

Opportunities at FCC-*ee* Focusing on Flavor Physics

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My views on the future program

- Building a $10 \times$ better microscope than the LHC is a clear case
We ought to explore Nature to the shortest distance scales that technologies allow
- When HL-LHC stops running, Higgs will have been studied for nearly 30 years
LHC is a Higgs factory, will want better precision & probe unexplored Higgs couplings — like other areas
- We don't know where and how new physics will show up $\Rightarrow$ need broad program
We must study the Higgs as much as possible, but it's no longer uncharted territory (except for 1st gen.)
 $\Rightarrow$ A high- p_T anomaly, a Higgs coupling anomaly, or a flavor anomaly, will be on similar footings
- If any deviation from SM is established, it would make a clear case for FCC- ee
- FCC- ee can be a discovery machine; very rich and challenging physics program
FCC- ee measurements will be essential to fully exploit FCC- hh (α_s , m_t , etc.)

Outline

- Why flavor?
Unique sensitivities
- Beyond LHCb and Belle II: FCC
Huge increases in data, what can they teach us?

New physics scales probed

- Heavy new physics generates dimension > 4 operators in SMEFT

$$\mathcal{L} = \text{SM} + \sum_i \frac{C_{5i}}{\Lambda} \mathcal{O}_{5i} + \sum_i \frac{C_{6i}}{\Lambda^2} \mathcal{O}_{6i} + \dots$$

- Dim-5 $LL\phi\phi$ discovered, iff m_ν violates lepton # ($0\nu\beta\beta?$); No dim-6 term established yet

- Baryon number violation: $\frac{QQQL}{\Lambda^2} \Rightarrow \Lambda \gtrsim 10^{16} \text{ GeV}$

- Higgs & precision electroweak: $\frac{(\phi D^\mu \phi)^2}{\Lambda^2} \Rightarrow \Lambda \gtrsim 10^4 \text{ GeV}$

- Flavor and CP violation (and EDMs): $\frac{QQQQ}{\Lambda^2} \Rightarrow \Lambda \gtrsim 10^{(3\dots 8)} \text{ GeV}$

Flavor and CPV are the only experimental probes of the $10^2 - 10^5 \text{ TeV}$ scale

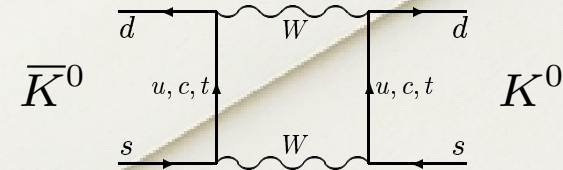
- New physics could show up any time the sensitivities improve (by a substantial amount)

Origin of high scale sensitivity

- Back of an envelope calculation of Δm_K : loop, CKM, GIM suppressions
- Why is $\Delta m_K/m_K \sim 7 \times 10^{-15}$?

In the SM:
$$\frac{\Delta m_K}{m_K} \sim \alpha_w^2 |V_{cs} V_{cd}|^2 \frac{m_c^2}{m_W^4} f_K^2$$

Predicted $m_c \sim 1.5 \text{ GeV}$ (Gaillard & Lee; Vainshtein & Khriplovich, 1974)



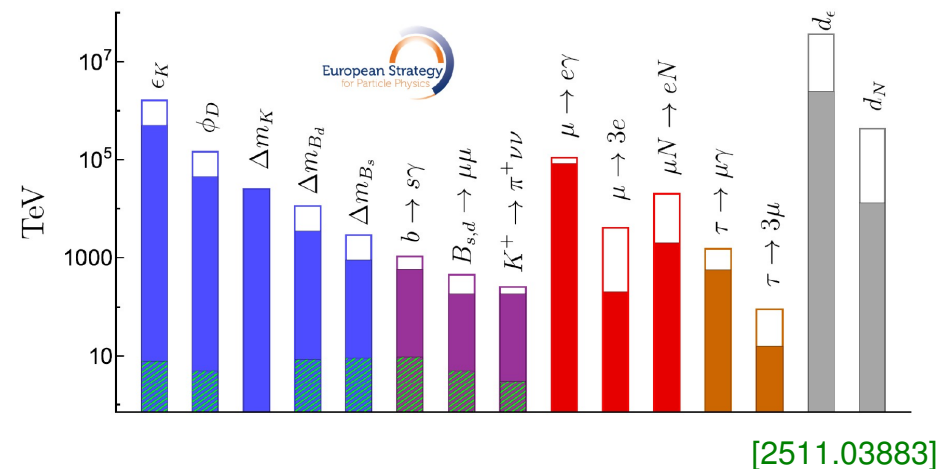
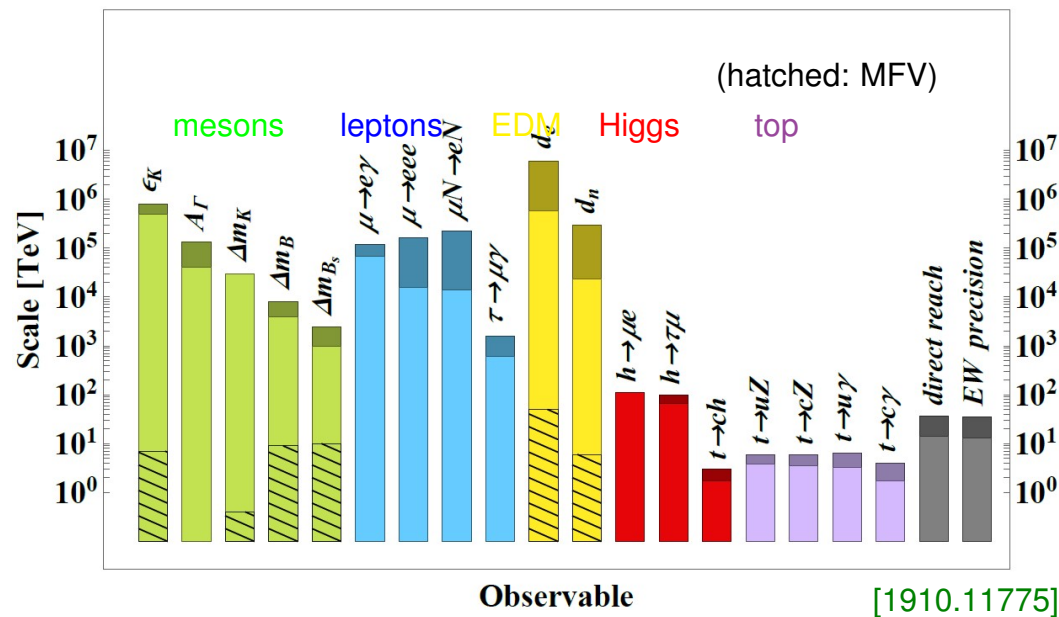
- If exchange of a heavy particle X contributes at the SM level:

$$\frac{\Delta m_K^{(X)}}{\Delta m_K} \sim \frac{g^2 \Lambda_{\text{QCD}}^3}{M_X^2 \Delta m_K} \Rightarrow M_X > g \times 10^3 \text{ TeV}$$

- Alternatively, sensitivity to TeV-scale particles with one-loop couplings [$g \sim \mathcal{O}(10^{-3})$]

