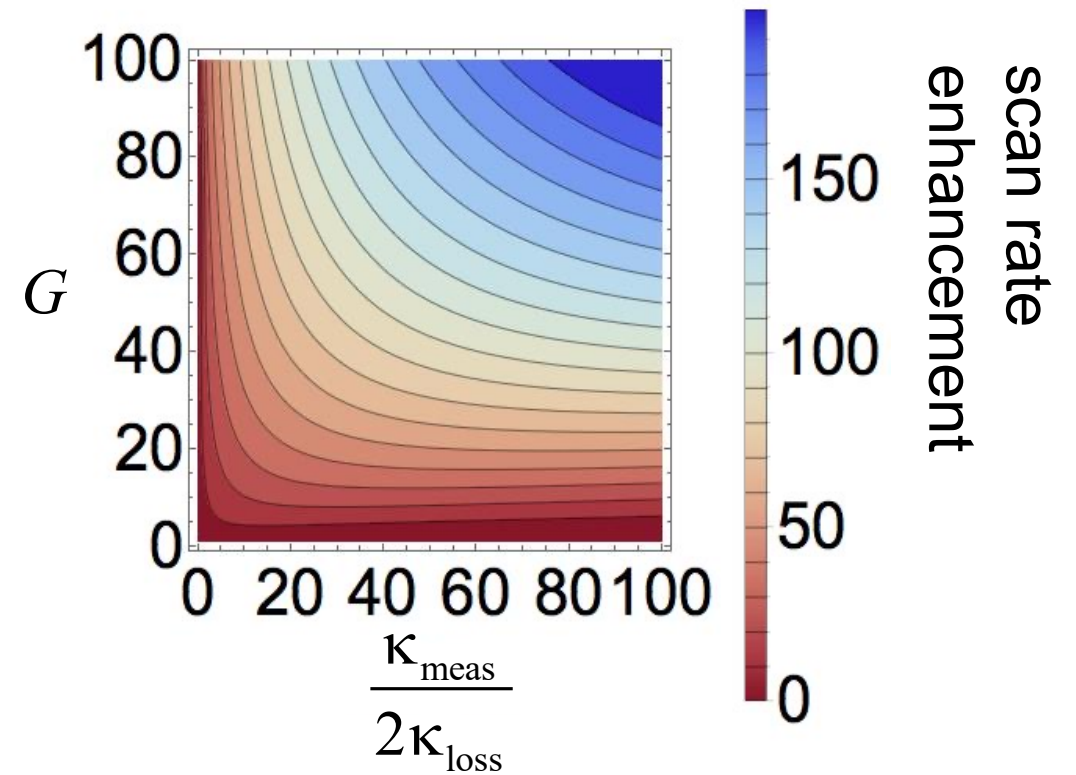
$$\kappa_{\text{meas}} = 9\kappa_{\text{loss}} \quad G \gg 5$$

$$\Delta\omega_{\text{cav}} = 10\kappa_{\text{loss}}$$

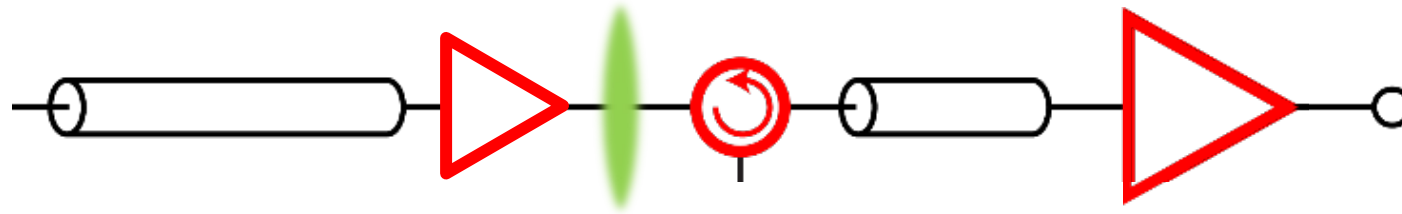
Scan rate enhancement, perfect efficiency



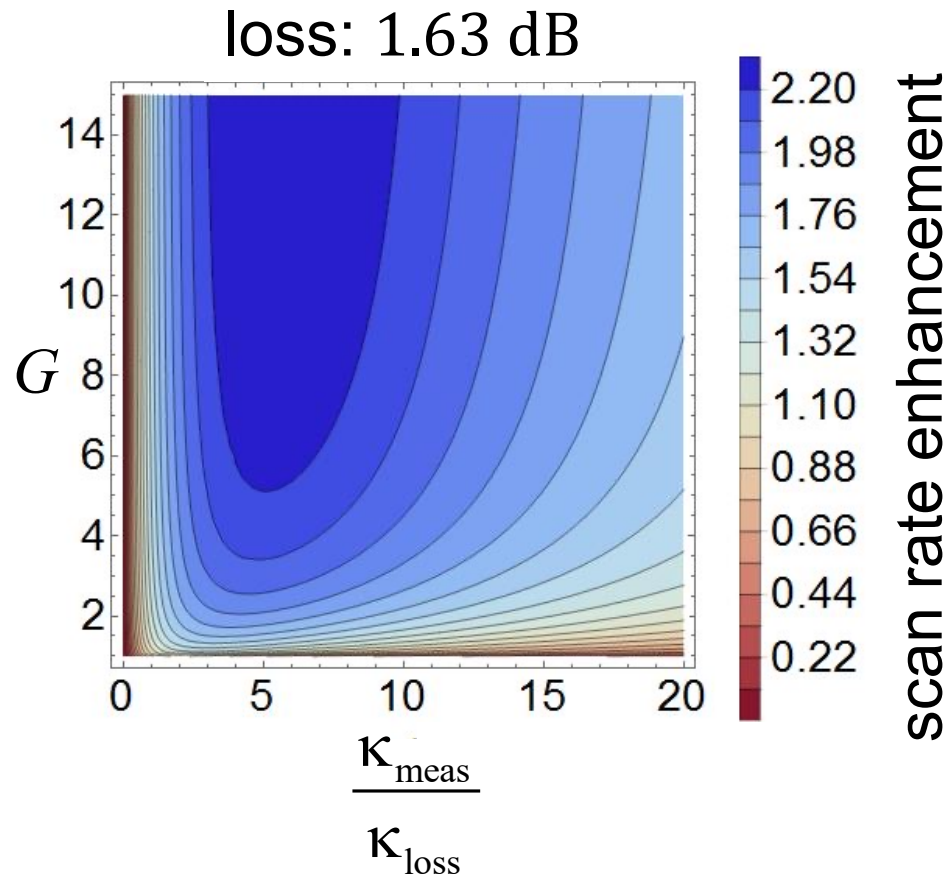
slight reduction in sensitivity
much larger bandwidth