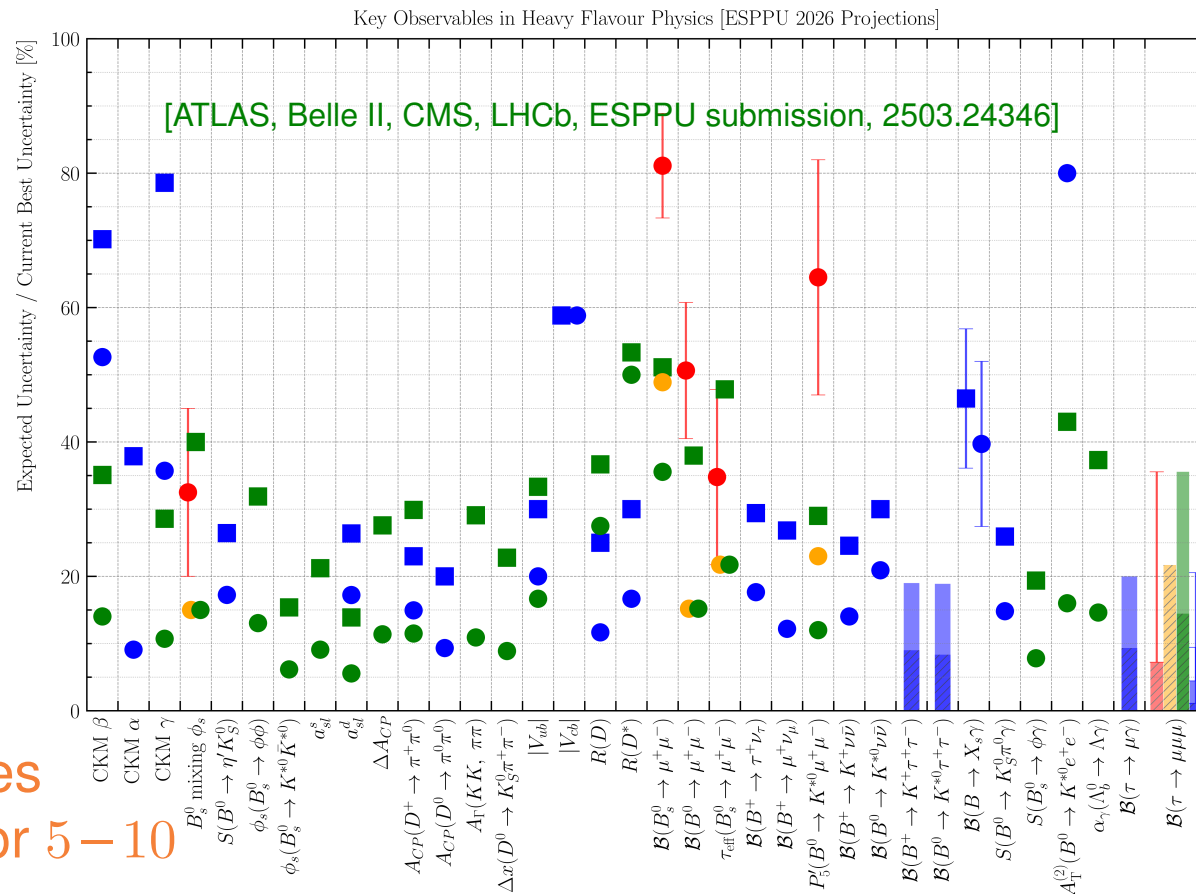
Similar story for many other flavor-changing neutral current (FCNC) processes

Scales, as shown in European strategy

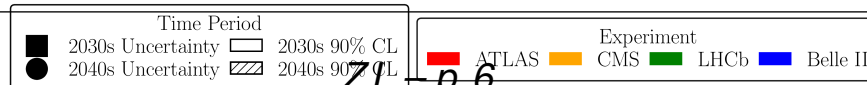


- All TeV-scale NP models must contain some mechanism to avoid violating constraints
Models devised to make deviations from SM small, revisit model building when tensions with SM arise
- Suppressions in SM are strongest for kaons, often Δm_K & ϵ_K are the most constraining

Large upcoming improvements

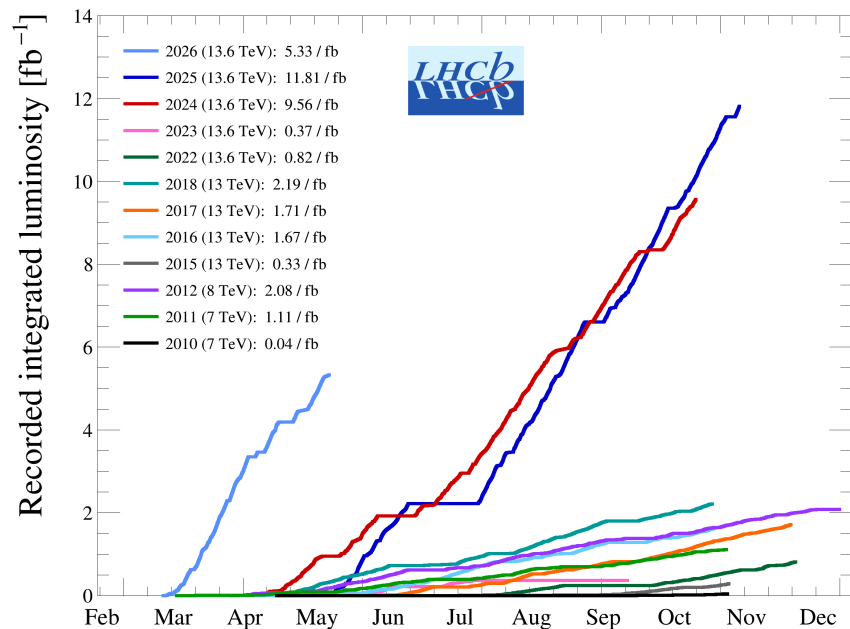


Many uncertainties
will shrink by factor 5–10



Past LHCb and Belle II data taking

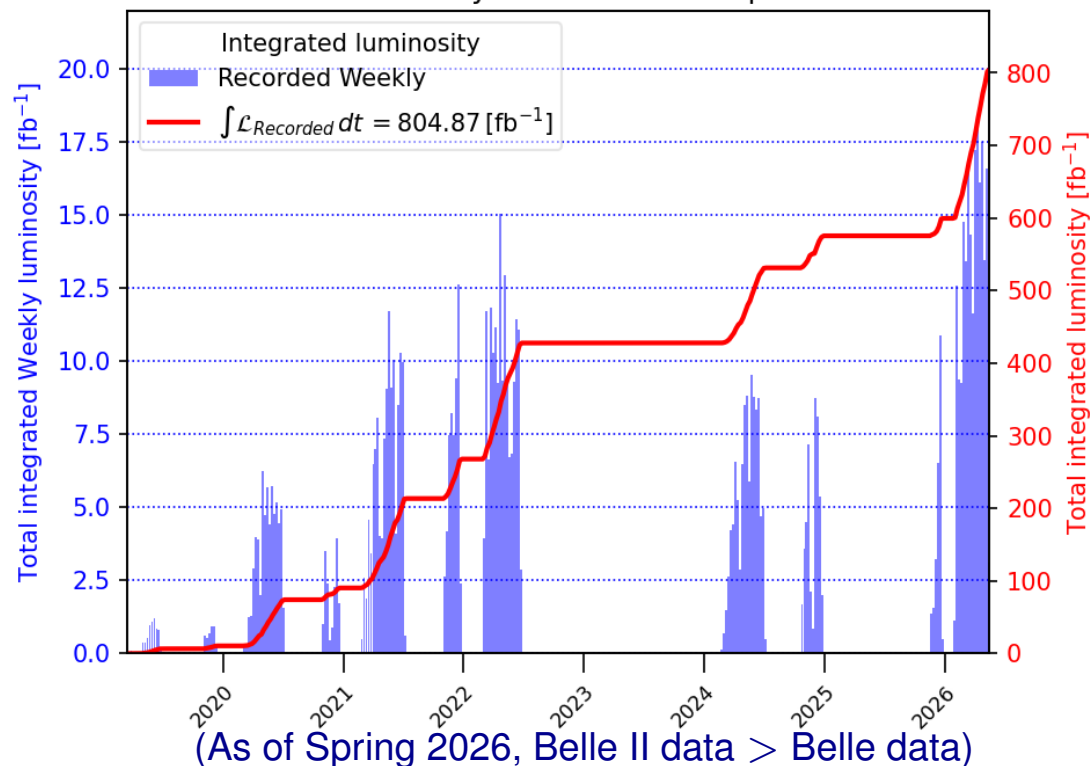
Total recorded luminosity by year – pp



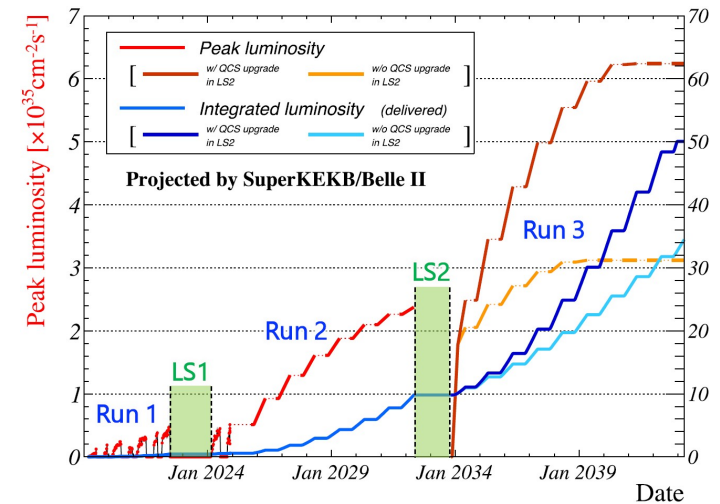
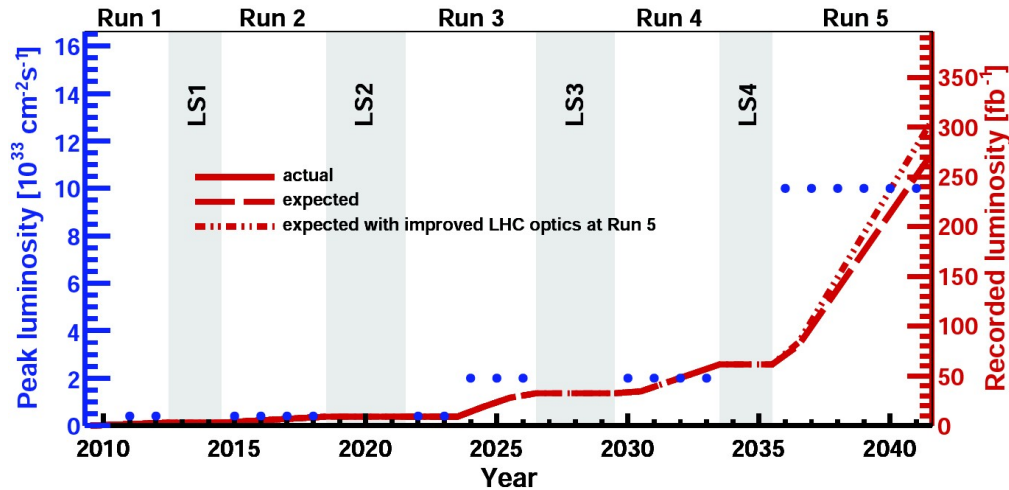
(Hardly any LHCb result is available yet from Run 3)

Belle II Online luminosity

Exp: 7-42 - All runs



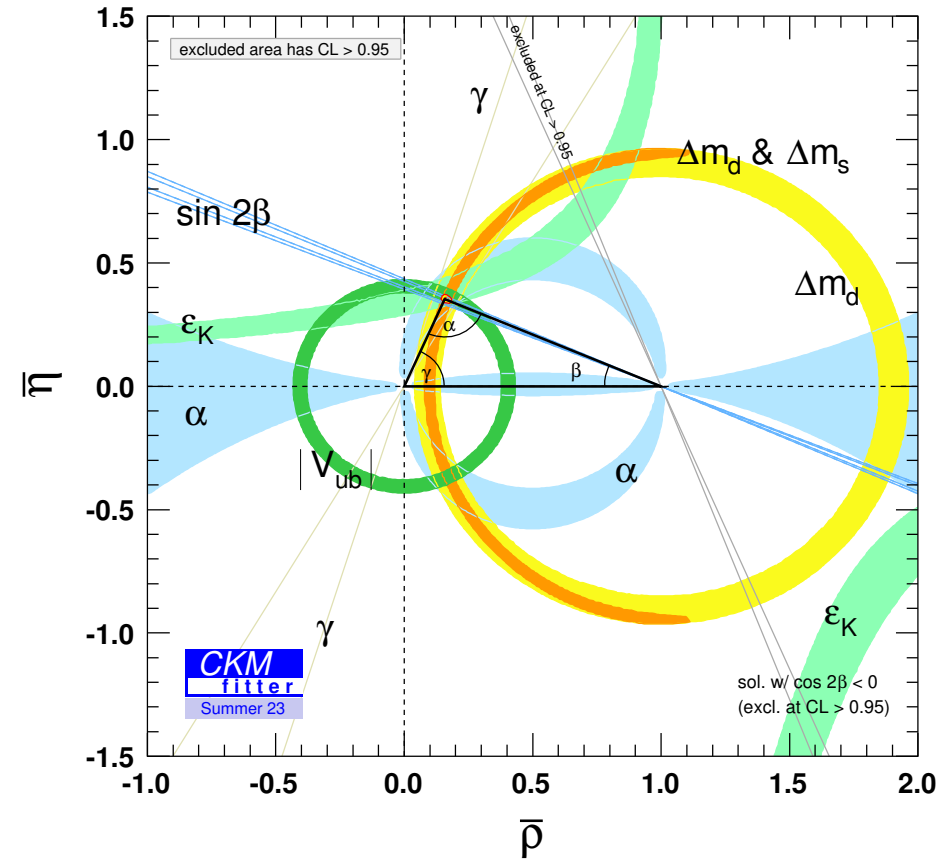
Future LHCb and Belle II plans



- LHCb upgrade in LS2 (inst. lumi.: 2×10^{33})
- LHCb Upgrade II in LS4 (inst. lumi.: 1.5×10^{34})
- ATLAS & CMS competitive in some modes
- Belle II goal: over $50 \times$ Belle data set
- Discussions about physics & feasibility of an upgrade (polarization? 250/ab?)