Effect of propagation losses on the scan rate



transmission loss
diminishes benefit



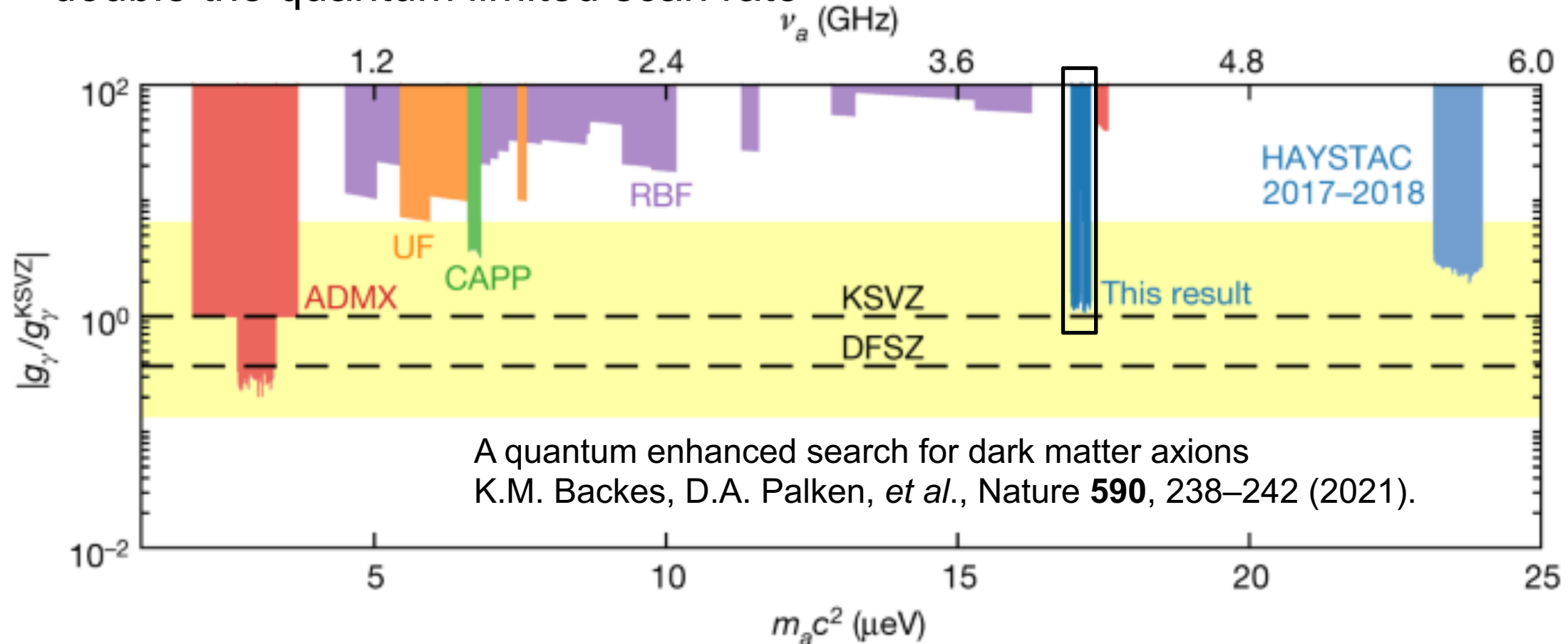
Is doubling the search rate meaningful?

saves 10,000 years or 600 M\$

dramatic improvement with reduced loss

Quantum enhanced sensing is now routine in HAYSTAC

double the quantum limited scan rate



M. J. Jewell *et al.* (HAYSTAC Collaboration)
 Phys. Rev. D **107**, 072007 (2023).

X. Bai *et al.* (HAYSTAC Collaboration)
 Phys. Rev. Lett. **134**, 151006 (2025).

The coherent state limit is hard to beat in a search for fundamental fields³¹

On the measurement of a weak classical force coupled to a quantum-mechanical oscillator. I. Issues of principle

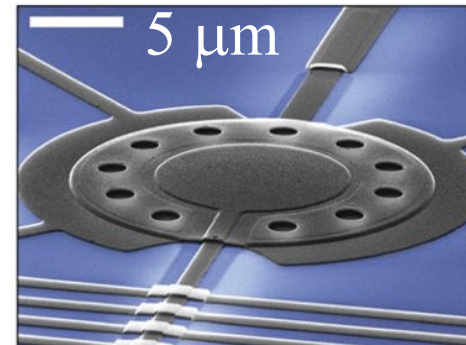
Carlton M. Caves, Kip S. Thorne, Ronald W. P. Drever, Vernon D. Sandberg, and Mark Zimmermann
Rev. Mod. Phys. **52**, 341 – Published 1 April 1980