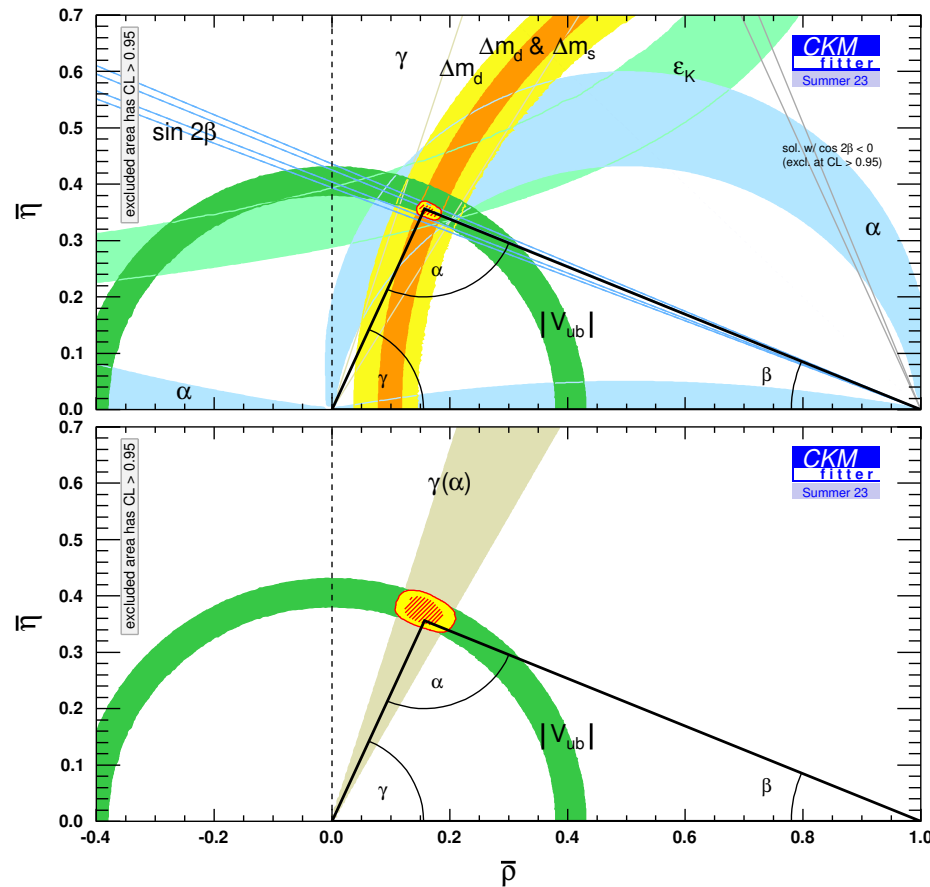
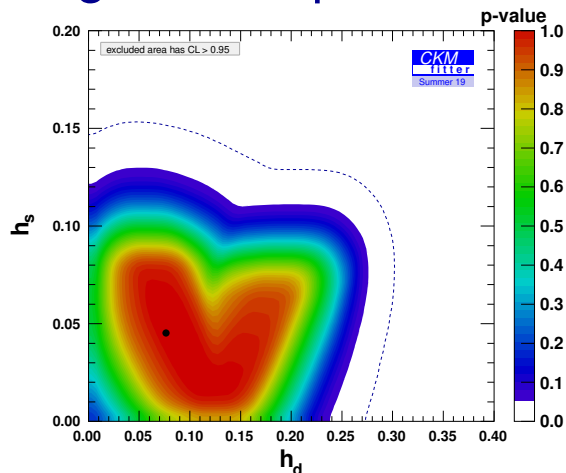
Snapshot: CKM fit in the SM

- Spectacular progress in the last 25 years
- The CKM mechanism describes consistently CP violation and flavor changing processes
- We did not know this, not even at $\mathcal{O}(1)$ level before BaBar and Belle



Snapshot: CKM fit in the SM

- Spectacular progress in the last 25 years
- Looser constraints if NP is allowed in the fit
Full fit (upper) vs. tree-dominated (lower) plot
- Implies, e.g., that 10–20% corrections to $B - \bar{B}$ mixing are still possible



Hints of deviations from the SM

- From a distance, everything looks fine... looking closer:

Less than half of B decays measured; most are incalculable, we have theories for some (HQET, SCET)

- Charged-current semileptonic $b \rightarrow c$ decays (e.g., $B \rightarrow D^{(*)} \ell \bar{\nu}$)
- Neutral-current (FCNC) semileptonic decays (e.g., $B \rightarrow K^{(*)} \ell \bar{\ell}$)
- Charged-current nonleptonic $b \rightarrow c$ decays (e.g., $B \rightarrow D^{(*)} h$ [$h = K, \pi$])
- Dominantly FCNC nonleptonic decays (e.g., $B \rightarrow K h$)

There are more...

- Intriguing tensions with the SM $\Rightarrow$ experimental scrutiny, new theory ideas
- What are smallest deviations from SM, which can be unambiguously established?

Breadth and surprises

- Most cited physics paper of each B factory was not in the planned program (#s mid-April)

- BaBar:

Evidence for an excess of $\bar{B} \rightarrow D^{(*)} \tau^- \bar{\nu}_\tau$ decays #2
BaBar Collaboration • J.P. Lees (Annecy, LAPP) et al. (May, 2012)
Published in: *Phys.Rev.Lett.* 109 (2012) 101802 • e-Print: [1205.5442](#) [hep-ex]
[pdf](#) [links](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [1,364 citations](#)

- Belle:

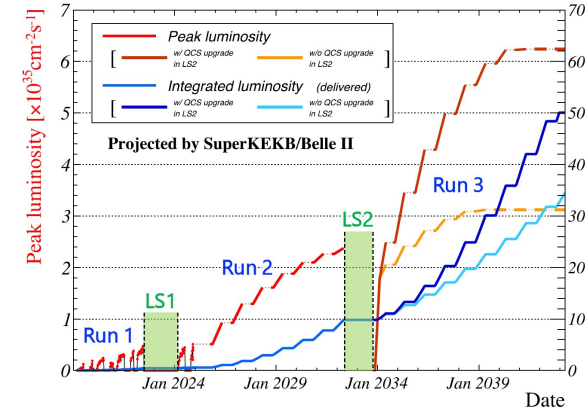
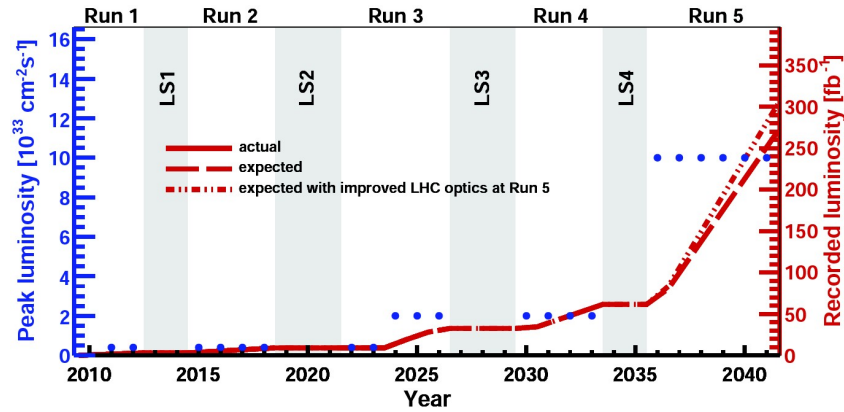
Observation of a narrow charmonium-like state in exclusive $B^\pm \rightarrow K^\pm \pi^+ \pi^- J/\psi$ decays #1
Belle Collaboration • S.K. Choi (Gyeongsang Natl. U.) et al. (Sep, 2003)
Published in: *Phys.Rev.Lett.* 91 (2003) 262001 • e-Print: [hep-ex/0309032](#) [hep-ex]
[pdf](#) [links](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [2,938 citations](#)

- LHCb:

Observation of $J/\psi p$ Resonances Consistent with Pentaquark States in $\Lambda_b^0 \rightarrow J/\psi K^- p$ Decays #1
LHCb Collaboration • Roel Aaij (CERN) et al. (Jul 13, 2015)
Published in: *Phys.Rev.Lett.* 115 (2015) 072001 • e-Print: [1507.03414](#) [hep-ex]
[pdf](#) [links](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [2,129 citations](#)