hard to beat CSL

coupling to fundamental fields: big objects

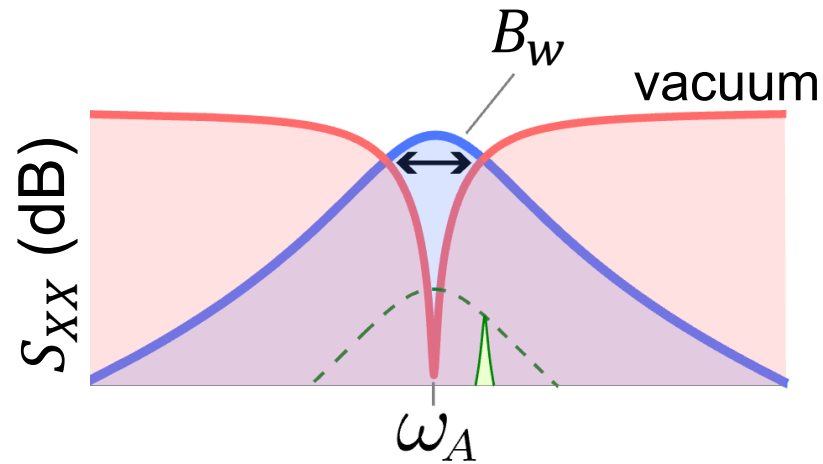
quantum control and measurement: small systems

near technical perfection required

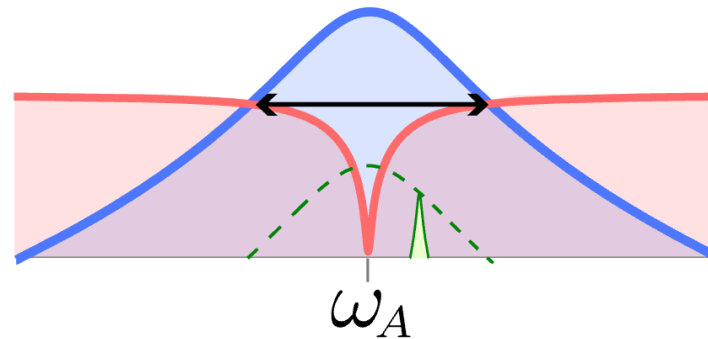


strategy for more quantum enhancement

Amplify signal before encountering measurement port noise

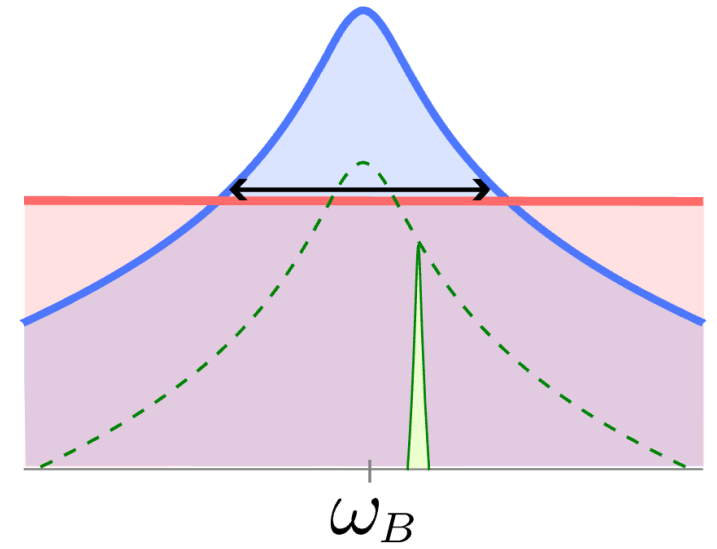


standard quantum limit



×2

squeezing
HAYSTAC apparatus



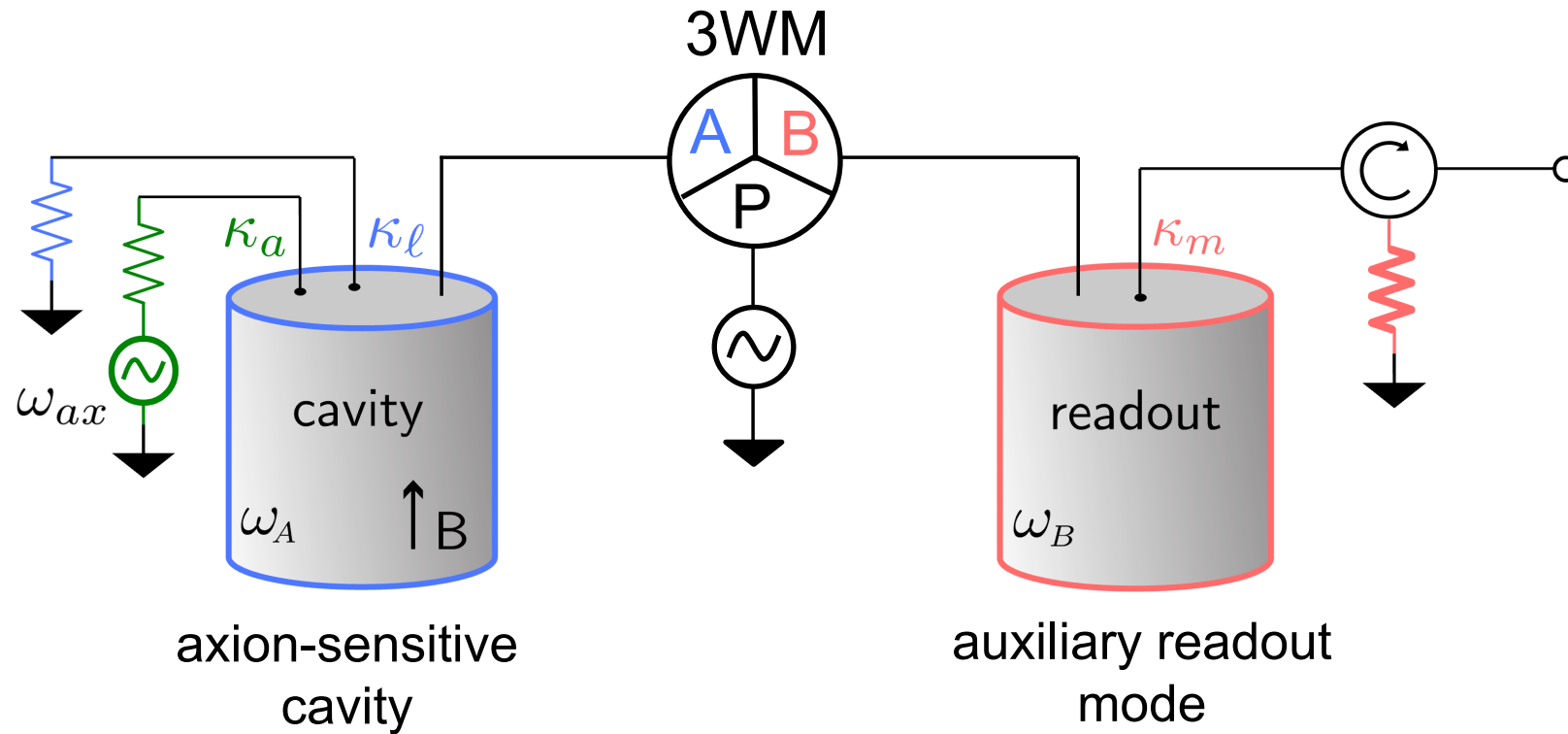
×8.2

cavity entanglement
“CEASEFIRE” Demo

Y. Jiang, E.P. Ruddy, K.O. Quinlan, M. Malnou, N.E. Frattini, KWL, *PRX Quantum* **4**, 020302 (2023)

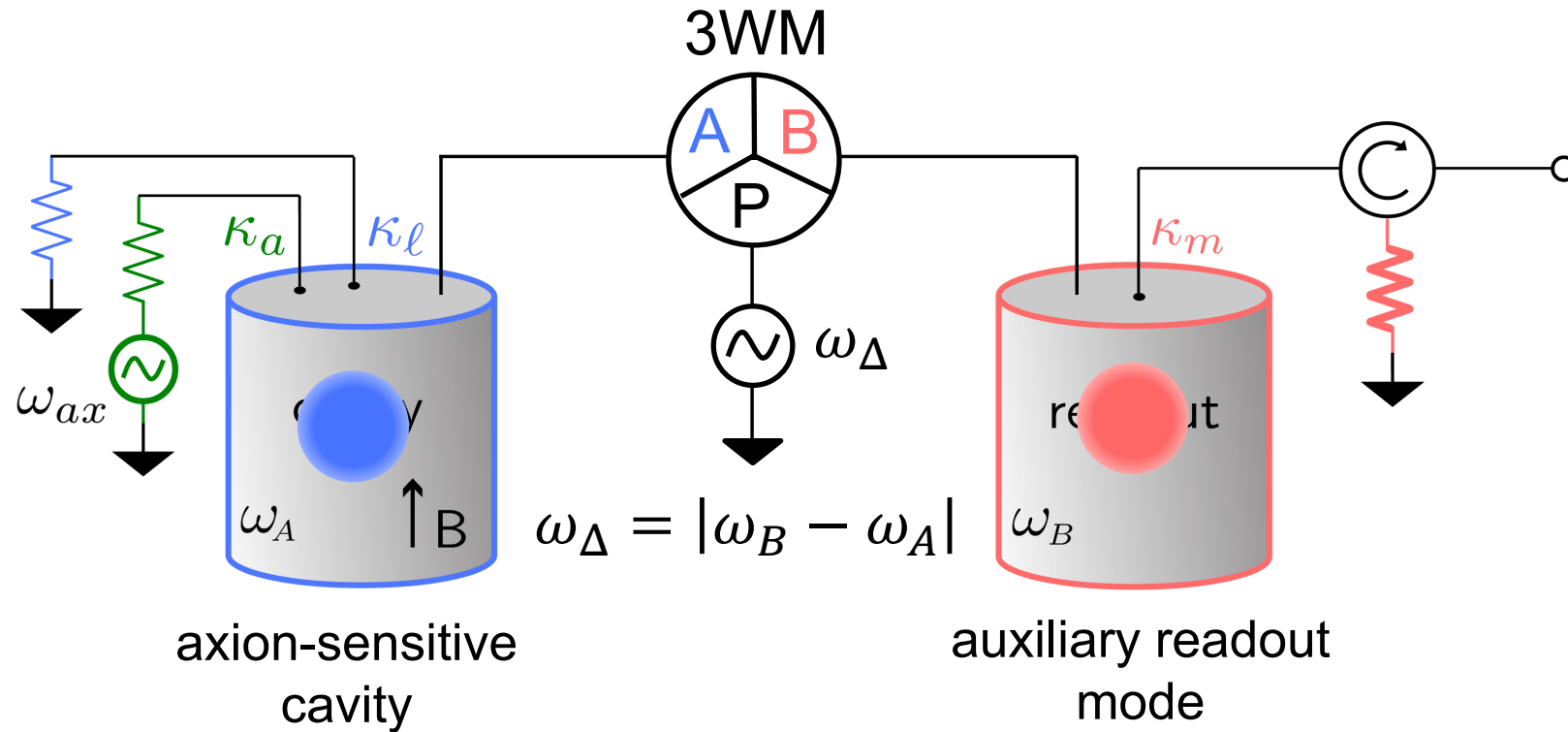
K. Wurtz, Benjamin Brubaker, Y. Jiang, E. Ruddy, Daniel Palken, KWL, *PRX Quantum* **2**, 040350 (2021)

Dynamically couple axion cavity and readout mode by 3-wave mixing



$$\hat{H}_{3WM} \propto (\hat{A} + \hat{A}^\dagger)(\hat{B} + \hat{B}^\dagger)(\hat{P} + \hat{P}^\dagger)$$