- Huge increases in data often yielded unexpected discoveries

Far future flavor



● Of the future colliders discussed, only FCC would go well beyond LHCb + Belle II goals

FCC- ee data sets for flavor

- Production yields, compared to Belle II goals:

[Monteil & Wilkinson, 2106.01259]

Particle production (10^9)	$B^0 + \bar{B}^0$	$B^\pm$	$B_s^0 + \bar{B}_s^0$	$\Lambda_b + \bar{\Lambda}_b$	$B_c^\pm$	$c\bar{c}$	$\tau^+\tau^-$
Belle II (50 ab^{-1})	27	27	tbd	—	—	65	45
tera- Z ($5 \times 10^{12} Z$)	600	600	150	130	3	600	170

Comparison with LHCb more complex: roles of trigger, LHCb has advantage if final state is fully reconstructed, if there are neutrals, tera- Z may win

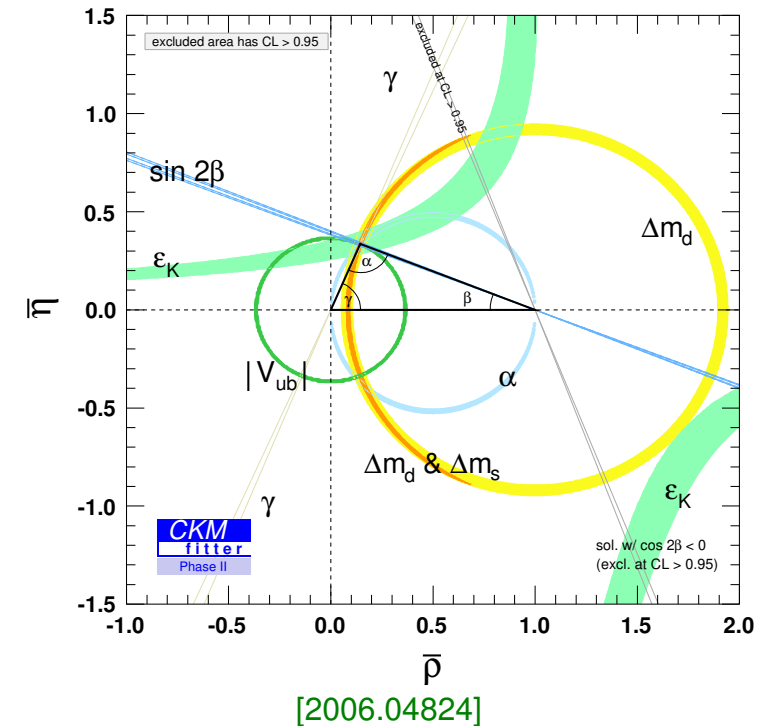
- WW threshold ($10^8 WW$): $W \rightarrow b\bar{c}$ can give a qualitatively new determination of $|V_{cb}|$
Estimate 0.2% uncertainty, independent of B decays [Monteil @ 7th FCC Workshop, Jan 2024]; [2405.08880]
- $t\bar{t}$ threshold: m_t is a flavor parameter... can FCNC sensitivity surpass that of HL-LHC?

Flavor physics at FCC- ee

- $10^5 \times \text{LEP}$ is the right target (mass scale) $\propto (\text{uncertainty})^{-1/2} \propto (\text{stat})^{-1/4}$
- Can one appreciate / anticipate a 10^5 improvement? (Recall: Belle II goal / ARGUS $\sim 10^5$)
Theory and experimental techniques both changed a lot! (e.g., full hadronic reconstruction)
Asymmetric B factories on $\Upsilon(4S)$ were devised for CP violation, less ideal for (semi)leptonic decays
- What was not even tried at LEP? (due to lack of statistics or lack of physics interest)
- Some rare decay sensitivities may improve linearly with statistics; e.g., $Z \rightarrow \mu\tau, \mu e$, etc.
- A lot of what's usually called precision electroweak, also concern flavor (R_b, R_ℓ for each lepton flavor, τ lifetime & mass, etc.)

Towards theory at the per mille level

- Theory uncertainty of γ is negligible (2nd order EW)
World average $\gamma = (66.4 \pm 2.8)^\circ$
Theory uncert. of everything else nontrivial at $\sim 1\%$ level
- Most precise so far: $\sin 2\beta = 0.710 \pm 0.011$ (22.62 ± 0.45) $^\circ$
Precision of γ may overtake that of β
- Can the precision of β keep up with statistics?
There are claims of possibly large V_{ub} (“penguin”) contamination
- Which other measurements can reach such precision?
(Both theory and experiment)



$B_q \rightarrow J/\psi h$ using $SU(3)$ flavor

- Expand amplitudes: $A(B_q \rightarrow J/\psi h) = (V_{cb}^* V_{cq})(A_c^{(0)} + \varepsilon A_c^{(1)}) + (V_{ub}^* V_{uq})A_u^{(0)} + \dots$
 - $SU(3)$ flavor symmetry $\Rightarrow 5 A_c^{(0)}, 4 A_c^{(1)}, 3 A_u^{(0)}$ relations [ZL & Robinson, 1507.06671]
 - 16 observables vs. 6 independent complex amplitudes: $1 A_c^{(0)}, 2 A_c^{(1)}, 3 A_u^{(0)}$
 - 4 relations when working to this order
-
- “New” relation: (might have been implicitly known)

$$S_{\psi K_S}^d - s_{2\beta} = -|V_{cd}/V_{cs}|^2 (c_{2\beta}/c_{2\beta_s}) (S_{\psi K_S}^s + s_{2\beta_s})$$

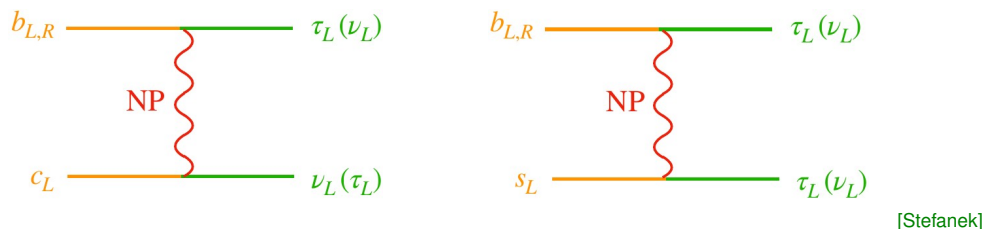
$$\Rightarrow S_{\psi K_S}^d - \sin 2\beta = 0.001 \pm 0.015$$
[ZL, Y. Nir, R. Schein, 2506.21675]
 - Uncertainty can be reduced by better measurement of $S_{\psi K_S}^s$ in $B_s \rightarrow \psi K_S$ (Run 1 only)

CP violation in $B^\pm \rightarrow \pi^\pm \pi^0$

- Direct CP asymmetry: $A_{CP}(B^\pm \rightarrow \pi^\pm \pi^0) = \frac{\Gamma(B^- \rightarrow \pi^- \pi^0) - \Gamma(B^+ \rightarrow \pi^+ \pi^0)}{\Gamma(B^- \rightarrow \pi^- \pi^0) + \Gamma(B^+ \rightarrow \pi^+ \pi^0)}$
World average: $A_{CP}(B^\pm \rightarrow \pi^\pm \pi^0) = -0.01 \pm 0.04$ (past theory papers: $10^{-4} - 10^{-2}$)
- In the “isospin limit”: $A_{CP}(B^\pm \rightarrow \pi^\pm \pi^0) = 0$, however: [Grossman, ZL, Nir, 2605.04137]
electroweak penguins, $\pi - \eta$ mixing, isospin violation in QCD penguins, $\Delta I = 5/2$
Our SM prediction: $A_{CP}(B^\pm \rightarrow \pi^\pm \pi^0) \sim 3 \times 10^{-3} \Rightarrow$ try to measure better!
- Understanding the accuracy of isospin relations in charmless B decays is important:
 - $A_{CP}(B^\pm \rightarrow \pi^\pm \pi^0)$ has direct implications for the extraction of α from $B \rightarrow \pi\pi$
 - May help understand the $K\pi$ puzzle (Gronau’s sum rule based on isospin)
 - $A_{CP}(D^\pm \rightarrow \pi^\pm \pi^0)$ may shed light on the puzzle regarding the large value of ΔA_{CP}