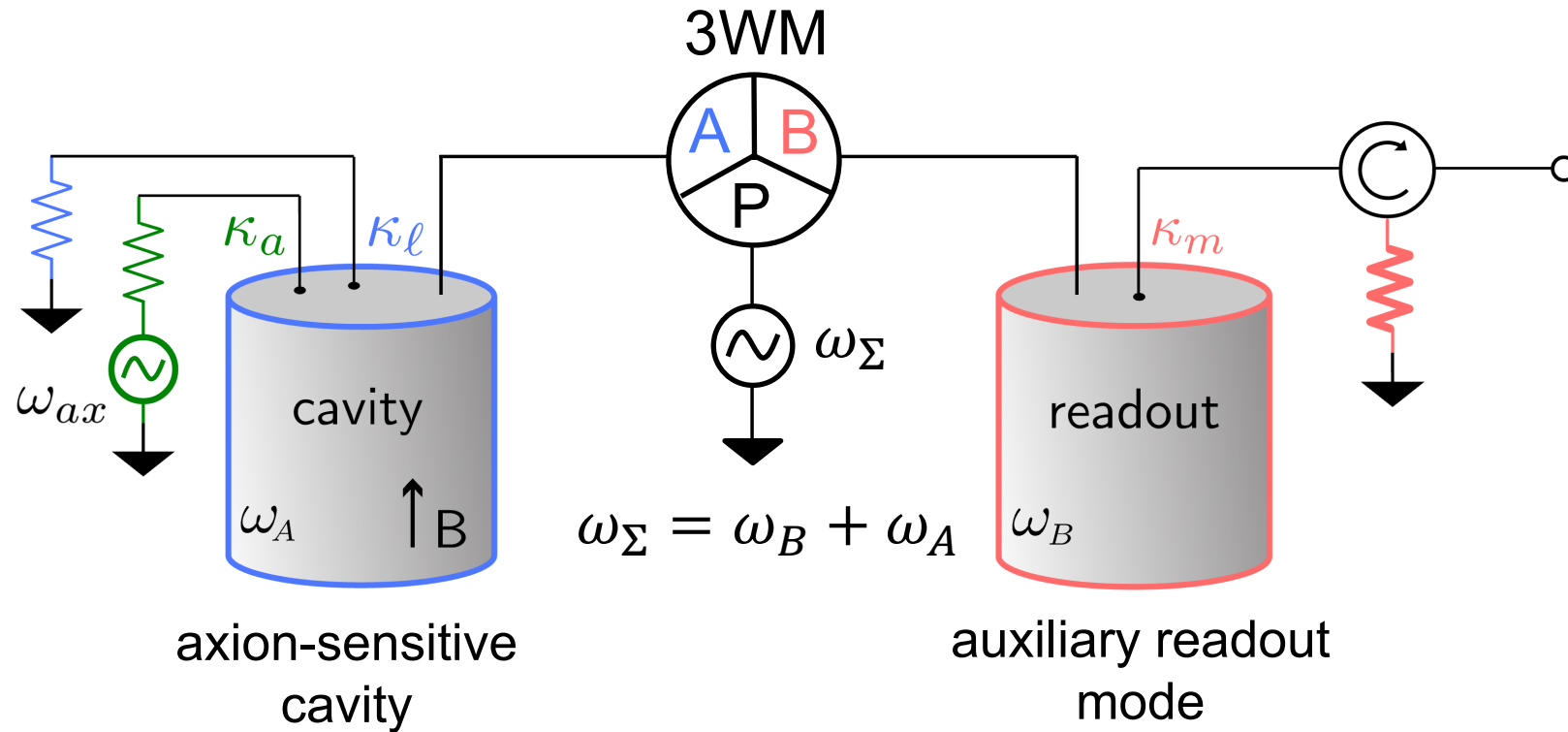
State swapping (C) interaction swaps states between two modes



$$\hat{H}_{3WM} \propto (\hat{A} + \hat{A}^\dagger)(\hat{B} + \hat{B}^\dagger)(\hat{P} + \hat{P}^\dagger)$$

$$\hat{P} \rightarrow g_C e^{-i\omega_\Delta t} + \text{c.c.} \quad \boxed{\rightarrow g_C (\hat{A}\hat{B}^\dagger + \hat{A}^\dagger\hat{B})} \quad \text{state-swapping}$$

Two-mode squeezing (G) induces amplification and entanglement ³⁶



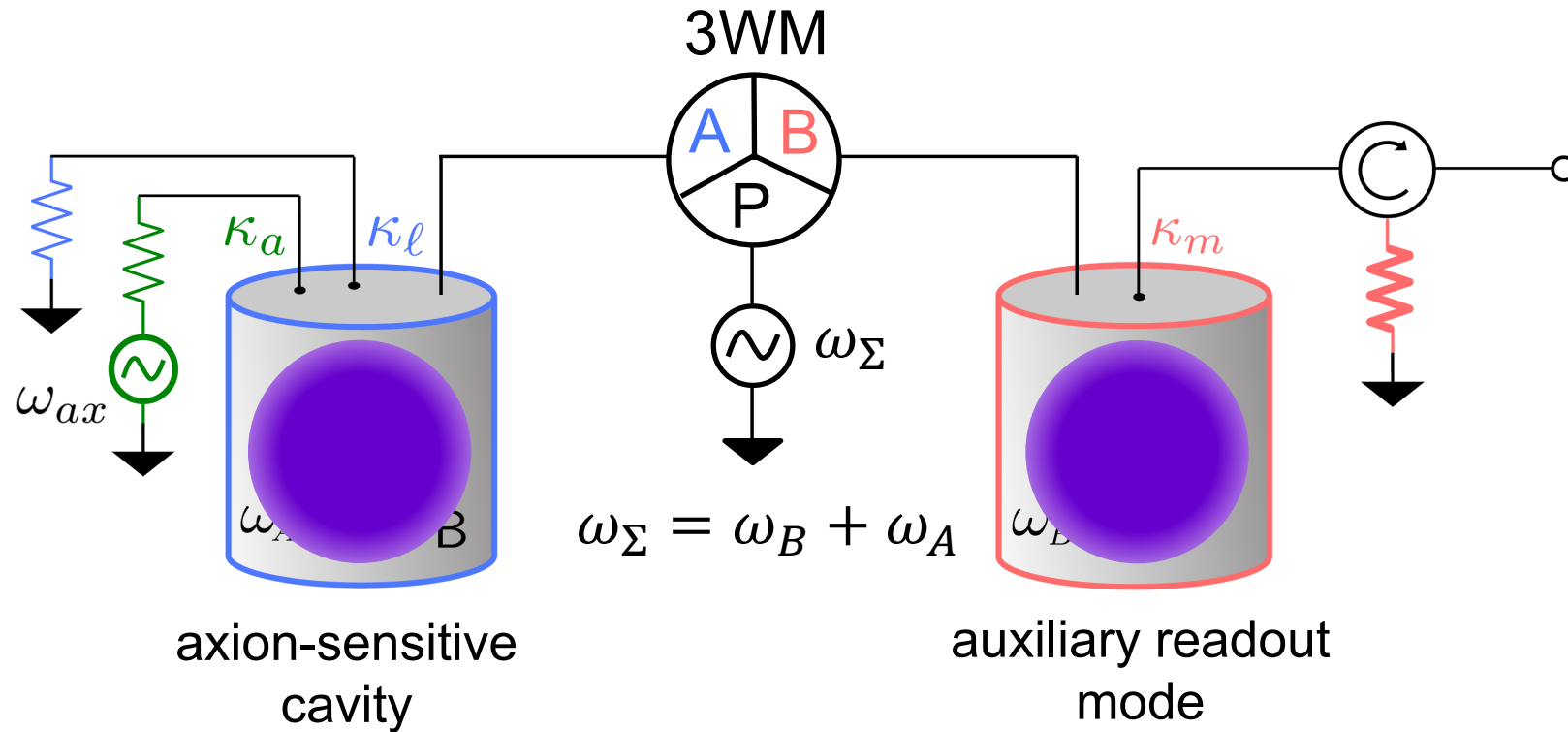
$$\hat{H}_{3WM} \propto (\hat{A} + \hat{A}^\dagger)(\hat{B} + \hat{B}^\dagger)(\hat{P} + \hat{P}^\dagger)$$