If BSM in $b \rightarrow c\tau\bar{\nu}$, must study $\nu\bar{\nu}$ & $\tau\tau$ modes

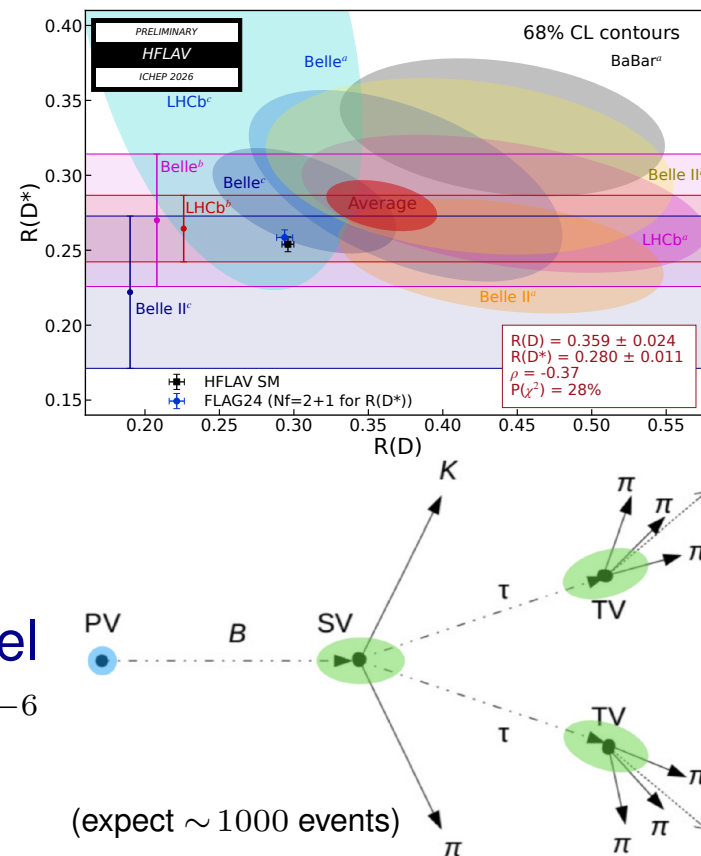
- SM and data in 3σ tension in $R(D^{(*)})$, if established, requires $\mathcal{O}(10\%)$ correction to a tree-level SM process
- If NP is charged under $SU(2)$, **unavoidable connection** to $b \rightarrow s\tau^+\tau^-$ or $b \rightarrow s\nu\bar{\nu}$ — correlations distinguish models



Only Z can measure $B \rightarrow K^*\tau^+\tau^-$, $K^*\nu\bar{\nu}$ at SM level

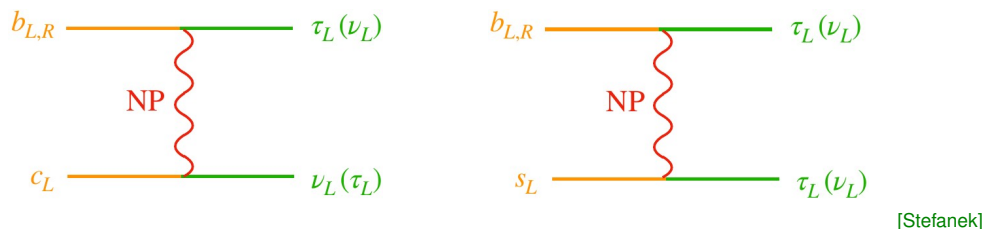
Belle II [2504.10042]: $\mathcal{B}(B \rightarrow K^*\tau^+\tau^-) < 1.8 \times 10^{-3}$ — while SM $\sim 10^{-6}$

- Boost of B in Z decay provides ideal environment



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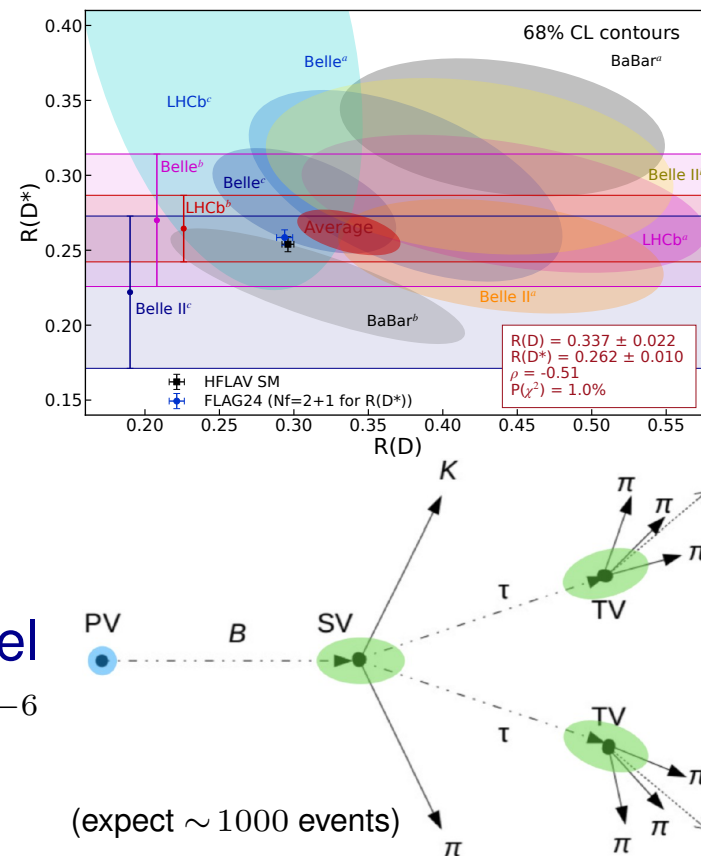
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$B_{d,s} \rightarrow \mu^+ \mu^-$: interesting at all imaginable statistics

- $\mathcal{B}_{\text{SM}}(B_s \rightarrow \mu^+ \mu^-) \sim 3 \times 10^{-9}$, BSM predictions extended orders of magnitudes higher
- $\mathcal{B}_{\text{SM}}(B_d \rightarrow \mu^+ \mu^-) \sim 10^{-10}$, LHCb expects 10% (300/fb), CMS expects 15% (3/ab)