$$\hat{P} \rightarrow g_G e^{-i\omega_\Sigma t} + \text{c.c.}$$

$$\rightarrow g_G (\hat{A}^\dagger \hat{B}^\dagger + \hat{A} \hat{B})$$

two-mode squeezing

Two-mode squeezing (G) induces amplification and entanglement ³⁷

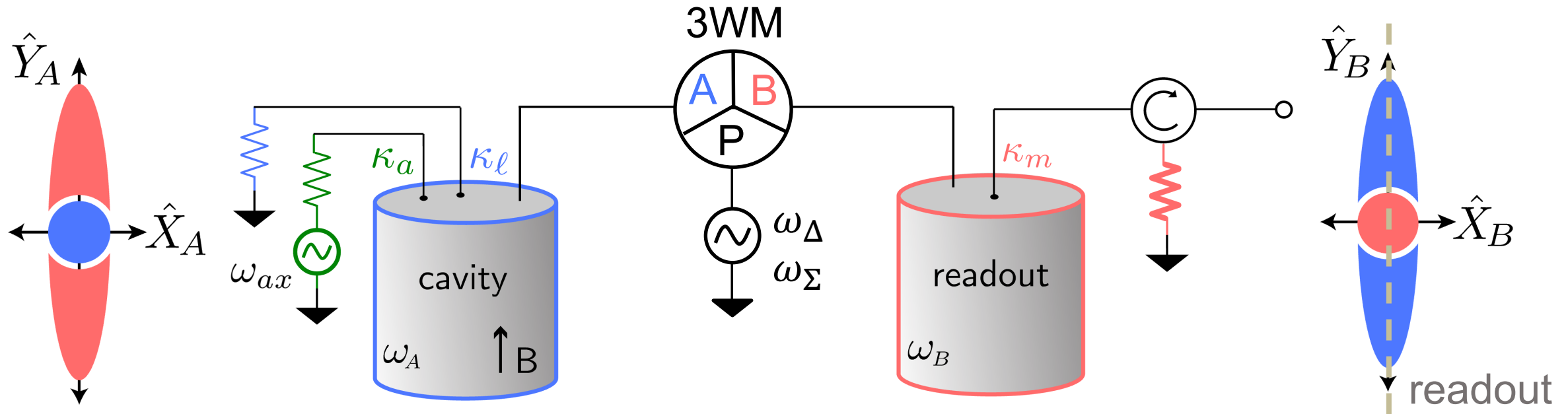


$$\hat{H}_{3\text{WM}} \propto (\hat{A} + \hat{A}^\dagger)(\hat{B} + \hat{B}^\dagger)(\hat{P} + \hat{P}^\dagger)$$

$$\hat{P} \rightarrow g_G e^{-i\omega_\Sigma t} + \text{c.c.}$$

$$\rightarrow g_G (\hat{A}^\dagger \hat{B}^\dagger + \hat{A} \hat{B}) \quad \text{two-mode squeezing}$$

Quantum non-demolition interaction yields bandwidth increase



$$\hat{H}_{3WM} = g_C \hat{A} \hat{B}^\dagger + g_G \hat{A}^\dagger \hat{B}^\dagger + \text{c.c.}$$

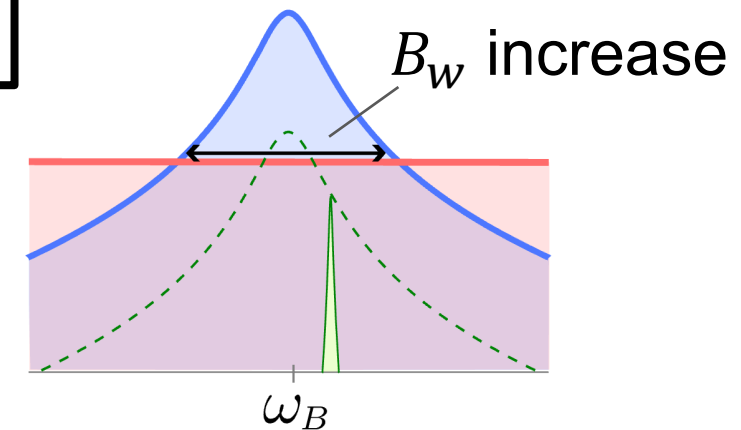
$$\xrightarrow{\text{QND}} 2g \hat{X}_A \hat{X}_B$$