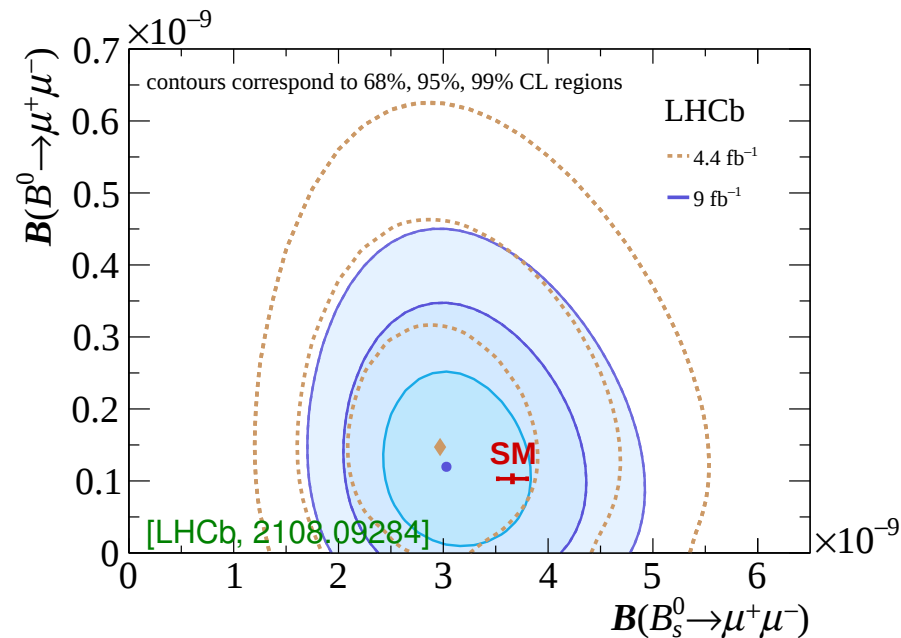
SM uncertainty $\simeq (2\%) \oplus f_{B_q}^2 \oplus \text{CKM}$, and may be further reduced

- Measure $|V_{ub}|$, using only isospin, from:

$$\mathcal{B}(B_u \rightarrow \ell \bar{\nu}) / \mathcal{B}(B_d \rightarrow \mu^+ \mu^-)$$

(Most precise $|V_{ub}|$... at FCC- hh statistics...?)

- A decay with mass-scale sensitivity (dim.-6 operator) that competes with $K \rightarrow \pi \nu \bar{\nu}$



PDG average:

[LHCb, CMS, ATLAS]

$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = (3.34 \pm 0.27) \times 10^{-9}$$

(Very) rare (semi)leptonic decays

- Unique capabilities for decays with large missing energy, i.e., ν or τ in final state
(And better than LHCb for $e^\pm$)
- Tera- Z could be the first to measure:
Many decays mediated by $b \rightarrow s\nu\bar{\nu}$ or $b \rightarrow s\tau^+\tau^-$, and their $b \rightarrow d$ counterparts
 $B \rightarrow K^{(*)0}\tau^+\tau^-$, $\Lambda_b \rightarrow \Lambda\tau^+\tau^-$, $B \rightarrow K^{(*)}\nu\bar{\nu}$, $B_s \rightarrow \phi\nu\bar{\nu}$, $\Lambda_b \rightarrow \Lambda\nu\bar{\nu}$, $B \rightarrow \pi(\rho)\nu\bar{\nu}$, etc.
- Two-body $B \rightarrow \ell^+\ell^-$ decays sensitive to very high scales (comparable to $K \rightarrow \pi\nu\bar{\nu}$)
 $B_{s,d} \rightarrow \mu^+\mu^-$: tera- Z expected to be comparable to HL-LHC
 $B_{s,d} \rightarrow \tau^+\tau^-$: tera- Z is much more sensitive: measure it, if $\geq$ SM level $[\sim 8 \times 10^{-7}]$
- Another important 2-body decay, to be measured by FCC- ee : $B_c \rightarrow \tau\bar{\nu}$

CP violation in neutral meson mixing: $A_{\text{SL}}^{d,s}$

- Only seen in K so far; In the SM: m_c^2/m_b^2 and CKM suppressions, can be lifted by BSM

[hep-ph/0202010]

$$A_{\text{SL}} = \frac{\Gamma[\bar{B}^0(t) \rightarrow \ell^+ X] - \Gamma[B^0(t) \rightarrow \ell^- X]}{\Gamma[\bar{B}^0(t) \rightarrow \ell^+ X] + \Gamma[B^0(t) \rightarrow \ell^- X]}$$

- Current status: Data: $A_{\text{SL}}^d = -(2.1 \pm 1.7) \times 10^{-3}$ $A_{\text{SL}}^s = -(0.6 \pm 2.8) \times 10^{-3}$
SM: $A_{\text{SL}}^d = -(4.7 \pm 0.6) \times 10^{-4}$ $A_{\text{SL}}^s = (2.22 \pm 0.27) \times 10^{-5}$ [1603.07770]

Plenty of room between current sensitivity and the SM predictions

(Hard to extrapolate whether LHCb becomes systematics limited)

- Unique to Tera- Z : uncertainty $\sim 2.5 \times 10^{-5}$ for both A_{SL}^d and A_{SL}^s , reach SM level

Final remarks

What are the largest useful data sets?

- No one has seriously explored it!
 - Many measurements will remain far from being limited by theory uncertainties:
 - The CKM angle $\gamma(\equiv \phi_3)$
 - $B_{s,d} \rightarrow \mu\mu$, $B \rightarrow \mu\nu$ and other leptonic decays
 - $A_{\text{SL}}^{d,s}$ — CPV in $B_{(s)}$ mixing
 - Lepton flavor violation & lepton universality violation searches
 - Dark sector searches, etc.
 - In some decays, even in 2040s we'll have $(\text{exp. bound})/\text{SM} \gtrsim 10^3$
 - NP sensitivity would improve with data $\gg$ LHCb, Belle II, $\text{tera-}Z$
- $\Rightarrow$ Case for an experiment focused on flavor at FCC- hh ...

Workshop advertisement



Flavours at FCC Workshops, next one @ CERN: Jan 19–22, 2027 [Isidori, ZL, Monteil, Wilkinson]

Goal: deepen understanding of the potential of FCC for flavor physics — Get involved!

Conclusions

- Flavor physics probes scales $\gg 1$ TeV, sensitivity limited by statistics
New physics could show up any time when measurements improve
- There is much to be learned from future measurements at LHCb, Belle II, ATLAS, CMS
- If any of the tensions with SM becomes decisive $\Rightarrow$ compelling case for largest statistics
- Interesting challenges both for experiment and theory to maximize sensitivity
Explosion of data always triggered unforeseen developments
- FCC- ee has very rich physics program, can be a discovery machine
In flavor physics, the only way to go well beyond Belle II and LHC(b)
- Clear motivations to aim for the largest data sets that technology may allow