$$d\hat{Y}_B/dt = -2g \hat{X}_A$$

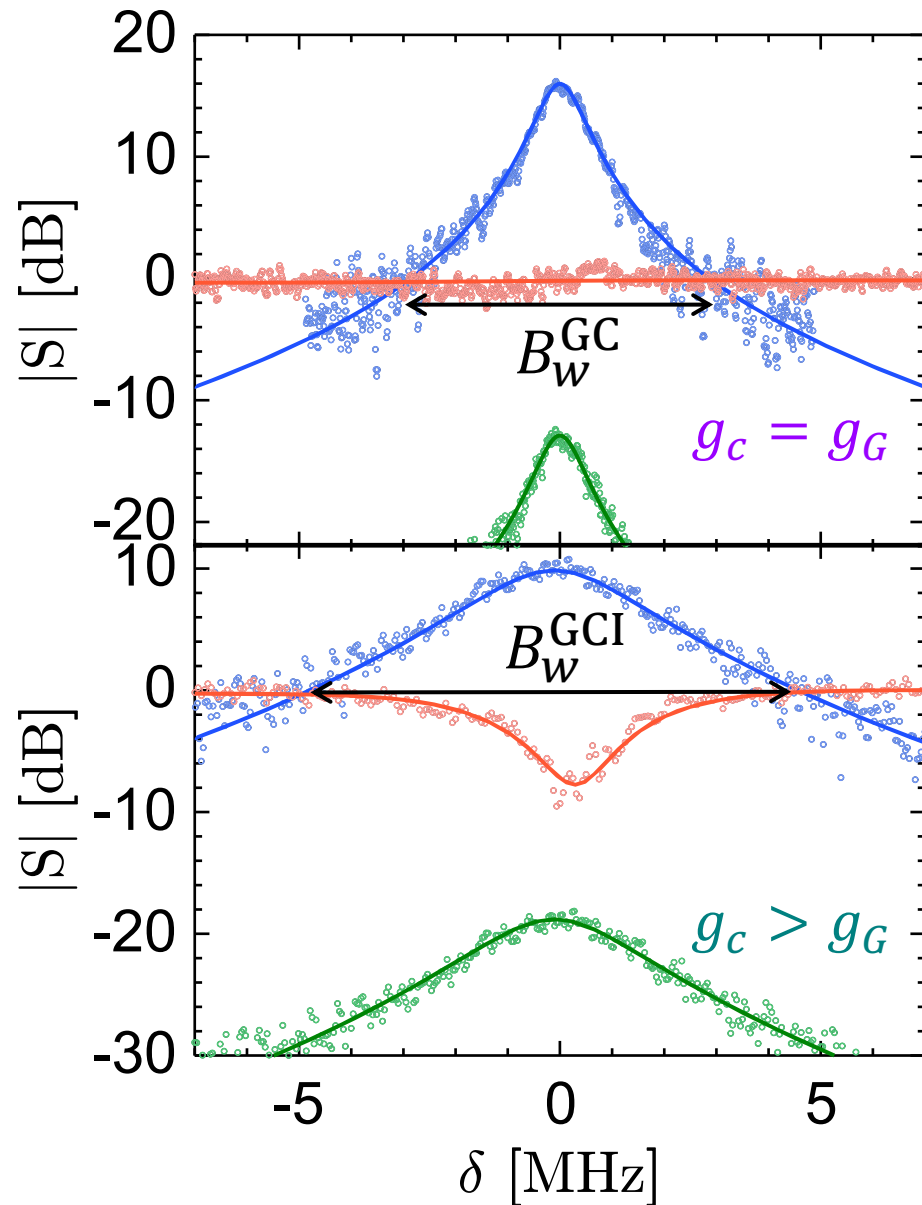
$$d\hat{X}_A/dt = 0$$

amplification

QND



Imbalanced GC operation for further scan rate enhancement



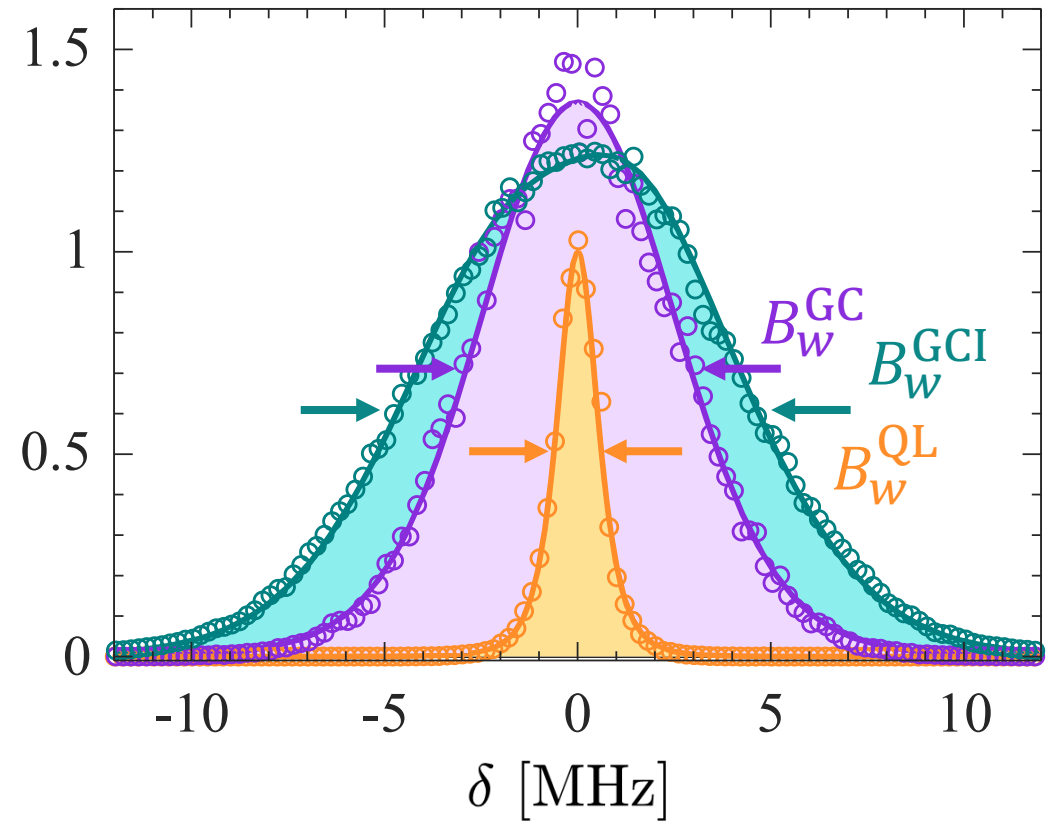
$$B_w^{\text{GC}} = 6 \text{ MHz}$$

$\times 5.6$

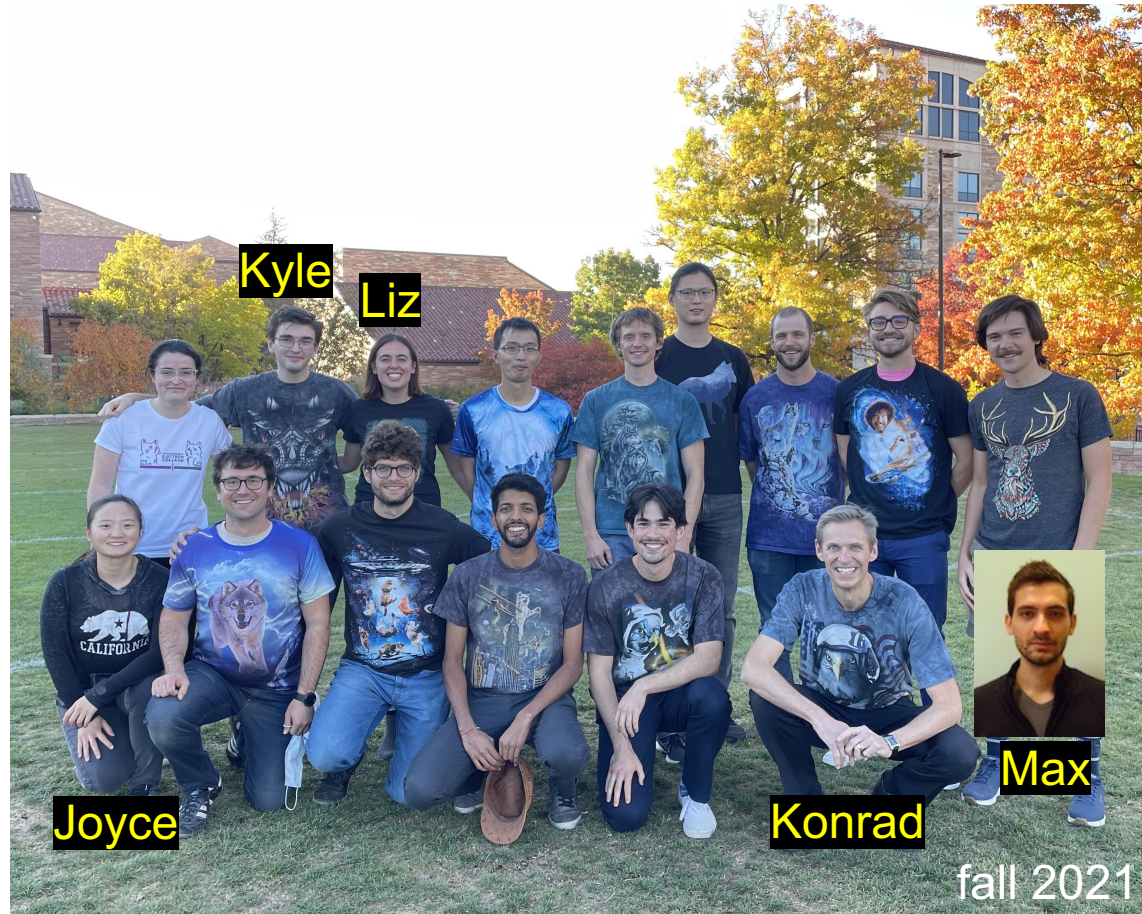
$$B_w^{\text{GCI}} = 10 \text{ MHz}$$

$\times 8.2$

$\text{SNR}^2_{\text{norm.}}$