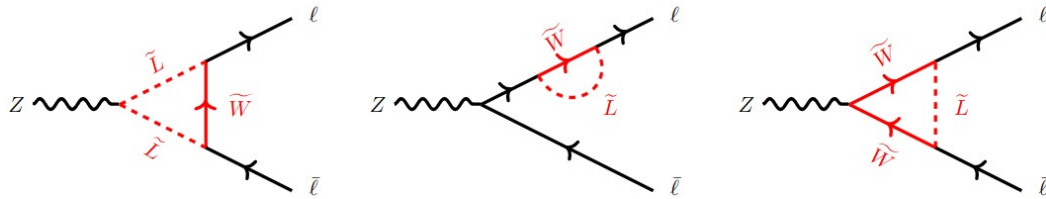


Extra slides

Actual discovery potential? E.g., SUSY in $Z \rightarrow \ell^+ \ell^-$

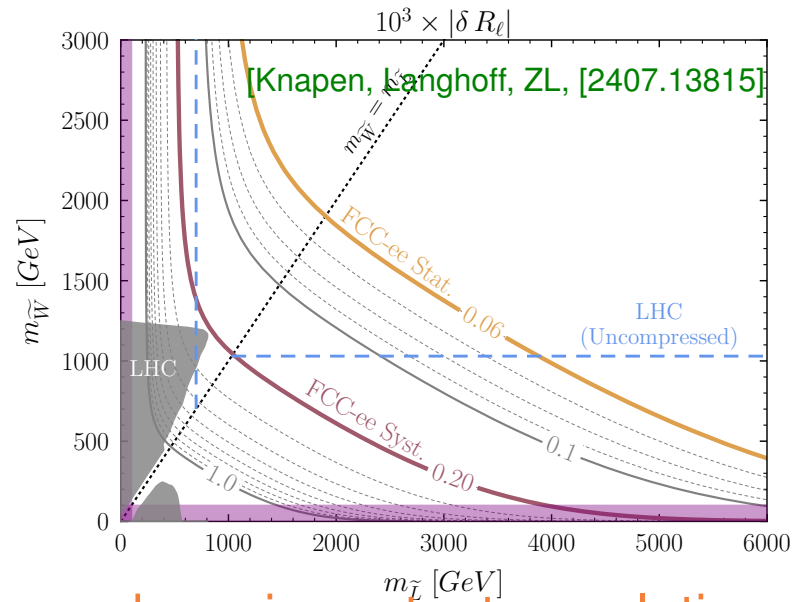
- Consider a SUSY simplified model: $\tilde{q}, \tilde{g}$ heavy, only electroweakinos & sleptons light

- Measurement:** $R_\ell = \frac{\Gamma_{\ell^+ \ell^-}}{\Gamma_{\text{hadrons}}}$
- | | | | | |
|--------------------------|---|-------------|------|-----------------------------|
| $R_\ell^Z (\times 10^3)$ | 20767 ± 25 | 0.05 | 0.05 | Ratio of hadrons to leptons |
| | Systematic limitation in Midterm Report resolved by Feasibility Study | | | Acceptance for leptons |



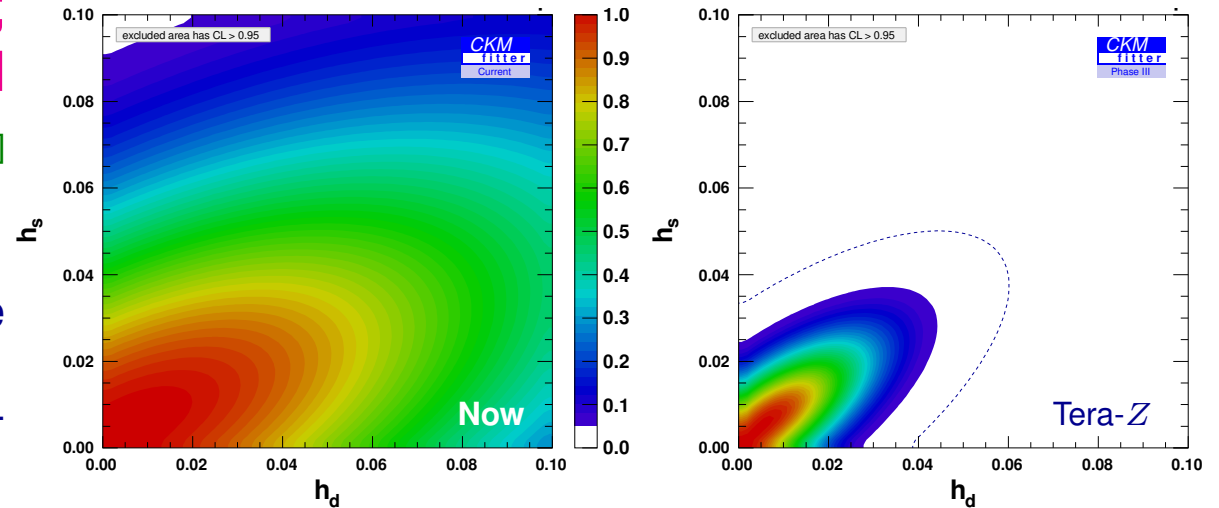
- Ultimate sensitivity depends on α_s , $\sin^2 \theta_w$, etc.
Several measurements combined for best physics reach
Even better sensitivity to flavor violating effects ($e/\mu/\tau$)

- Can probe beyond (or between) HL-LHC exclusions
- Complementary to SMEFT studies, a specific model may have important correlations

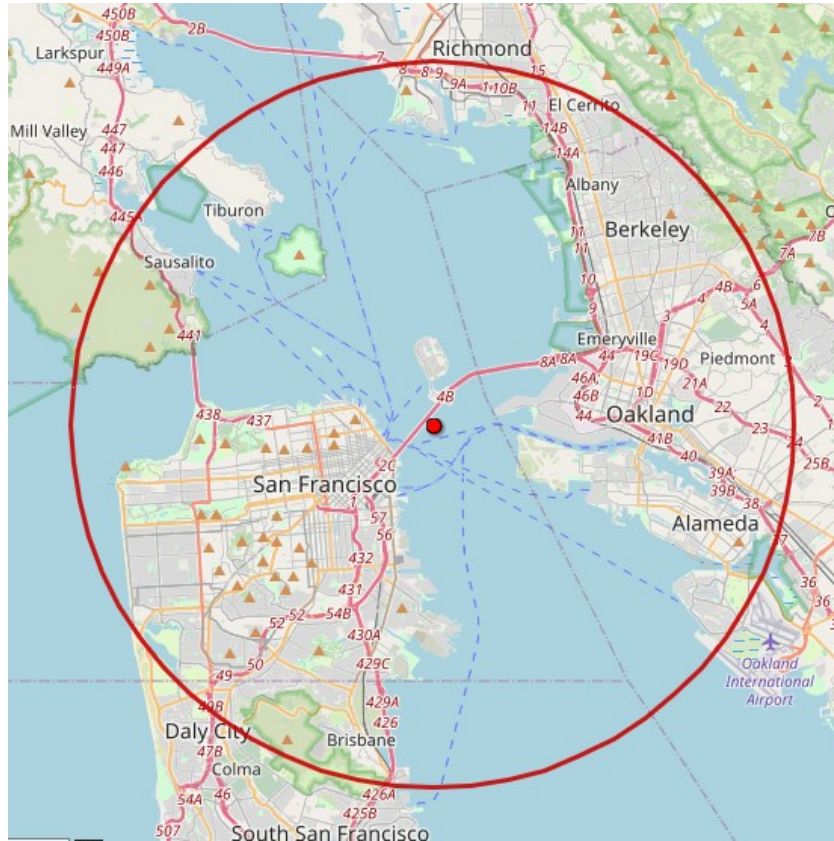


Sensitivity to new physics in B mixing

- In many BSM scenarios, dominant deviations from SM may be in neutral meson mixing
Assume: (i) 3×3 CKM matrix is unitary; (ii) tree-level decays dominated by SM
General parametrization: $h e^{2i\sigma} = A_{\text{NP}}(B^0 \rightarrow \bar{B}^0)/A_{\text{SM}}(B^0 \rightarrow \bar{B}^0)$ ($h_{d,s}, \sigma_{d,s}$: NP param's)
- CKM fit with 4 BSM param's added; combines many measurements and theory inputs [Charles *et al.*, 2006.04824]
($\Rightarrow$ conservative view of future progress)
- Sensitive to TeV scale, even if NP is MFV-like
- $|V_{cb}|$ becomes a bottleneck; Tera- Z sensitivity will be better (no LQCD extrapolations)



FCC doesn't look that big in the Bay Area



US units for FCC enthusiasts:

X mile radius $\Leftrightarrow 10X$ km circumference
(2π miles = 10 km)

Units for flavor: $m_B/\text{MeV} = \text{mile}/\text{foot}$

10^{-2} and 10^{-4} coincidences, respectively