Acknowledgements for CEASEFIRE data



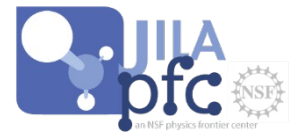
Yale/JILA

Liz Ruddy
Yue (Joyce) Jiang
Kyle Quinlan
Nick Frattini
Konrad Lehnert

NIST Maxime Malnou

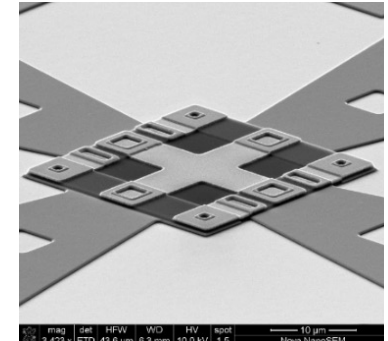
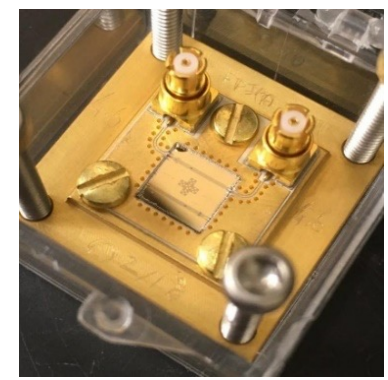
HAYSTAC collaborators

Yale
Berkeley
Johns Hopkins



U.S. DEPARTMENT OF
ENERGY

Office of
Science



The Haloscope At Yale Sensitive To Axion CDM

HAYSTAC